

### **Computational models in Systems Biology**

Nicolas Le Novère





### What is Computational Systems Biology?





### What is Computational Systems Biology?

 « Je tiens impossible de connaître les parties sans connaître le tout, non plus que de connaître le tout sans connaître particulièrement les parties » Blaise Pascal, Pensées, 1660.

"[A system consists of] a dynamic order of parts and processes standing in mutual interaction. [...] The fundamental task of biology [is] the discovery of the laws of biological systems" Ludwig von Bertalanfy, Kritische Theorie der Formbildung, 1928





### What is Computational Systems Biology

For us and for today ...





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 Systems Biology is the study of a biological systems taking into account all its constituents, their relationships and their evolution





### What is Computational Systems Biology

For us and for today ...

 Systems Biology is the study of a biological systems taking into account all its constituents, their relationships and their evolution

 Computational Systems Biology is the construction of quantitative models that describe the behaviour of a system, on its own, or in response to its environment





### What is a model? A simulation?

- A model is a mathematical description of the components of a system, their relationships, and the evolution of both.
  - ordinary differential equations (system evolution) dX/dt = f(X)
  - partial differential equation (system description)  $\nabla X = g(X)$
  - $\blacksquare$  algebraic equations (conservation laws) h(X) = 0
  - probability distributions PX = i(X)
  - $\blacksquare$  master equation dPX/dt = j(PX)
  - cell automata/finite elements



# ЕМВІ-ЕВІ 🎒

### What is a model? A simulation?

- A simulation is the instantiation of a model over time, using a given algorithmic approach, and a particular software: A model can generate simulations giving different results!
  - Logical (boolean or discrete) approach
  - Deterministic approach
  - Stochastic approach
  - Fixed timesteps
  - Adaptative timesteps
  - ...
- Plus ... range of simulations
  - parameter scan
  - parameter search/optimisation
  - phase-plane analysis
  - bifurcation analysis
  - ...



# Systems Biology Markup Language

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The Systems Biology Markup Language (SBML) is a computer-readable format for representing **models of biochemical reaction networks**. SBML is applicable to metabolic networks, cell-signaling pathways, regulatory networks, and many others.

#### Internationally Supported and Widely Used

SBML has been evolving since mid-2000 through the efforts of an international group of software developers and users. Today, SBML is **supported by over 110 software systems**, including the following (where '\*' indicates SBML support in development):

CDM C:--

NATIONAL CONTRACTOR

BALSA	Dizzy	Moleculizer	SBMLSim
BASIS	E-CÉLL	Monod	SBMLToolbox
BIOCHAM	ecellJ	Narrator	SBO
BioCharon	ESS	NetBuilder	SBToolbox
ByoDyn	FluxAnalyzer	Oscill8	SBW
BioCyc	Fluxor	PANTHER Pathway	SCIpath
BioGrid	Gepasi	PathArt	Sigmoid*
BioModels	Gillespie2	Pathway Analyser	SigPath
BioNetGen	HSMB	PathwayLab	SigTran
BioPathwise	HybridSBML	Pathway Tools	SIMBA
Bio Sketch Pad	INSILICO discovery	PathwayBuilder	SimBiology
BioSens	JACOBIAN	PATIKAweb	Simpathica
BioSPICE Dashboard	Jarnac	PaVESy	SimPheny*
BioSpreadsheet	JDesigner	PET	SimWiz
BioTapestry	JigCell	PNK	SloppyCell
BioUML	JSim	PottersWheel	SmartCell
BSTLab	JWS Online	ProcessDB	SRS Pathway Editor
CADLIVE	Karyote*	PROTON	StochSim
CellDesigner	KEGG2SBML	pysbml	StochKit
Cellerator	Kineticon	PySCeS	STOCKS
Cell Illustrator	Kinsolver*	Reactome	TERANODE Suite
CellML2SBML	libSBML	RSBML	Trelis
Cellware	MathSBML	runSBML	VANTED
CL-SBML	MesoRD	SABIO-RK	Virtual Cell
CLEML	Meta-All	SBML ODE Solver	WebCell
COPASI	MetaFluxNet	SBML-PET	WinSCAMP
Cyto-Sim	MIRIAM	SBMLeditor	Xholon
Cytoscape	MMT2	SBMLmerge	XPPAUT
DBsolve	Modesto	SBMLR	

#### COPASI 4.1 Build 21 Released

(May 21, 2007) **COPASI** version 4.1 (build 21) has been released. COPASI is a free, general simulator for systems biology with a large number of features. read more

#### SBML Hackathon 2007!

(April 3, 2007) This year's **SBML Hackathon** will be held at the University of Newcastle, UK. Please join us and don't forget to register ASAP!

read more

#### VANTED supports SBML

(April 3, 2007) **VANTED** is a network editing and visualization system with features for network-integrated visualization of data from experiments and simulations.

read more

#### RSBML, a package for R

(March 29, 2007) **RSBML** is a package that allows SBML to be imported into R either as an S4 object or a Bioconductor graph object.

read more

#### Xholon supports SBML

(March 27, 2007) **Xholon** is an open-source, general-purpose modeling and simulation tool. It can read models created using UML, among other things.

read more

See older news items.

#### A Free and Open Language

http://www.jst.go.jp/kisoken/sorst/

DALCA





"The goal of SBML is to help people to disagree as precisely as possible". Ed Franck, Argonne National Laboratory







SBML is a computer readable format for representing models describing the dynamical behaviour of biological entities





