

Path2Models

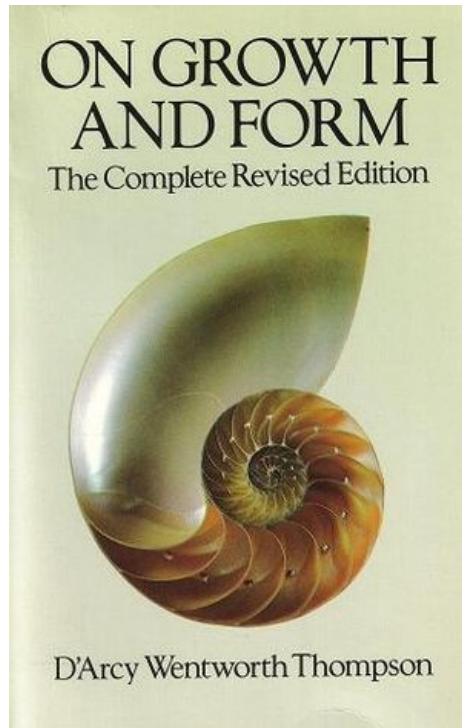
Large-scale harnessing of pathway knowledge to provide pump-priming models for all

<http://arxiv.org/abs/1307.7005>

*Nicolas Le Novère, Babraham Institute
n.lenovere@gmail.com*

Why using mathematical models?

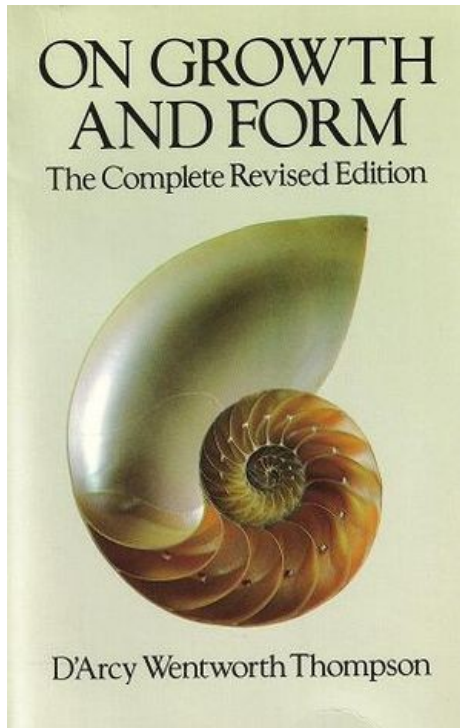
Describe



1917

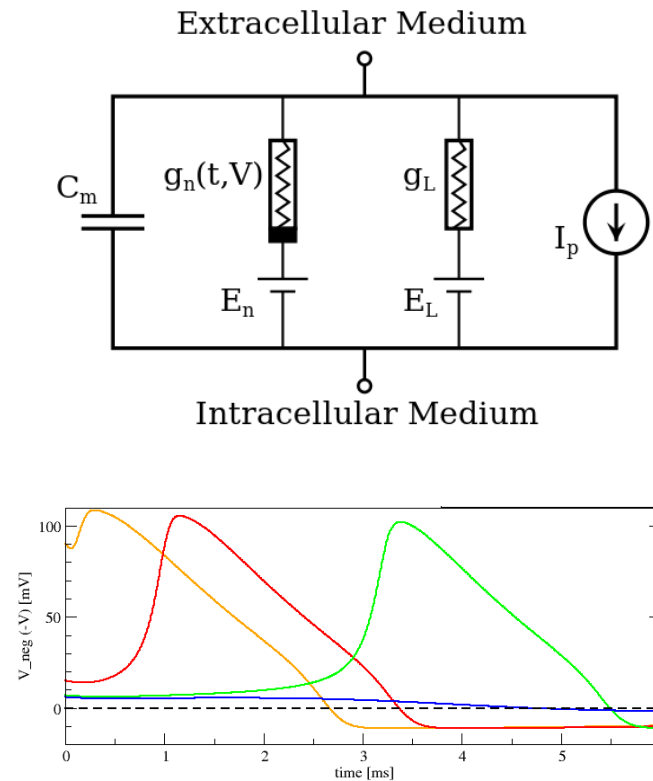
Why using mathematical models?

Describe



1917

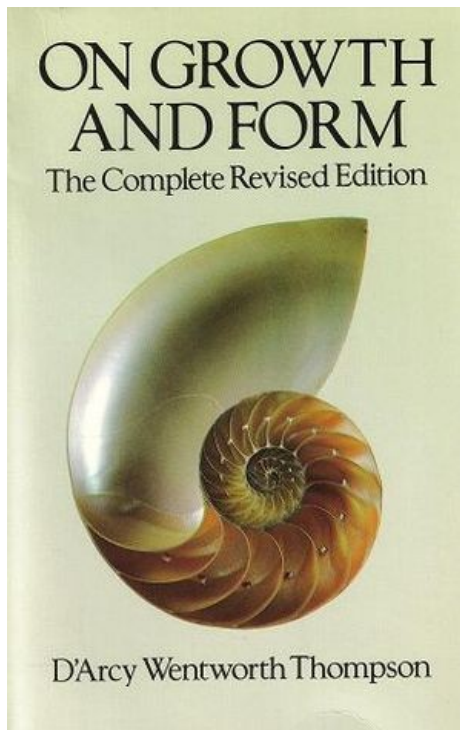
Explain



1952

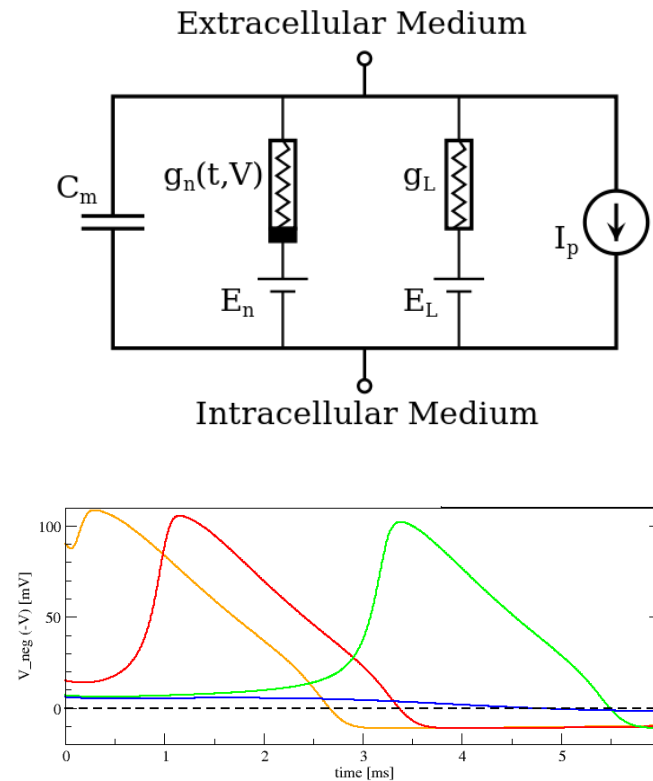
Why using mathematical models?

Describe



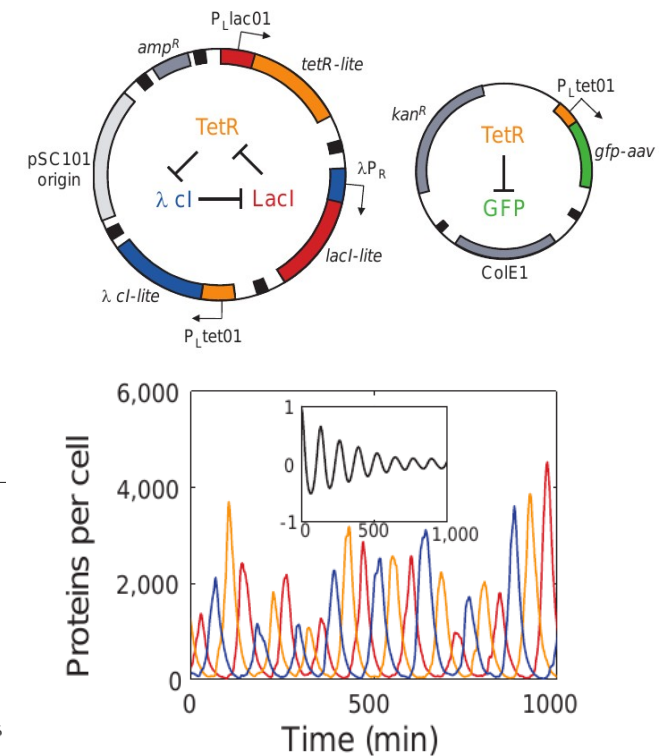
1917

Explain



1952

Predict



2000

What is a mathematical model?