### What can we encode in SBML?







### compartments

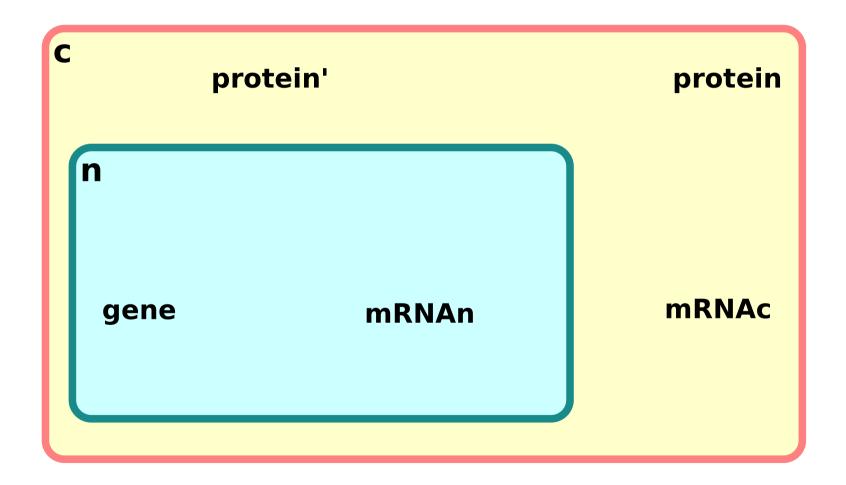
C		
n		







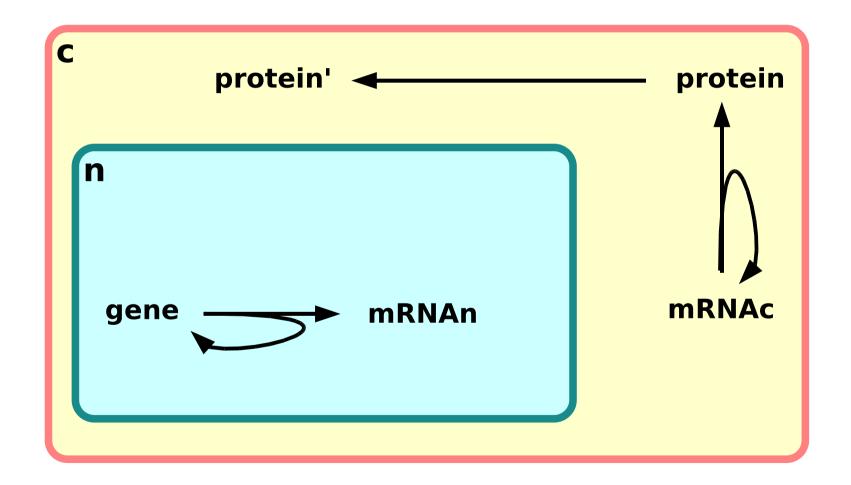
### species







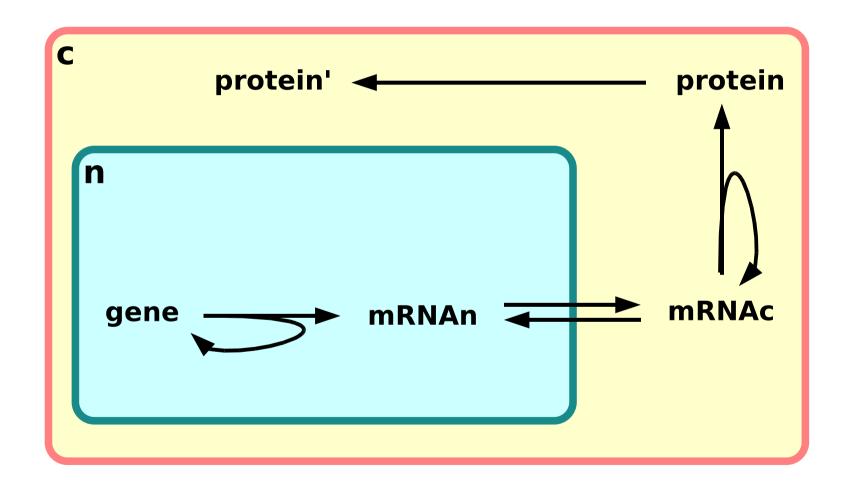
### reactions







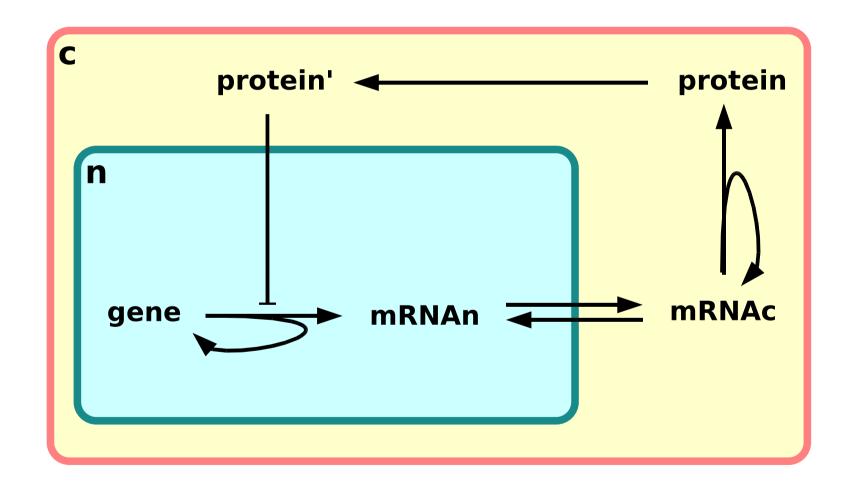
### reactions







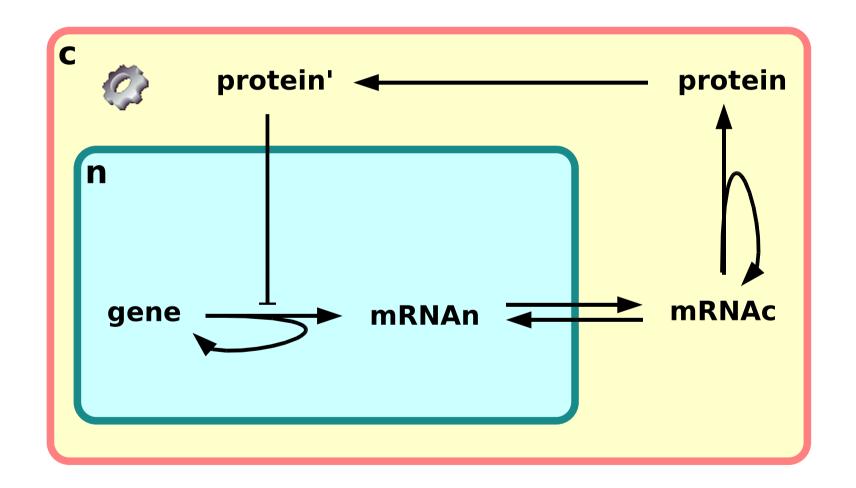
### modulations







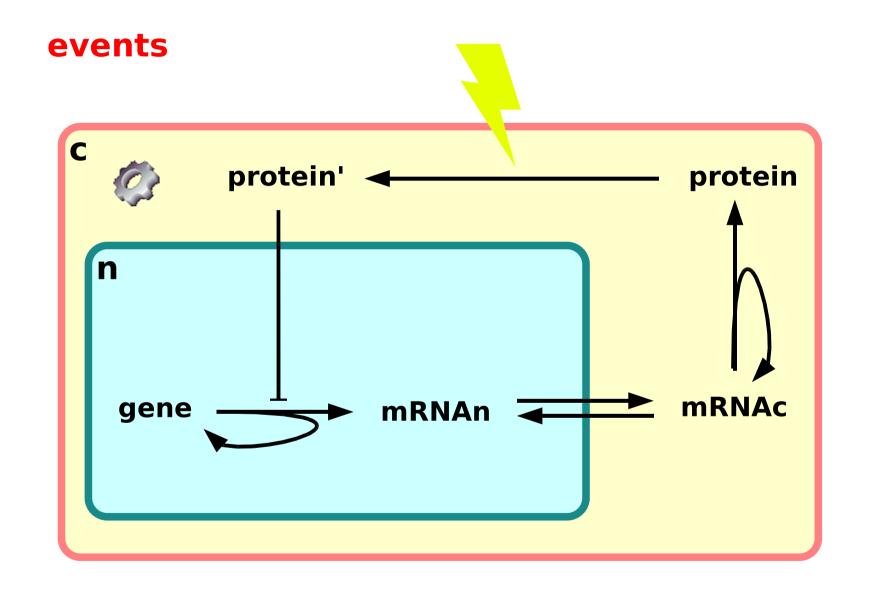
### rules















- The Systems Biology Markup Language is defined as a set of classes represented in the Unified Modelling Language (UML)
- In practise it is used as serialised using
  - An XML schema 1) lists all the elements and attributes, 2) specifies the containment relationships between them, 3) precises the datatype of each
  - An additional set of constraints is listed in the specification and implemented as a list of consistency checks