Wikipedia (October 14th 2013): “A mathematical model is a description of a **system** using **mathematical** concepts and language.”

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variables

$[x]$

$V_{\max}$

K_d

EC_{50}

length

$t_{1/2}$

**What we want to know
or compare with experiments**

What is a mathematical model?

Wikipedia (October 14th 2013): “A mathematical model is a description of a **system** using **mathematical** concepts and language.”

variables

$[X]$

$V_{\max}$

K_d

EC_{50}

length

$t_{1/2}$

relationships

$$K_d = \frac{[A] \cdot [B]}{[AB]}$$

$$d[X]/dt = k \cdot [Y]^2$$

$$\sum_i [X]_i - F(t) = 0$$

$$k(t) \sim N(k, \sigma^2)$$

If $\text{mass}_t > \text{threshold}$
then $\text{mass}_{t+\Delta t} = 0.5 \cdot \text{mass}$

**What we already know
or want to test**

What is a mathematical model?

Wikipedia (October 14th 2013): “A mathematical model is a description of a **system** using **mathematical** concepts and language.”

variables

[x]

Vmax

Kd

EC₅₀

length

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relationships

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If $\text{mass}_t > \text{threshold}$
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constraints

$$[x] > 0$$

Energy conservation

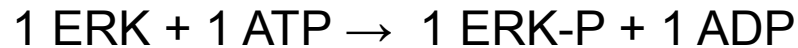
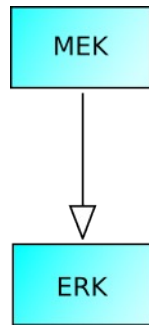
Boundary conditions
(v < upper limit)

Objective functions
(maximise ATP)

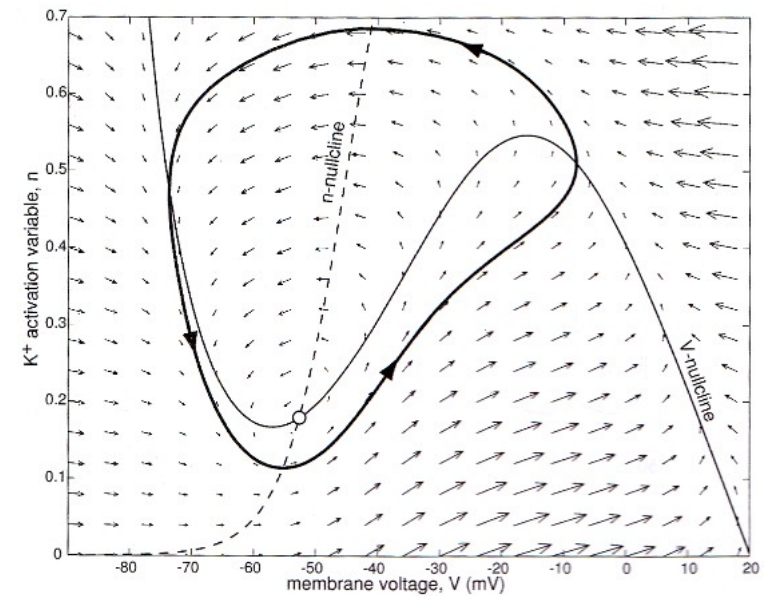
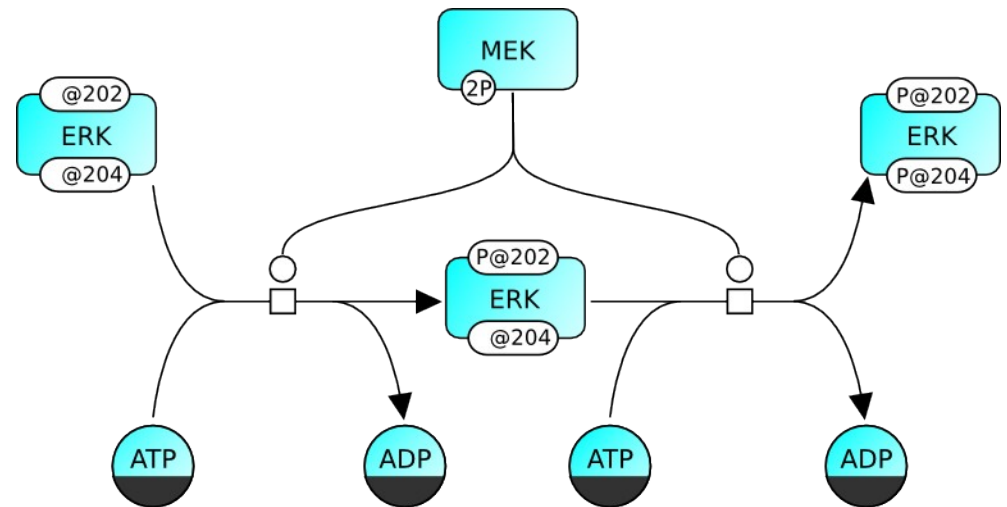
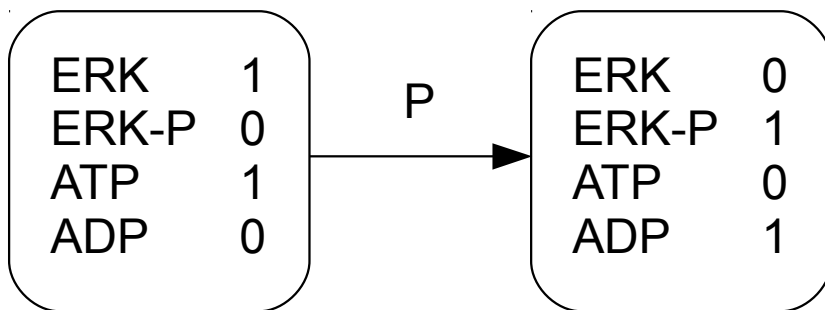
Initial conditions

**The context or what
we want to ignore**

Many levels of “modelling”



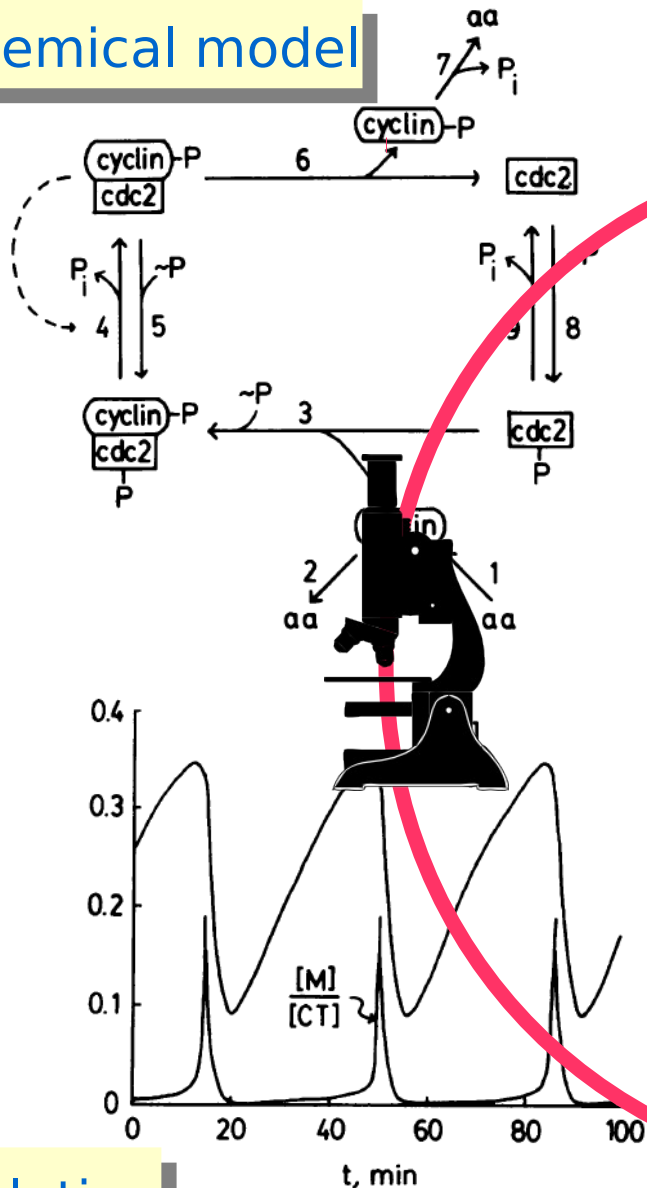
$$\frac{d[\text{ERK} - \text{P}]}{dt} = V_{\max} \frac{[\text{ERK}]}{K_m + [\text{ERK}]}$$



The models I am talking about

biochemical model

mathematical model



$$\begin{aligned} \frac{d[C2]}{dt} &= k_6[M] - k_8[\sim P][C2] + k_9[CP] \\ \frac{d[CP]}{dt} &= -k_3[CP][Y] + k_8[\sim P][C2] - k_9[CP] \\ \frac{d[pM]}{dt} &= k_3[CP][Y] - [pM]F([M]) + k_5[\sim P][M] \\ \frac{d[M]}{dt} &= [pM]F([M]) - k_5[\sim P][M] - k_6[M] \\ \frac{d[Y]}{dt} &= k_1[aa] - k_2[Y] - k_3[CP][Y] \\ \frac{d[YP]}{dt} &= k_6[M] - k_7[YP] \end{aligned}$$

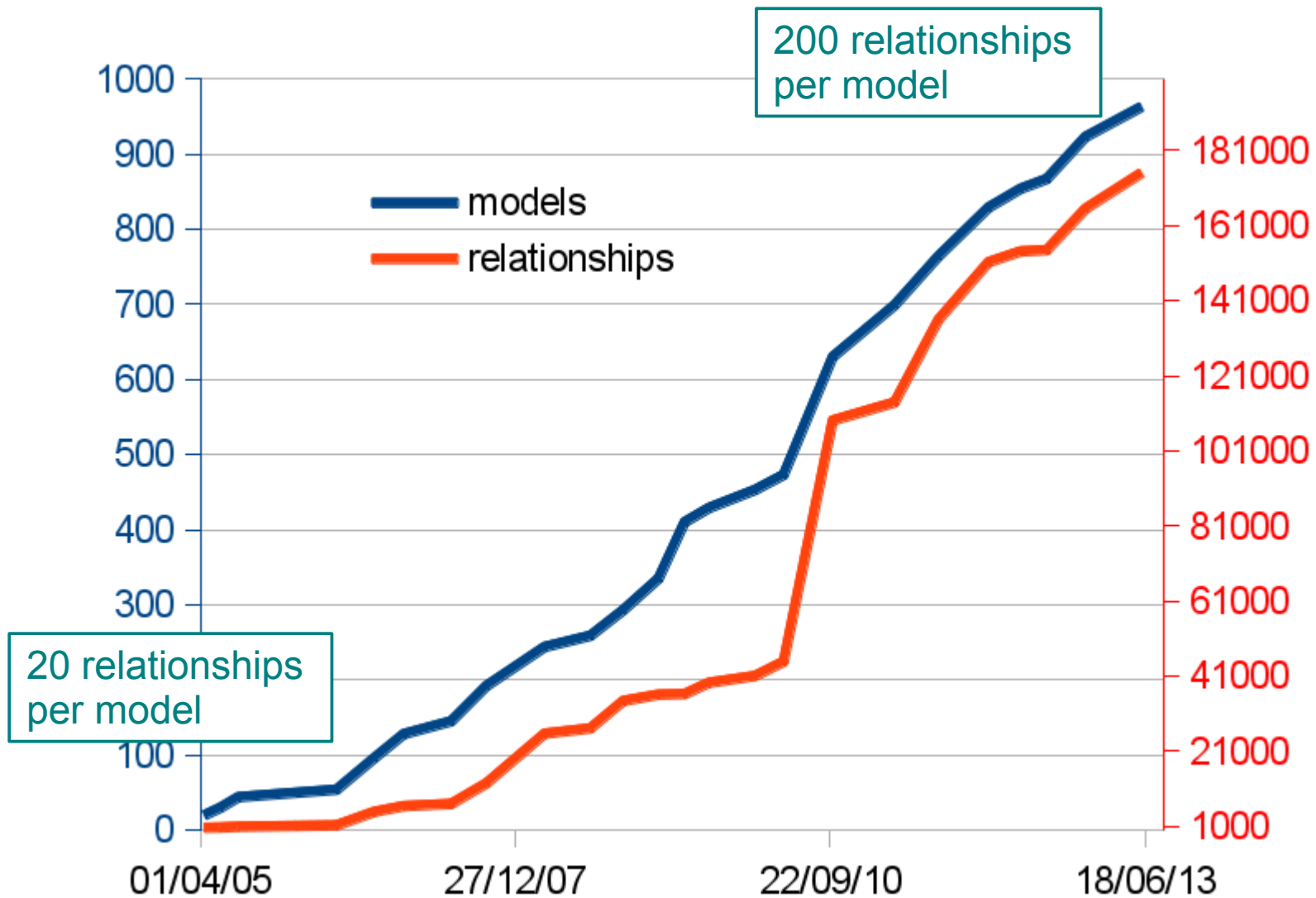
Parameter	Value	Notes
$k_1[aa]/[CT]$	0.015 min^{-1}	*
k_2	0	†
$k_3[CT]$	200 min^{-1}	*
k_4	$10\text{--}1000 \text{ min}^{-1}$ (adjustable)	
k_4'	0.018 min^{-1}	
$k_5[\sim P]$	0	‡
k_6	$0.1\text{--}10 \text{ min}^{-1}$ (adjustable)	
k_7	0.6 min^{-1}	†
$k_8[\sim P]$	$\gg k_9$	§
k_9	$\gg k_6$	§

simulation

computational model

Tyson et al (1991) PNAS 88(1):7328-32

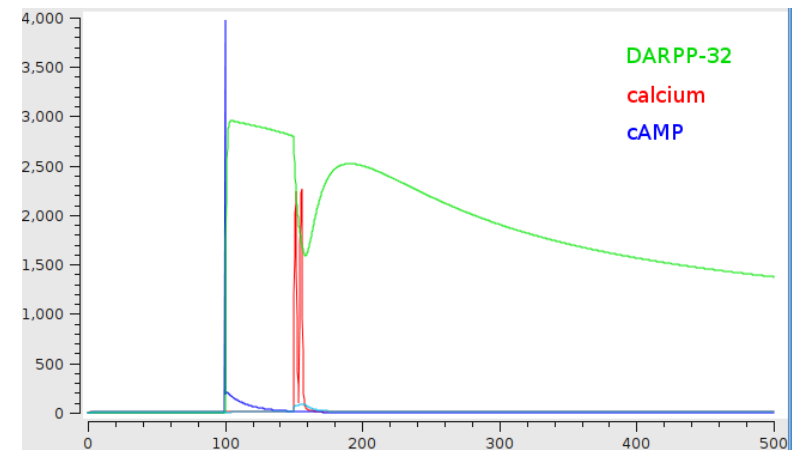
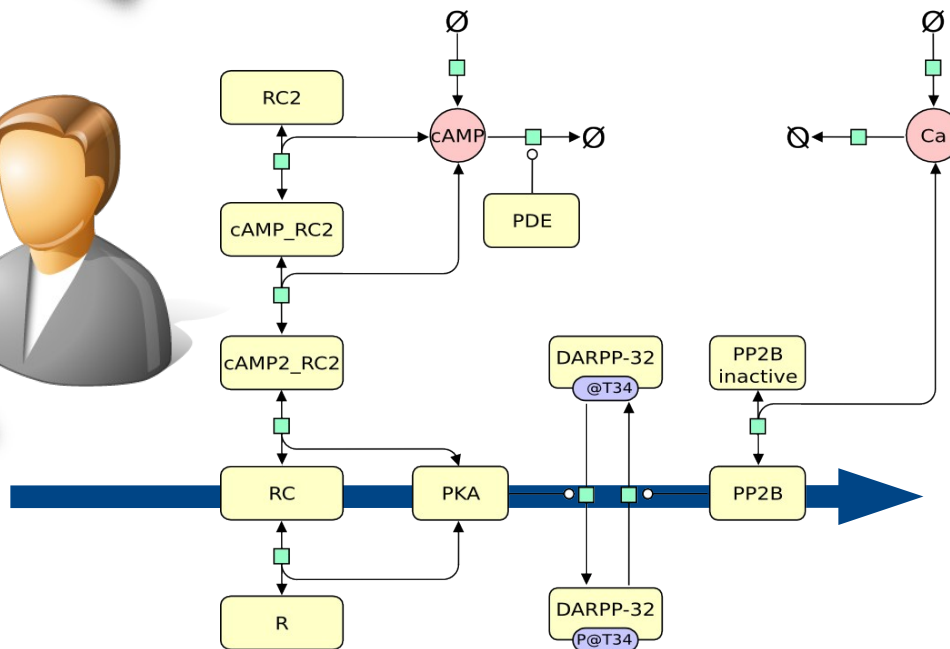
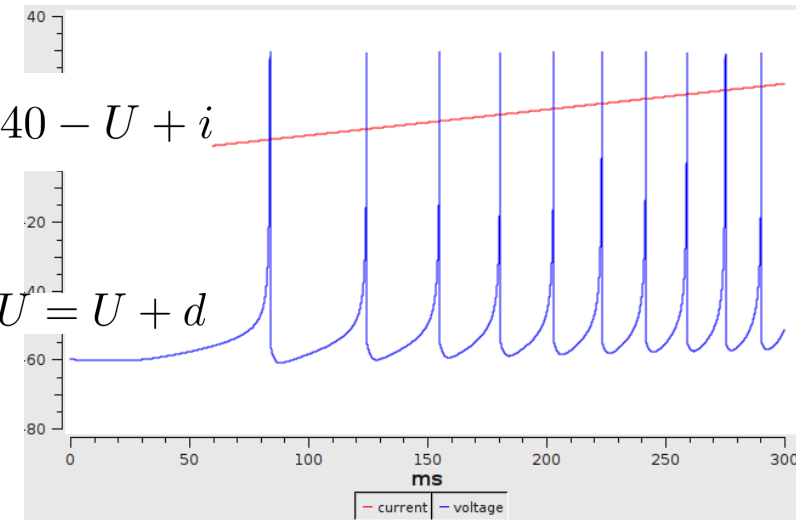
Computational models on the rise