### What the heck is XML?



- The eXtensible Markup Language (XML) is a text-format that allow to define languages to store structured information
- An XML language is made-up of elements and attributes:

```
<element1 attribute1="valeur1" attribute2="valeur2">
        <element2 attribute1="valeur3" />
</element1>
```

- An XML language can be defined in another XML language called XML schema. An XML file can be transformed into something else using other XML files called XML style-sheets
- Thanks to a strict namespace system, one can build XML files using several XML languages
- There are a constellation of tools to help processing XML languages
- Most known example of XML language is XHTML, the language used to designed webpages.





```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="1" xmlns="http://www.sbml.org/sbml/level2">
        <model>
```













```
</reaction>
  </listOfReactions>
  </model>
</sbml>
```





```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="1" xmlns="http://www.sbml.org/sbml/level2">
  <model>
    <listOfCompartments>
      <compartment id="cell" />
    </listOfCompartments>
    <listOfSpecies>
      <species id="A" compartment="cell" initialConcentration="1"/>
      <species id="B" compartment="cell" initialConcentration="0"/>
    </listOfSpecies>
    <listOfParameters>
      <parameter id="kon" value="1"/>
    </listOfParameters>
    <listOfReactions>
      <reaction>
        <listOfReactants>
          <speciesReference species="A" />
        </listOfReactants>
        <listOfProducts>
          <speciesReference species="B" />
        </listOfProducts>
```

```
</reaction>
  </listOfReactions>
  </model>
</sbml>
```





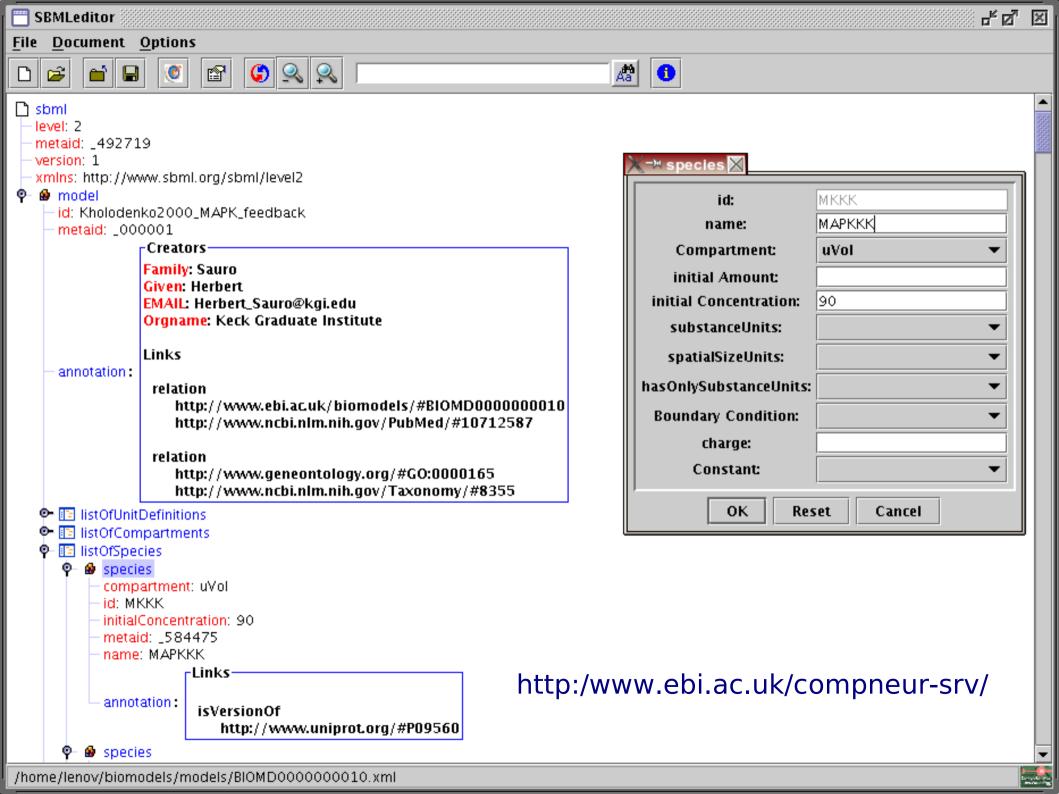
```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="2" version="1" xmlns="http://www.sbml.org/sbml/level2">
  <model>
    <listOfCompartments>
      <compartment id="cell" />
    </listOfCompartments>
    <listOfSpecies>
      <species id="A" compartment="cell" initialConcentration="1"/>
      <species id="B" compartment="cell" initialConcentration="0"/>
    </listOfSpecies>
    <listOfParameters>
      <parameter id="kon" value="1"/>
    </listOfParameters>
    <listOfReactions>
      <reaction>
        <listOfReactants>
          <speciesReference species="A" />
        </listOfReactants>
        <listOfProducts>
          <speciesReference species="B" />
        </listOfProducts>
        <kineticLaw>
          <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
              <times />
              <ci>kon</ci>
              <ci>A</ci>
              <ci>ci>cell</ci>
            </apply>
          </kineticLaw>
      </reaction>
    </listOfReactions>
  </model>
</sbml>
```





### A more realistic example ...

```
<species</pre>
    id="A"
    name="\alpha-tubulin"
    compartment="cell"
    initialAmount="1000"
    substanceUnits="item"
    hasOnlySubstanceUnits="true"
    boundaryCondition="true"
    constant="false"
    charge="0"
    metaid="PX" >
  <notes>
    <body xmlns="http://www.w3.org/1999/xhtml">
      One of the components of microtubule
    </body>
  </notes>
  <annotation>
    <rdf:RDF
        xmlns:bqbiol="http://biomodels.net/biology-qualifiers/"
        xmlns:bqmodel="http://biomodels.net/model-qualifiers/"
        xmlns:rdf="http://www.w3.org/1999/02/22-rdf-syntax-ns#">
      <rdf:Description rdf:about="#PX">
        <bqbiol:is>
          <rdf:Bag>
            <rdf:li rdf:resource="http://www.uniprot.org/#P68370"/>
            <rdf:li rdf:resource="http://www.geneontology.org/#G0:0045298"/>
          </rdf:Bag>
        </bqbiol:is>
      </rdf:Description>
    </rdf:RDF>
  </annotation>
</species>
```





### **SBML** is not limited to biochemistry!

- Rate Rules can describe the temporal evolution of <u>any</u> <u>quantitative parameter</u>, e.g. transmembrane voltage;
- Events can describe any discontinuous change, e.g. neurotransmitter release;
- A species is an entity participating to a reaction, not always a chemical entity:
  - It can be a molecule
  - It can be a cell
  - It can be an organ
  - It can be an organism
- → Remember, Systems Biology is scale-free!







- Released on June 16<sup>th</sup> 2007
- Simpler and cleaner (units ...)
- Generic entities (compartmentType, speciesType)
  - → path to generalised reactions
- Constraints and initialAssignments
- Controlle annotations (MIRIAM + SBO)
- Backward compatible with Level 2 Version 1
- More detailed and bug-free specification ... 164 pages, 10pt, small margin.