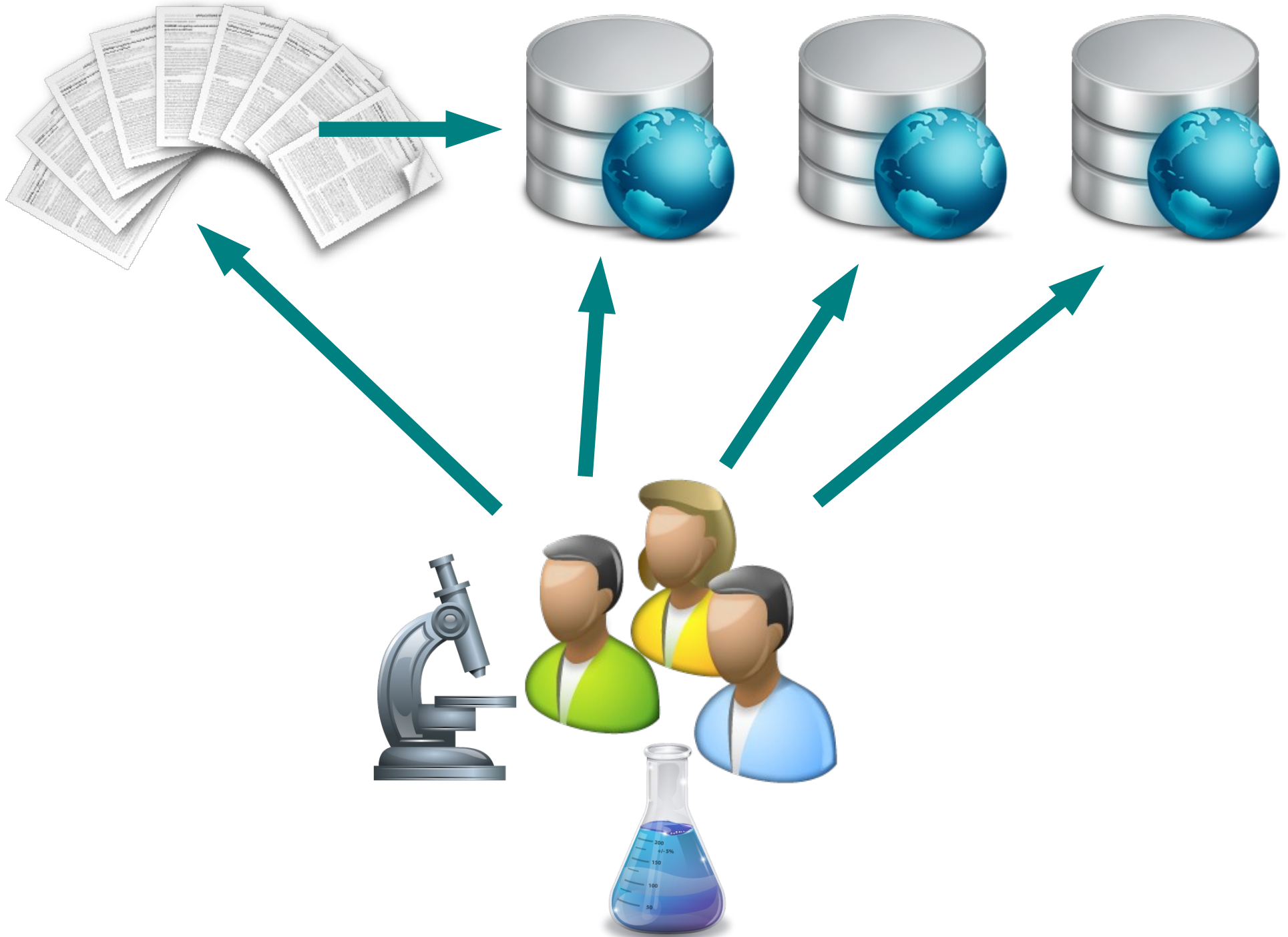


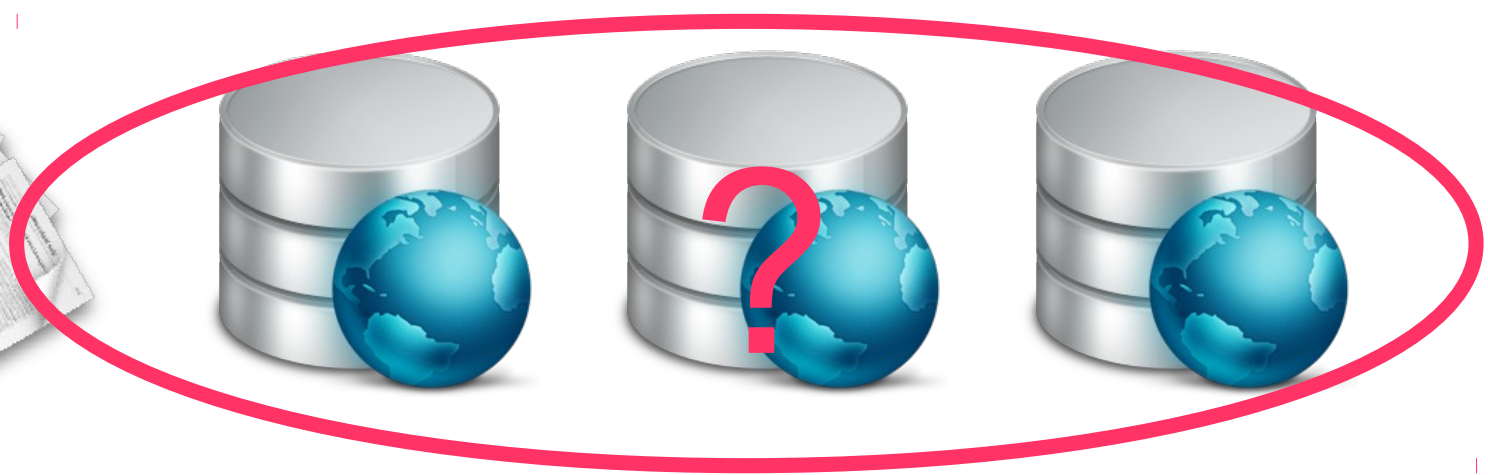
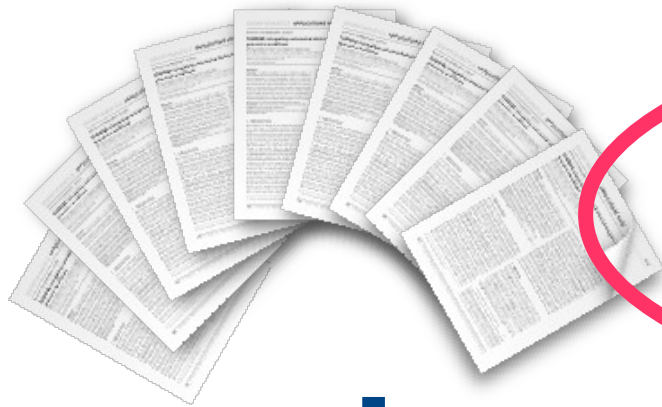
BioModels Database growth (published models branch) since its creation



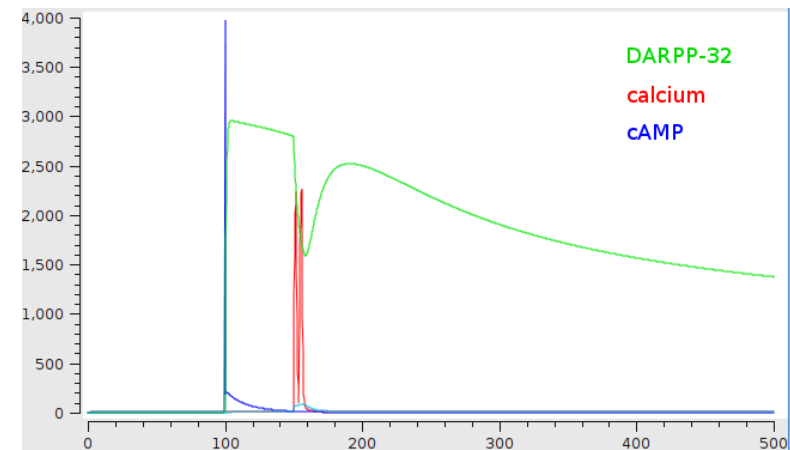
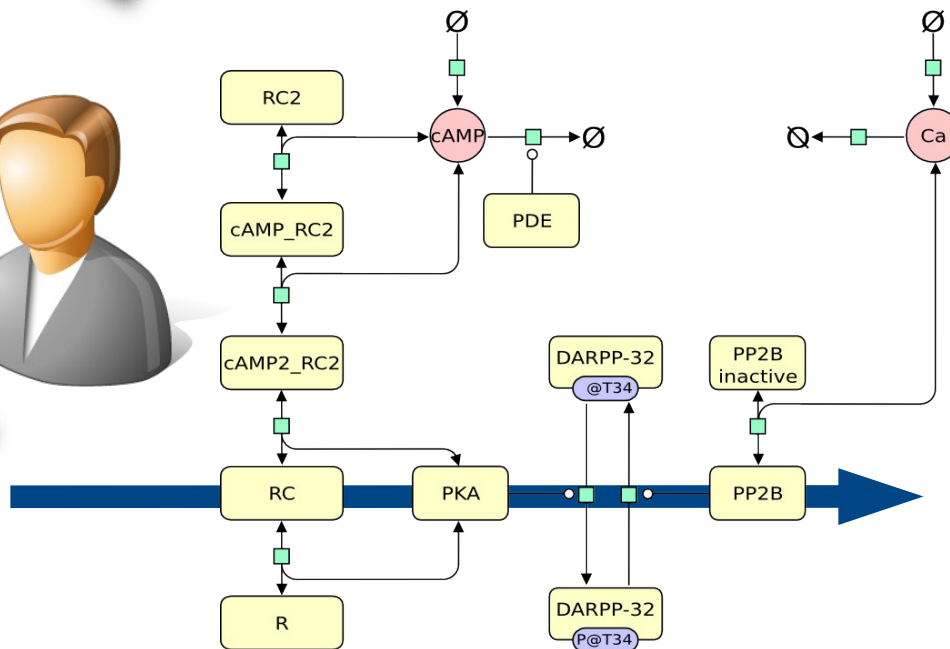
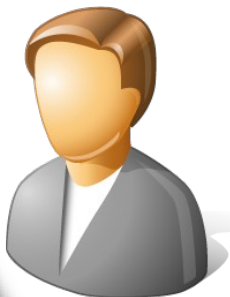
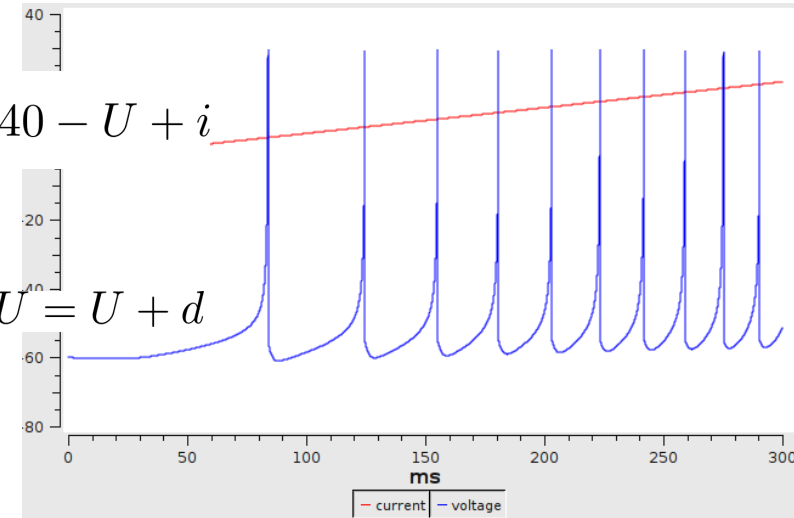
$$\begin{aligned}\frac{dv}{dt} &= 0.04v^2 + 5v + 140 - U + i \\ \frac{dU}{dt} &= a(bv - U) \\ v > V_{\text{thresh}} &\Rightarrow v = c; U = U + d\end{aligned}$$







$$\begin{aligned} \frac{dv}{dt} &= 0.04v^2 + 5v + 140 - U + i \\ \frac{dU}{dt} &= a(bv - U) \\ v > V_{\text{thresh}} &\Rightarrow v = c; U = U + d \end{aligned}$$



Training

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Joint EMBL-EBI-Wellcome Trust Course: In Silico Systems Biology

Venue:

European Bioinformatics Institute, Cambridge, CB10 1SD
United Kingdom

See map: [Google Maps](#)

Date: Tuesday, June 25, 2013 - Saturday, June 29, 2013

Organizers:

[Laura Emery](#) , EMBL-EBI, UK

[Julio Saez-Rodriguez](#) , EMBL-EBI

[Nicolas Le Novère](#) , EMBL-EBI

Admin support:

[Wellcome Trust Advanced Courses](#) , Wellcome Trust Advanced Courses, UK

Registration Opens Date: Thursday, August 23, 2012

Registration Deadline: Friday, March 8, 2013

Participation: Open application with selection

I want my pathways
from



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Starting on July 1, 2011 the KEGG FTP site for academic users will be transferred from GenomeNet at Kyoto University to NPO Bioinformatics Japan, and it will be available only to paid subscribers. The publicly funded portion, the [medicus](#) directory, will continue to be freely accessible at GenomeNet. The KEGG FTP site for commercial customers managed by Pathway Solutions will remain unchanged. The new FTP site is available for free trial until the end of June.

Please register to learn more about the KEGG FTP subscription.

Thank you!