- Modular SBML, with core + optional packages
- Graph Layout
- Generalised reactions (probable)
- Model composition (probable)
- Complex species (probable)
- Arrays or sets (maybe)
- Geometry (maybe)
- Movements (maybe)
- Dynamic compartments (maybe)
- ????



## ЕМВС-ЕВІ 🎒

### What is BioModels Database?

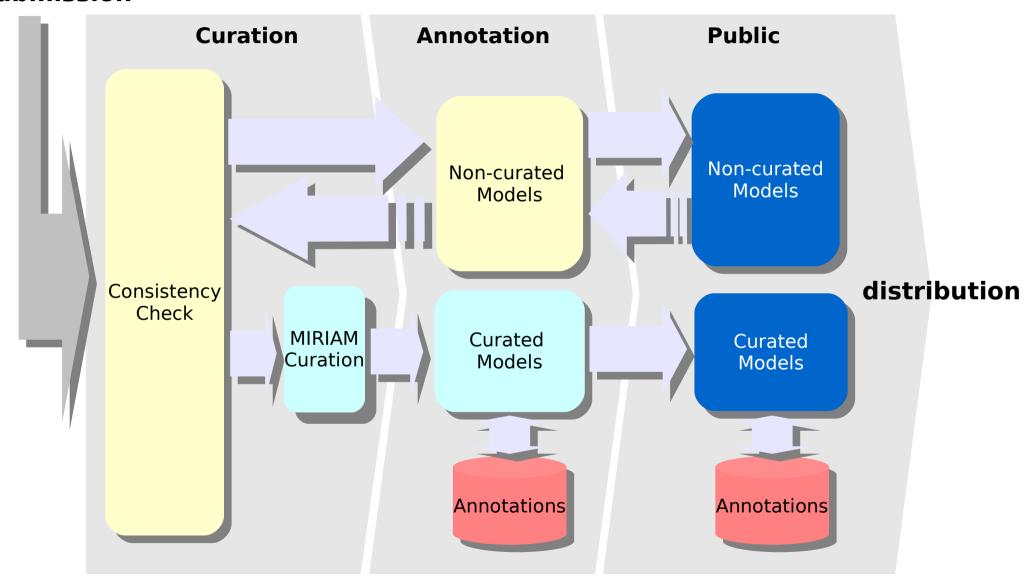
- Store and serve quantitative models of biomedical interest
- Only models described in the peer-reviewed scientific literature.
- Models are curated: computer software check the syntax, while human curators check the semantics.
- Models are simulated to check the reference correspondence
- Model components are annotated, to improve identification and retrieval.
- Models are accepted in several formats, and served in several others.
- Aims to be the "UniProt" of quantitative modelling.