Minoru Kanehisa



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[Nicolas Le Novère](#), EMBL-EBI

Admin support:

[Wellcome Trust Advanced Courses](#)

Registration Opens Date: Thursday, June 27, 2013

Registration Deadline: Friday, June 28, 2013

Participation: Open application with limited places

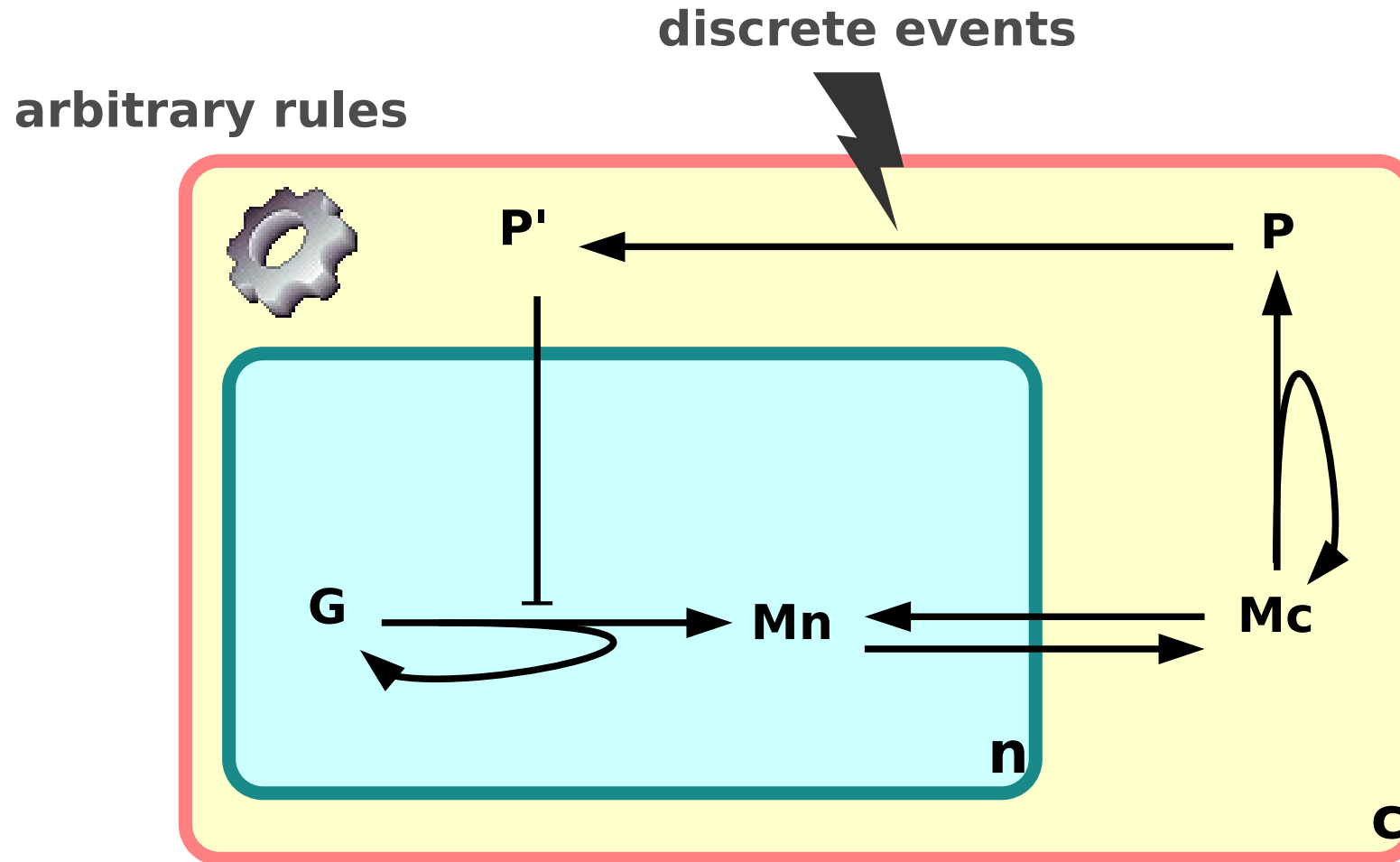
I want my pathways
from



I want my pathways
in



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Hucka *et al.* The Systems Biology Markup Language (SBML): A Medium for Representation and Exchange of Biochemical Network Models. *Bioinformatics* (2003), 19: 524-531.

```
<?xml version="1.0" encoding="UTF-8"?>
<sbml level="3" version="1".
  xmlns="http://www.sbml.org/sbml/level3/version1/core">
  <model>
    <listOfFunctionDefinitions> <!-- --> </listOfFunctionDefinitions>
    <listOfUnitDefinitions> <!-- --> </listOfUnitDefinitions>
    <listOfCompartments> <!-- --> </listOfCompartments>
    <listOfSpecies> <!-- --> </listOfSpecies>
    <listOfParameters> <!-- --> </listOfParameters>
    <listOfInitialAssignments> <!-- --> </listOfInitialAssignments>
    <listOfRules> <!-- --> </listOfRules>
    <listOfConstraints> <!-- --> </listOfConstraints>
    <listOfReactions> <!-- --> </listOfReactions>
    <listOfEvents> <!-- --> </listOfEvents>
  </model>
</sbml>
```

variables

relationships

Systems Biology Markup Language



```
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version4" level="2" version="4">
  <model name="Simple Model">
    <listOfCompartments>
      <compartment id="cell" size="1" />
    </listOfCompartments>
    <listOfSpecies>
      <species id="A" compartment="cell" initialConcentration="1"/>
      <species id="B" compartment="cell" initialConcentration="1"/>
    </listOfSpecies>
    <listOfParameters>
      <parameter id="k1" value="0.1"/>
    </listOfParameters>
    <listOfReactions>
      <reaction id="r1" reversible="false">
        <listOfReactants>
          <speciesReference species="A"/>
        </listOfReactants>
        <listOfProducts>
          <speciesReference species="B"/>
        </listOfProducts>
        <kineticLaw>
          <math xmlns="http://www.w3.org/1998/Math/MathML">
            <apply>
              <times/>
              <ci> cell </ci>
              <ci> k1 </ci>
              <ci> A </ci>
            </apply>
          </math>
        </kineticLaw>
      </reaction>
    </listOfReactions>
  </model>
</sbml>
```

$A \rightarrow B$

$v_1 = k_1 \times [A] \times V_{cell}$

A very simple
SBML file



SimpleSBML - COPASI 4.6 (Build 32) /home/.../2011-03-ModelsIndustry/SimpleSBML.cps

File Tools Help

Concentrations

- Copasi
 - Model
 - Biochemical
 - Compartments
 - cell
 - Species
 - A
 - B
 - Reactions
 - r1
 - Global Quantities
 - Events
 - Parameter Overview
 - Mathematical
 - Differential Equations
 - Matrices
 - Diagrams
 - Tasks
 - Steady-State
 - Stoichiometric Analysis
 - Time Course
 - Metabolic Control Analysis
 - Lyapunov Exponents
 - Time Scale Separation Analysis
 - Parameter Scan
 - Optimization
 - Parameter Estimation
 - Sensitivities



$$\frac{d([A] \cdot V_{\text{cell}})}{dt} = -V_{\text{cell}} \cdot (k_1 \cdot [A])$$

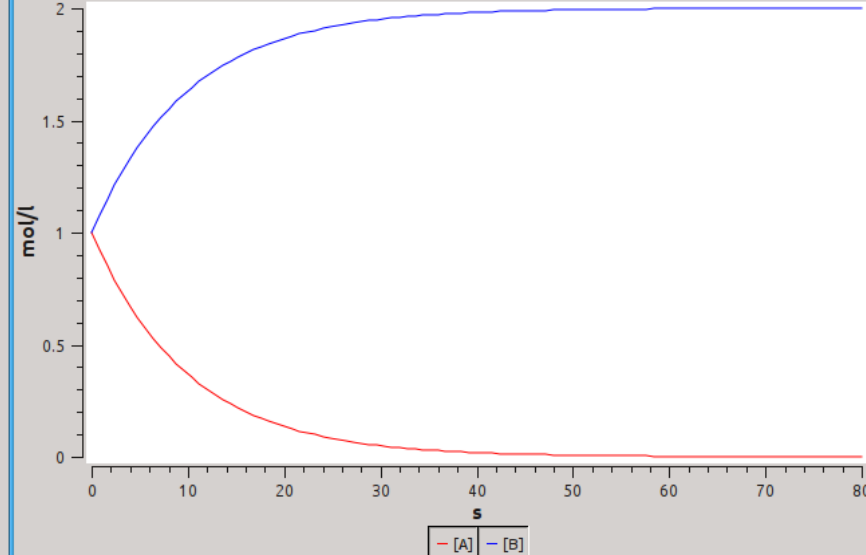
$$\frac{d([B] \cdot V_{\text{cell}})}{dt} = +V_{\text{cell}} \cdot (k_1 \cdot [A])$$

local parameters display numerical value Save Formula to Disk

Copasi Plot: Concentrations, Volumes, and Global Quantity Values

Print Save Image Save Data Zoom out Show All Hide All Close

Concentrations, Volumes, and Global Quantity Values



CellDesigner

File Edit Component View Database Layout Simulation Plugin Window SBW Preference Help

SimpleSBML.xml

Model

Compartments

Species

Reactions

Layer base

SimpleSBML.xml *

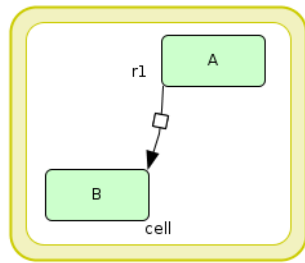
Species Proteins Genes RNAs asRNAs Reactions Compartments Par

Edit Export

class id name speciesType compar... positio... included

PROTEIN A A cell inside included

PROTEIN B B cell inside included



ControlPanel SimpleSBML.xml

File Edit Data Simulation

Time span

End Time 80

Num. o... 100

Error tolerance

Exp. -6

Solver

SOSlib

COPASI

Species Parameters Change amount Parameter Scan

Id Name Compart... Quantity ... Initial

A A cell Concentra...

B B cell Concentra...

Graph Table

Concentration raw Species Fluxes Parameters Compe

2.00

1.5

1.0

0.5

0.00

Time

80.00

Initialize Save As Execute Close show scatter plot

Graph Table

Concentration raw Species Fluxes Parameters Compe

2.00

1.5

1.0

0.5

0.00

Time

80.00

Initialize Save As Execute Close show scatter plot

V... S... C...

Species

Fluxes

Parameters

Compe

Unselect all

species search

search

A community-driven global reconstruction of human metabolism

Ines Thiele^{1,2,37}, Neil Swainston^{3,4,37}, Ronan M T Fleming^{1,5}, Andreas Hoppe⁶, Swagatika Sahoo¹, Maike K Aurich¹, Hulda Haraldsdottir¹, Monica L Mo⁷, Ottar Rolfsson¹, Miranda D Stobbe^{8,9}, Stefan G Thorleifsson¹, Rasmus Agren¹⁰, Christian Bölling⁶, Sergio Bordel¹⁰, Arvind K Chavali¹¹, Paul Dobson¹², Warwick B Dunn^{3,13}, Lukas Endler¹⁴, David Hala¹⁵, Michael Hucka¹⁶, Duncan Hull⁴, Daniel Jameson^{3,4}, Neema Jamshidi⁷, Jon J Jonsson⁵, Nick Judy¹⁷, Sarah Keating¹⁷, Intawat Nookaew¹⁰, Nicolas Le Novère^{17,18}, Naglis Malys^{3,19,20}, Alexander Mazein²¹, Jason A Papin¹¹, Nathan D Price²², Evgeni Selkov, Sr²³, Martin I Sigurdsson¹, Evangelos Simeonidis^{22,24}, Nikolaus Sonnenschein²⁵, Kieran Smallbone^{3,26}, Anatoly Sorokin^{21,27}, Johannes H G M van Beek^{28–30}, Dieter Weichart^{3,31}, Igor Goryanin^{21,32}, Jens Nielsen¹⁰, Hans V Westerhoff^{3,28,33,34}, Douglas B Kell^{3,35}, Pedro Mendes^{3,4,36} & Bernhard Ø Palsson^{1,7}

Multiple models of human metabolism have been reconstructed, but each represents only a subset of our knowledge. Here we describe Recon 2, a community-driven, consensus 'metabolic reconstruction', which is the most comprehensive representation of human metabolism that is applicable to computational modeling. Compared with its predecessors, the reconstruction has improved topological and functional features, including ~2× more reactions and ~1.7× more unique metabolites. Using Recon 2 we predicted changes in metabolite biomarkers for 49 inborn errors of metabolism with 77% accuracy when compared to experimental data. Mapping metabolomic data and drug information onto Recon 2 demonstrates its potential for integrating and analyzing diverse data types. Using protein expression data, we automatically generated a compendium of 65 cell type-specific models, providing a basis for manual curation or investigation of cell-specific metabolic properties. Recon 2 will facilitate many future biomedical studies and is freely available at <http://humanmetabolism.org/>.

An understanding of metabolism is fundamental to comprehending the phenotypic behavior of all living organisms, including humans, where metabolism is integral to health and is involved in much of human disease. High quality, genome-scale 'metabolic reconstructions' are at the heart of bottom-up systems biology analyses and represent the entire network of metabolic reactions that a given organism is known to exhibit¹. The metabolic-network reconstruction procedure

is now well-established² and has been applied to a growing number of model organisms³. Metabolic reconstructions allow for the conversion of biological knowledge into a mathematical format and the subsequent computation of physiological states^{1,4,5} to address a variety of scientific and applied questions^{3,6}. Reconstructions enable network-wide mechanistic investigations of the genotype-phenotype relationship. A high-quality reconstruction of the metabolic network is thus

A not so simple SBML file (Recon2)

- 8 compartments
- 5 063 metabolites
- 2 194 proteins
- 7 440 reactions

¹Center for Systems Biology, University of Iceland, Reykjavik, Iceland. ²Faculty of Industrial Engineering, Mechanical Engineering and Computer Science, University of Iceland, Reykjavik, Iceland. ³Manchester Centre for Integrative Systems Biology, University of Manchester, Manchester Institute of Biotechnology, Manchester, UK. ⁴School of Computer Science, University of Manchester, Manchester, UK. ⁵Department of Biochemistry and Molecular Biology, University of Iceland, Reykjavik, Iceland. ⁶Computational Systems Biochemistry Group, Charité–Universitätsmedizin Berlin, Berlin, Germany. ⁷Department of Bioengineering, University of California, San Diego, La Jolla, California, USA. ⁸Department of Clinical Epidemiology, Biostatistics and Bioinformatics, Academic Medical Center, University of Amsterdam, Amsterdam, the Netherlands. ⁹Netherlands Bioinformatics Centre, Nijmegen, the Netherlands. ¹⁰Department of Chemical and Biological Engineering, Chalmers University of Technology, Gothenburg, Sweden. ¹¹Department of Biomedical Engineering, University of Virginia, Charlottesville, Virginia, USA. ¹²Department of Chemical and Biological Engineering, University of Sheffield, Sheffield, UK. ¹³Centre for Advanced Discovery and Experimental Therapeutics (CADET), Central Manchester University Hospitals NHS Foundation Trust, Manchester Academic Health Sciences Centre, Manchester, UK. ¹⁴Institute for Theoretical Chemistry, University of Vienna, Vienna, Austria. ¹⁵Department of Biology, University of North Texas, Denton, Texas, USA. ¹⁶Computing and Mathematical Sciences Department, California Institute of Technology, Pasadena, California, USA. ¹⁷European Molecular Biology Laboratory, European Bioinformatics Institute, Hinxton, UK. ¹⁸Babraham Research Campus, Cambridge, UK. ¹⁹Faculty of Life Sciences, University of Manchester, Manchester, UK. ²⁰School of Life Sciences, Gibbet Hill Campus, University of Warwick, Coventry, UK. ²¹School of Informatics, University of Edinburgh, Edinburgh, UK. ²²Institute for Systems Biology, Seattle, Washington, USA. ²³Genome Designs, Inc., Walnut Creek, California, USA. ²⁴Luxembourg Centre for Systems Biomedicine, University of Luxembourg, Campus Belval, Esch-sur-Alzette, Luxembourg. ²⁵School of Engineering and Science, Jacobs University Bremen, Bremen, Germany. ²⁶School of Mathematics, University of Manchester, Manchester, UK. ²⁷Institute of Cell Biophysics, Russian Academy of Sciences, Moscow region, Pushchino, Russia. ²⁸Department of Molecular Cell Physiology, Vrije Universiteit, Amsterdam, the Netherlands. ²⁹Section Medical Genomics, Department of Clinical Genetics, Vrije Universiteit University Medical Centre, Amsterdam, the Netherlands. ³⁰Netherlands Consortium for Systems Biology, Amsterdam, The Netherlands. ³¹School of Dentistry, The University of Manchester, Manchester, UK. ³²Okinawa Institute Science and Technology, Okinawa, Japan. ³³School of Chemical Engineering and Analytical Science, University of Manchester, Manchester, UK. ³⁴Swammerdam Institute for Life Sciences, Faculty of Science, University of Amsterdam, Amsterdam, The Netherlands. ³⁵School of Chemistry, The University of Manchester, Manchester, UK. ³⁶Virginia Bioinformatics Institute, Virginia Tech, Blacksburg, Virginia, USA. ³⁷These authors contributed equally to this work. Correspondence should be addressed to I.T. (ines.thiele@gmail.com).