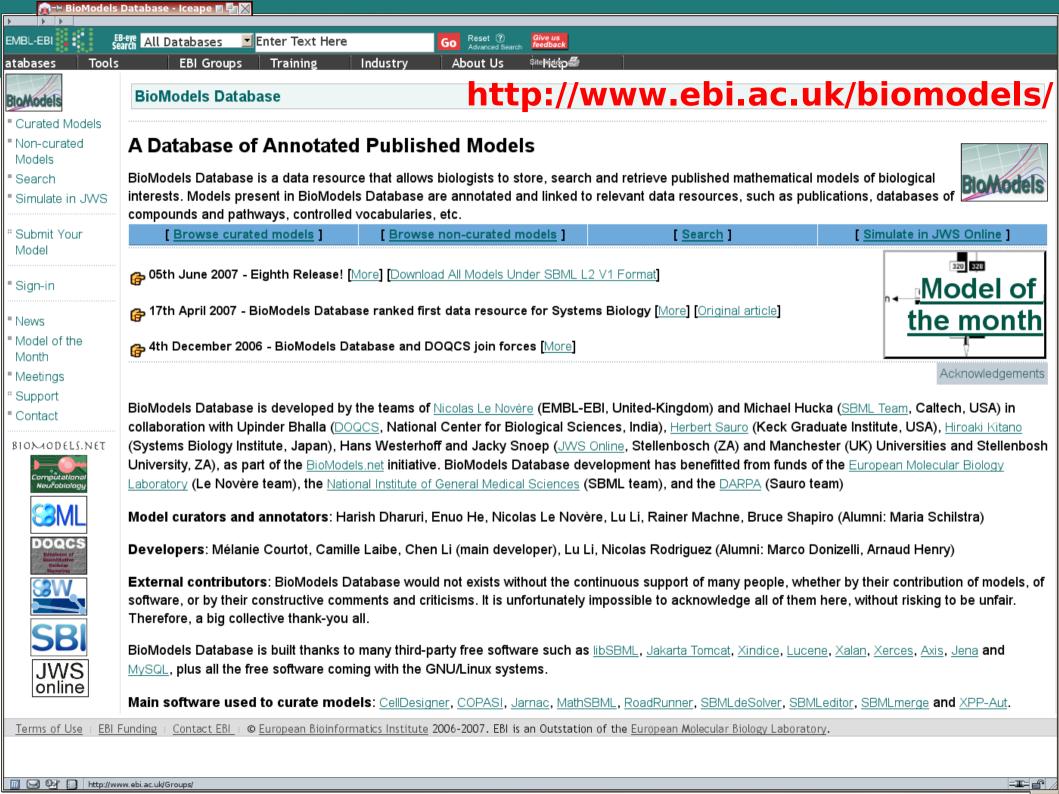


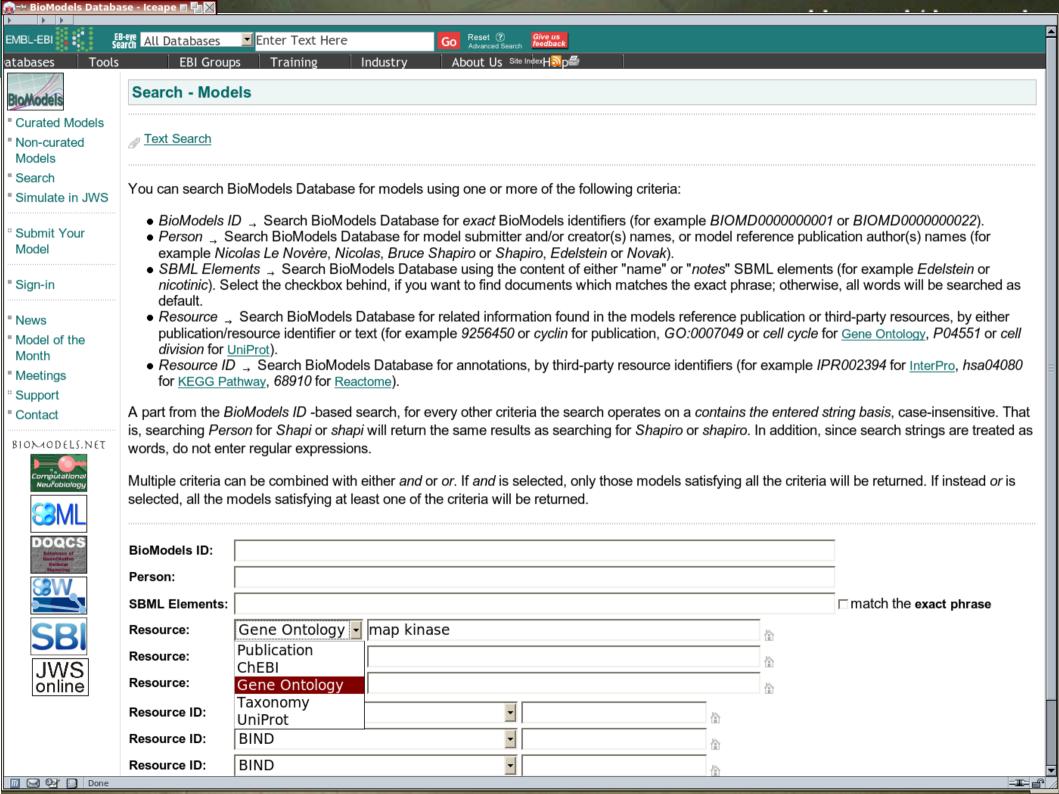


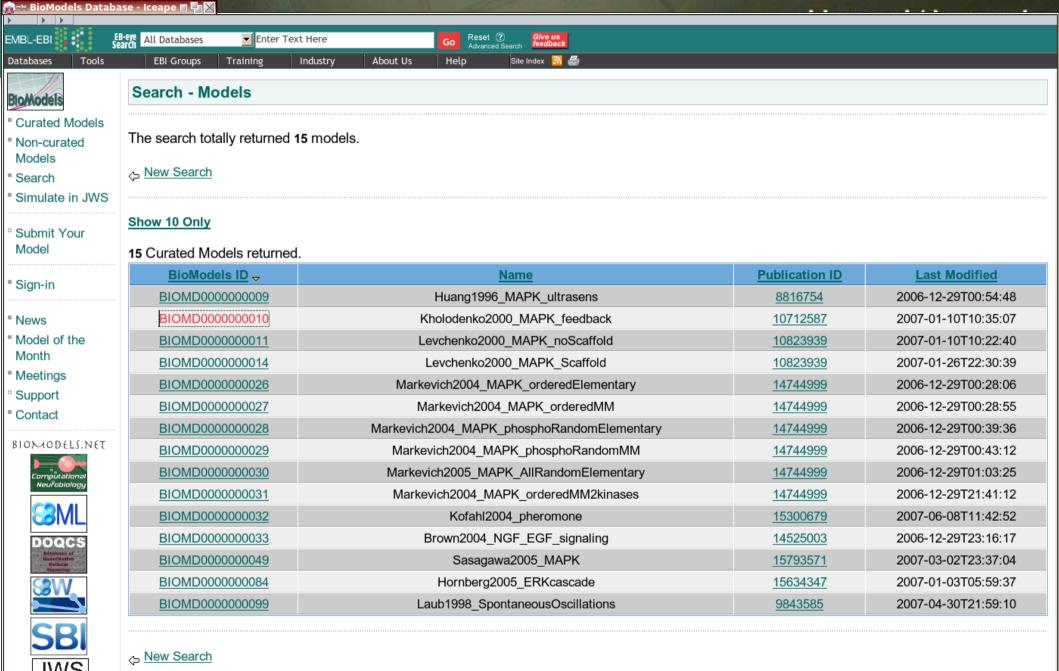
### **Submission**





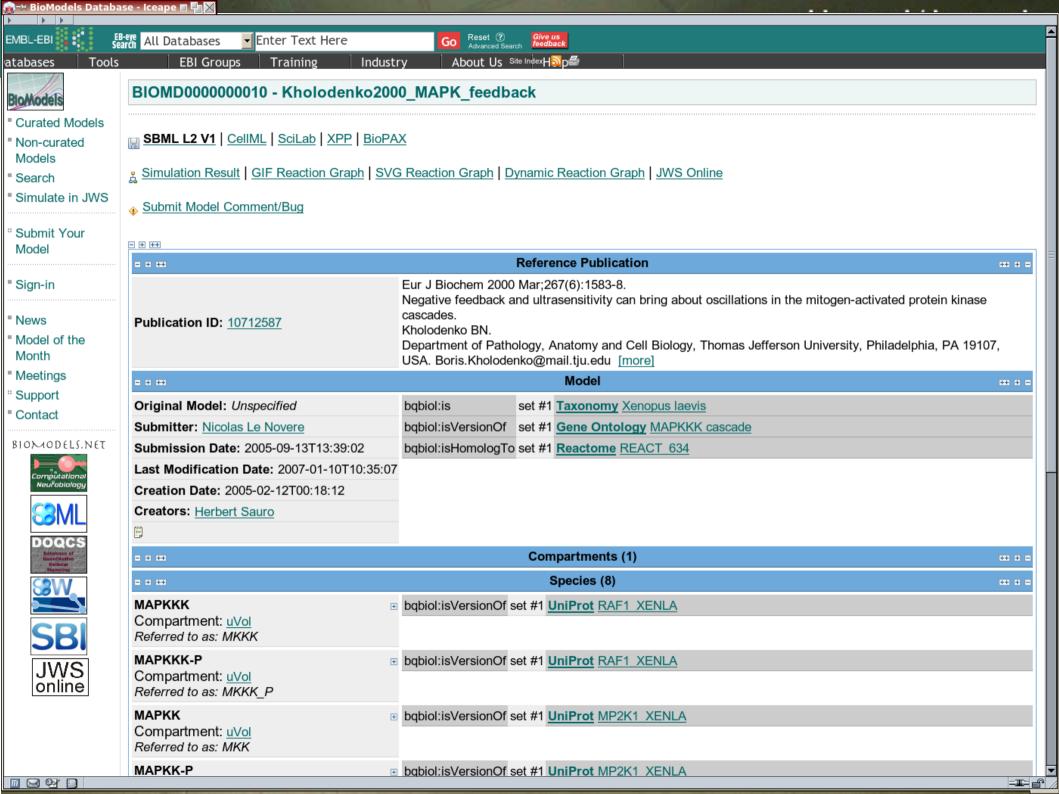


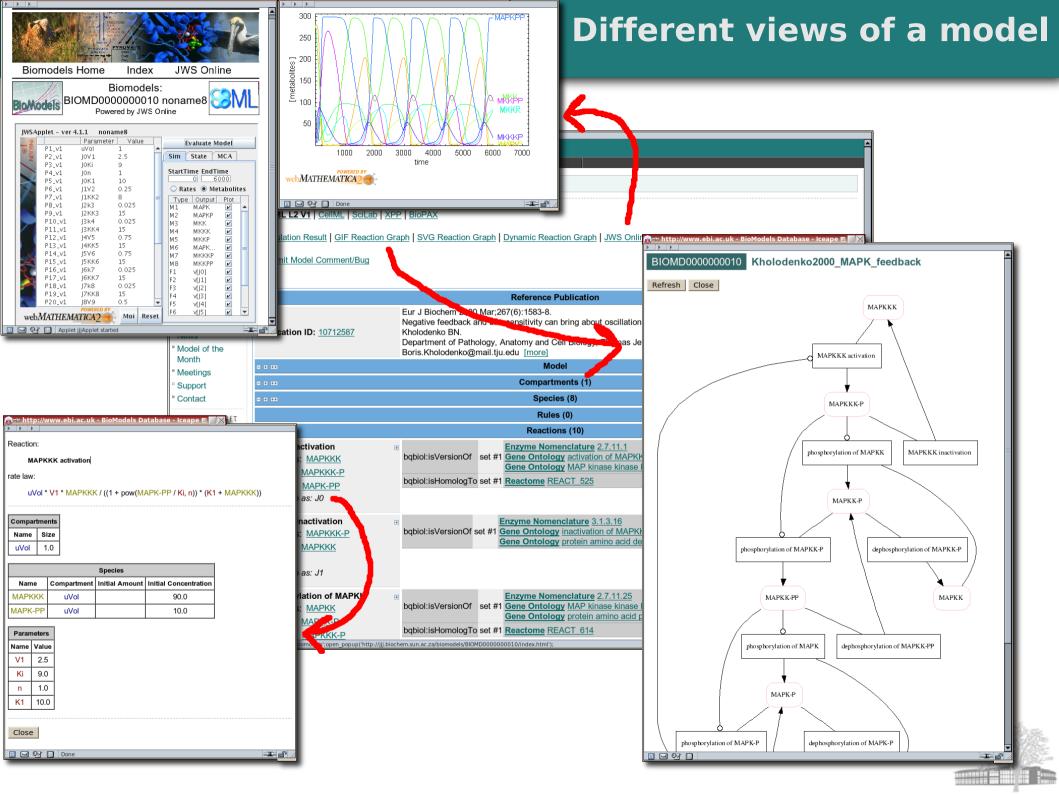


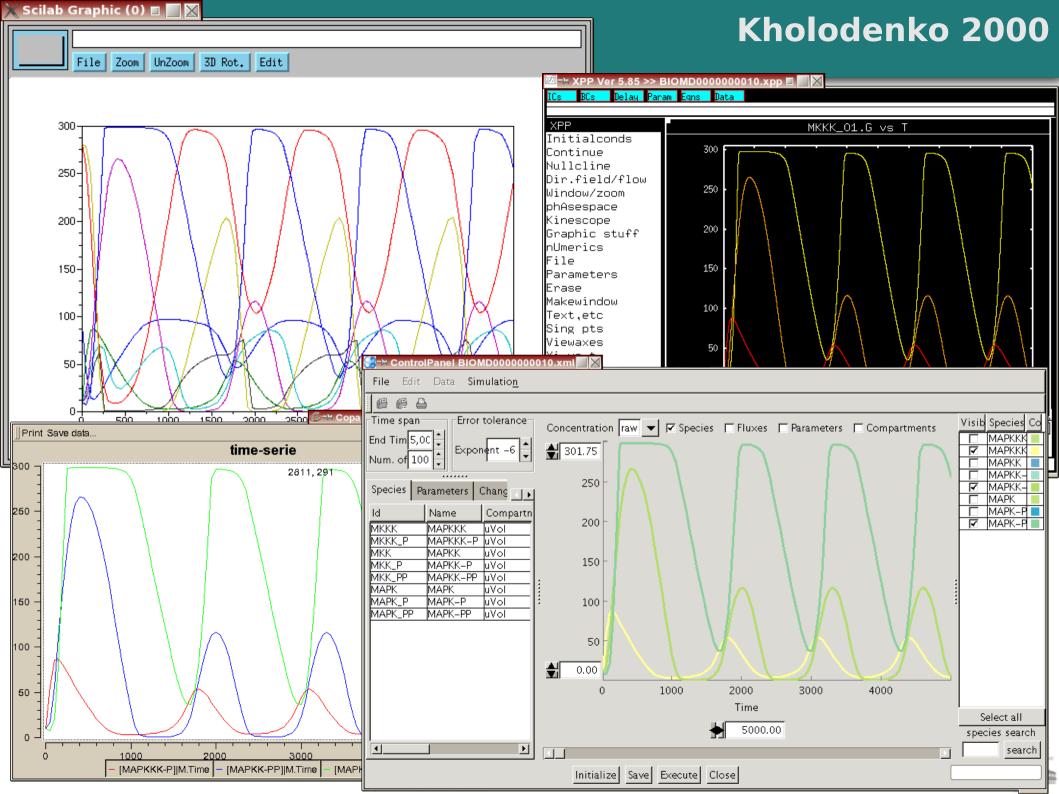


EBI Funding : Contact EBI : © European Bioinformatics Institute 2006-2007. EBI is an Outstation of the European Molecular Biology Laboratory.

online









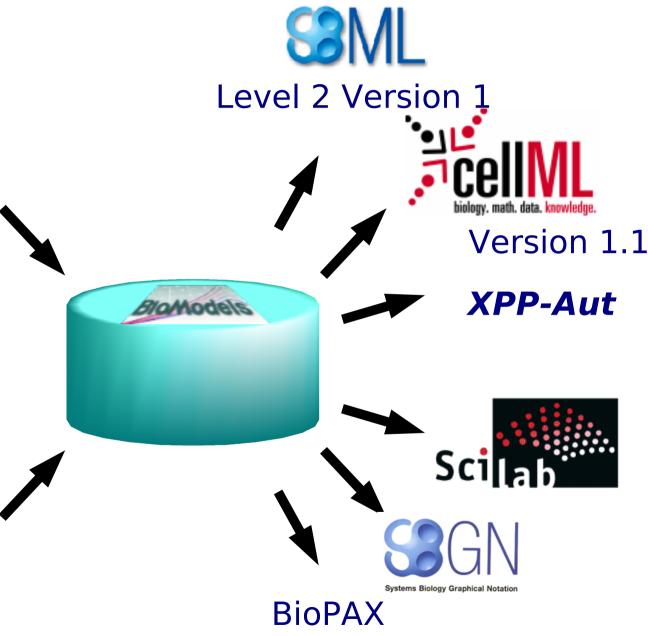
#### **BioModels DB and interoperability in CSB**



Level 1 Version 1 Level 1 Version 2 Level 2 Version 1



Version 1.0 Version 1.1







#### The BioModels Database team

Nicolas Le Novère





Michael Hucka

#### **Development**

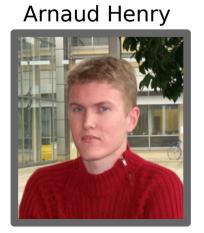
Marco Donizelli



Chen Li



Lu Li



**Curation** Harish Dharuri

**Bruce Shapiro** 



Enuo He



Rainer Machne



## ЕМВІ-ЕВІ

#### An international collaboration

- EBI
  - Nicolas Le Novère
  - Mélanie Courtot
  - Marco Donizelli
  - Arnaud Henry
  - Christian Knuepfer
  - Chen Li
  - Lu Li
  - Camille Laibe
  - Nicolas Rodriguez
  - Alexander Broicher
- SBML team (Caltech)
  - Michael Hucka
  - Andrew Finney
  - Benjamin Borstein
  - Harish Dharuri
  - Enuo He
  - Sarah Keating
  - Maria Schilstra
  - Bruce Shapiro

- NCBS (Bangalore)
  - Upinder Bhalla
  - Harsha Rani
- University of Washington
  - Herbert Sauro
- Vienna TBI
  - Rainer Machne
  - Christof Flamm
  - James Lu
- Systems Biology Institute (Tokyo)
  - Hiroaki Kitano
  - Akira Funahashi

- Journals supporting BioModels Database
  - Molecular Systems Biology
  - All PLoS Journals
  - All BioMedCentral Journals
- Programs used for curation
  - CellDesigner/SBMLodeSolver
  - COPASI
  - Jarnac/JDesigner
  - MathSBML
  - RoadRunner
  - SBMLeditor
  - XPP-Aut
- The community of Systems Biology for (Stellenbosh+Amsterdam) their contributions of models and comments.
  - Jacky Snoep
  - Hans Westerhoff













We will use COPASI, developed by: Virginia Bioinformatics Institute European Medial Laboratory

http://www.copasi.org/

Download:

http://www.copasi.org/tiki-index.php?page=SecureDownload

documentation:

http://www.copasi.org/static/userguide/copasi.xhtml





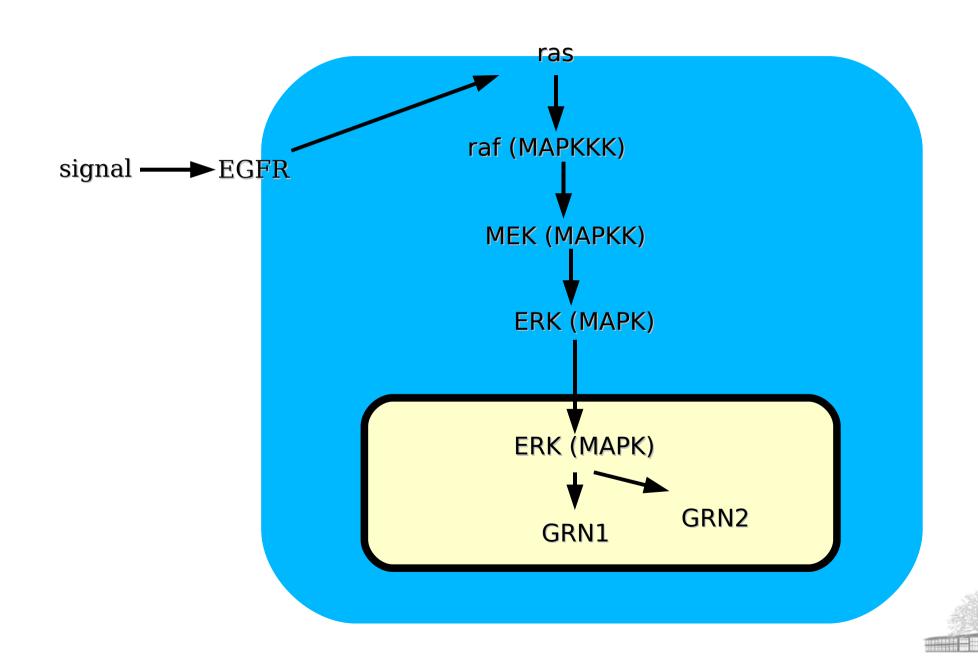




- Mitogen Activated Protein kinase
   ->mitosis, differentiation, cell survival, apoptosis
   => CANCER
- Integration of many signalling pathways
- Activation of many regulatory networks
- Model systems in computational biology









Proc. Natl. Acad. Sci. USA Vol. 78, No. 11, pp. 6840-6844, November 1981 Biochemistry

## An amplified sensitivity arising from covalent modification in biological systems

1 of 5

(protein modification/metabolic regulation/switch mechanism/enzyme cascades)

ALBERT GOLDBETER<sup>†</sup> AND DANIEL E. KOSHLAND, JR.

Department of Biochemistry, University of California, Berkeley, California 94720

Contributed by Daniel E. Koshland, Jr., August 11, 1981

ABSTRACT The transient and steady-state behavior of a reversible covalent modification system is examined. When the modifying enzymes operate outside the region of first-order kinetics, small percentage changes in the concentration of the effector controlling either of the modifying enzymes can give much larger percentage changes in the amount of modified protein. This amplification of the response to a stimulus can provide additional sensitivity in biological control, equivalent to that of allosteric proteins with high Hill coefficients.

Biological systems must respond to internal and external variations such as the depletion of nutrients, the variations in hormone levels, and the reception of sensory signals. The stimuli are processed to change the activities of enzymes controlling pathways in the biological system. Two basic phenomena play a large role in this processing: allosteric changes in protein conformation and covalent modification of proteins.

Since the findings of Cari and Croon (1) and Krobs and

ture of covalent regulation was possible, if the differential equations could be solved analytically outside the first-order region.

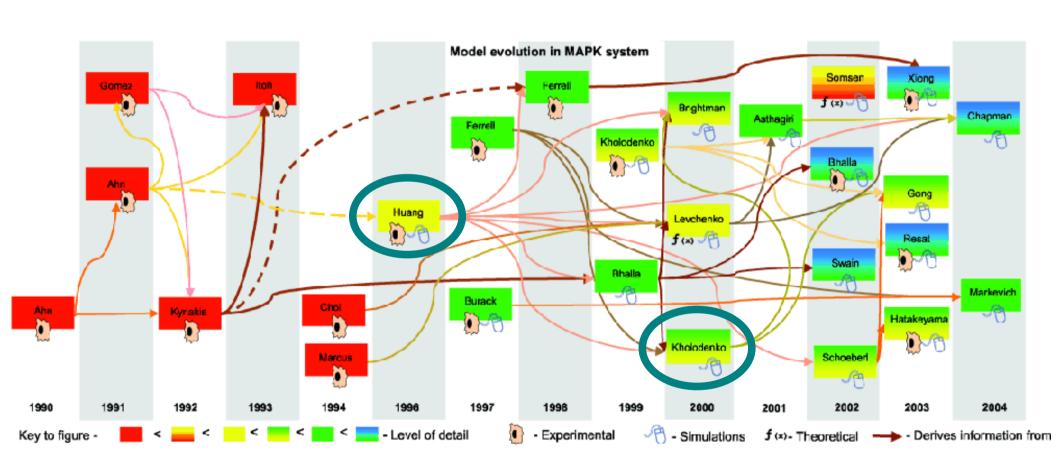
This analysis has been achieved, and the results reveal that there is an added sensitivity inherent in covalent modification schemes when one or more of the converter enzymes operate in the "zero-order" region—i.e., region of saturation with respect to protein substrate. Thus there is a property of covalent systems that, in the absence of allosteric cooperativity and multiple inputs, can generate sensitivity equivalent to cooperative enzymes with high Hill coefficients. The derivations leading to and the implications of this finding are discussed below. For convenience, we shall use the term "ultrasensitivity" to describe an output response that is more sensitive to change in stimulus than the hyperbolic (Michaelis—Menten) equation.

#### Steady-state behavior of modification system

We shall consider a covalent modification system in which a



#### **History of MAPK models**

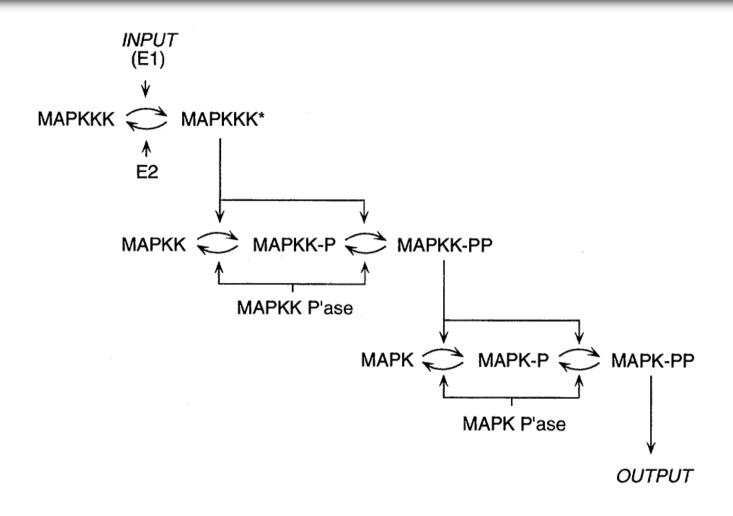


Vayttaden, Ajay, Bhalla (2004) A spectrum of models of signalling pathways. *Chembiochem* 5: 1365-1374.





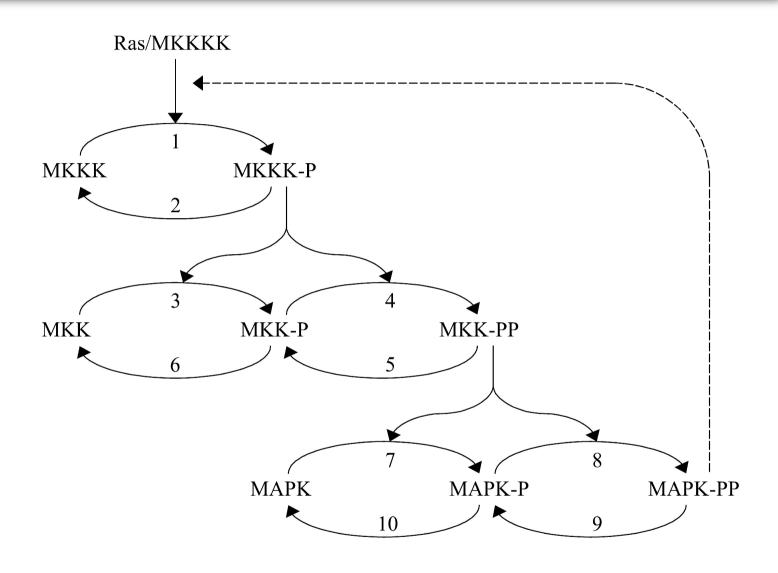
#### **Huang and Ferrell**



Huang and Ferrell (1996) Ultrasensitivity in the mitogen-activated protein kinase cascade. *Proc Natl Acad Sci USA* 93: 10078-10083.







Kholodenko (2000) Negative feedback and ultrasensitivity can bring about oscillations in the mitogen-activated protein kinase cascades. *Eur J Biochem* 267: 1583-1588.





E+S 
$$\frac{kds}{kas}$$
 ES  $\frac{kcat}{kcat'}$  EP  $\frac{kap}{kdp}$  E+P  $\frac{d[P]}{dt} = kdp[EP] - kap[E][P]$ 





E+S 
$$kas$$
 ES  $kcat$  EP  $kap$  E+P  $d[P]$  =  $kdp[EP] - kap[E][P]$ 

E+S  $kas$  ES  $kcat$  EP  $kap$  E+P  $ap[E][P]$  catalysis irreversible





E+S 
$$\stackrel{\text{kds}}{\longleftarrow}$$
 ES  $\stackrel{\text{kcat}}{\longleftarrow}$  EP  $\stackrel{\text{kap}}{\longleftarrow}$  E+P  $\stackrel{\text{d[P]}}{\longrightarrow}$  = kdp[EP] - kap[E][P]

E+S 
$$\stackrel{\text{kds}}{\longleftarrow}$$
 ES  $\stackrel{\text{kcat}}{\longleftarrow}$  EP  $\stackrel{\text{kap}}{\longleftarrow}$  E+P catalysis irreversible

product is consumed before rebinding





E+S 
$$\stackrel{\text{kds}}{\longleftarrow}$$
 ES  $\stackrel{\text{kcat}}{\longleftarrow}$  EP  $\stackrel{\text{kap}}{\longleftarrow}$  E+P  $\stackrel{\text{d[P]}}{\longrightarrow}$  = kdp[EP] - kap[E][P]

E+S 
$$\stackrel{\text{kds}}{\longleftarrow}$$
 ES  $\stackrel{\text{kcat}}{\longleftarrow}$  EP  $\stackrel{\text{kap}}{\longleftarrow}$  E+P catalysis irreversible

$$E+S \xrightarrow{ksa} ES \xrightarrow{kcat} E+P$$

product is consumed before rebinding

$$S \longrightarrow P$$
 steady-state

$$\frac{d[P]}{dt} = \frac{[E] \text{ kcat}}{Km}$$

$$1 + \frac{[S]}{[S]}$$





E+S 
$$\frac{kds}{kas}$$
 ES  $\frac{kcat}{kcat'}$  EP  $\frac{kap}{kdp}$  E+P  $\frac{d[P]}{dt} = kdp[EP] - kap[E][P]$ 

$$E+S \xrightarrow{kds} ES \xrightarrow{kcat} EP \xrightarrow{kap} E+P$$
 catalysis irreversible

# $E+S \xrightarrow{ksa} ES \xrightarrow{kcat} E+P$

### **Huang and Ferrell**

product is consumed before rebinding

$$\frac{d[P]}{dt} = \frac{[E] \text{ kcat}}{Km}$$
Kholodenko

Kholodenko





#### Briggs-Haldane (Michaelis-Menten)

$$E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$$

$$k_{-1}$$

$$\frac{d[P]}{dt} = k_2[ES]$$

$$[E] = [E_0] - [ES]$$

$$[ES] = \frac{([E_0] - [ES])[S]}{K_m}$$

$$[ES]\frac{K_m}{[S]} = [E_0] - [ES]$$

$$[ES](1 + \frac{K_m}{[S]}) = [E_0]$$

$$[ES] = [E_0] \frac{1}{1 + \frac{K_m}{|S|}}$$

$$\frac{d[P]}{dt} = k_2[E_0] \frac{[S]}{K_m + [S]} = V_{max} \frac{[S]}{K_m + [S]}$$

$$[ES] = \frac{k_1[E][S]}{k_{-1} + k_2}$$

$$K_m = \frac{k_{-1} + k_2}{k_1}$$

$$[ES] = \frac{[E][S]}{K_m}$$







$$E + S \xrightarrow{k_1} ES \xrightarrow{k_2} E + P$$

$$k_{-1}$$

$$\frac{d[ES]}{dt} = k_1[E][S] - k_{-1}[ES] - k_2[ES] = 0$$

#### steady-state!!!

$$[ES] = \frac{k_1[E][S]}{k_{-1} + k_2}$$

$$K_m = \frac{k_{-1} + k_2}{k_1}$$

$$[ES] = \frac{[E][S]}{K_m}$$

$$\frac{d[P]}{dt} = k_2[ES]$$

$$[E] = [E_0] - [ES]$$

$$[ES] = \frac{([E_0] - [ES])[S]}{K_m}$$

$$[ES]\frac{K_m}{[S]} = [E_0] - [ES]$$

$$[ES](1 + \frac{K_m}{[S]}) = [E_0]$$

$$[ES] = [E_0] \frac{1}{1 + \frac{K_m}{[S]}}$$

$$\frac{d[P]}{dt} = k_2[E_0] \frac{[S]}{K_m + [S]} = V_{max} \frac{[S]}{K_m + [S]}$$