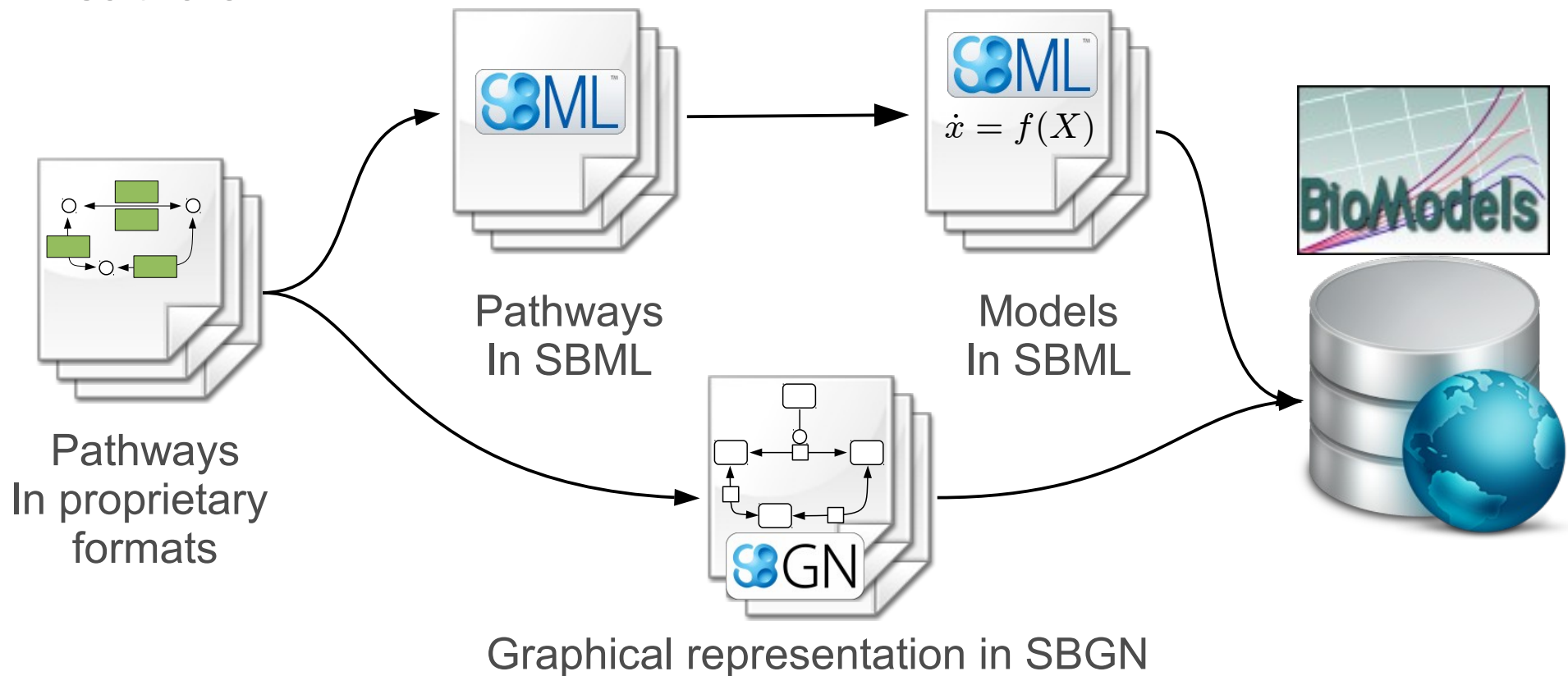
Received 7 September 2012; accepted 19 December 2012; published online 3 March 2013; doi:10.1038/nbt.2488

- Core package – public specification
- Flux balance constraint – public specification
- Model composition – public specification
- Qualitative models – public specification
- Graph Layout – public specification
- Graph rendering – specification finalised
- Complex species – specification finalised
- Groups - specification finalised
- Distributions and ranges - specification under discussion
- Spatial diffusion – specification under discussion
- Enhanced metadata – specification under discussion
- Arrays and sets – specification proposed
- Dynamic structures - discussed

**SBML Level 3
is modular**

Aims of the Path2Models project

- To re-use existing pathway data to generate biochemically based models
- To provide a starting point to model as many biochemical pathways as possible in as many species as possible
- To provide models in a standard format readable by most systems biology software



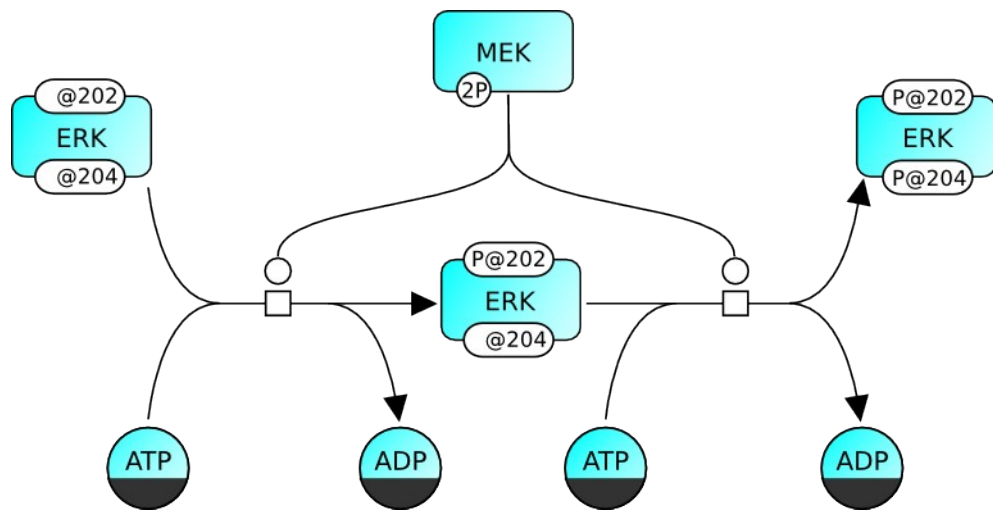
What is GN?

- An **unambiguous** way of graphically **describing and interpreting** biochemical and cellular events: “biological circuit diagrams”
 - Limited amount of symbols
Re-use existing symbols
- ➡ **Smooth learning curve**
- Can represent logical or mechanistic models, biochemical pathways, at different levels of granularity
 - Detailed **technical specification**, precise data-models, **standard API** and growing software support
 - Developed over four years by a **diverse community**, including biologists, modellers, computer scientists etc.

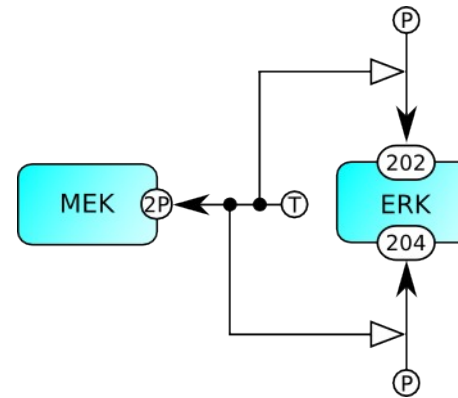
Le Novère et al. The Systems Biology Graphical Notation.
Nat Biotechnol (2009), 27: 735-741

Graph trinity: three languages in one notation

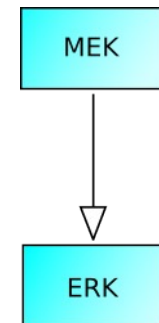
Process Descriptions

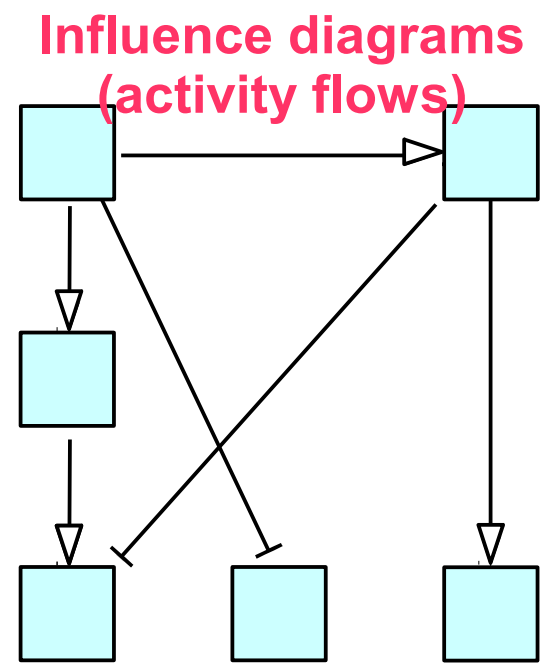
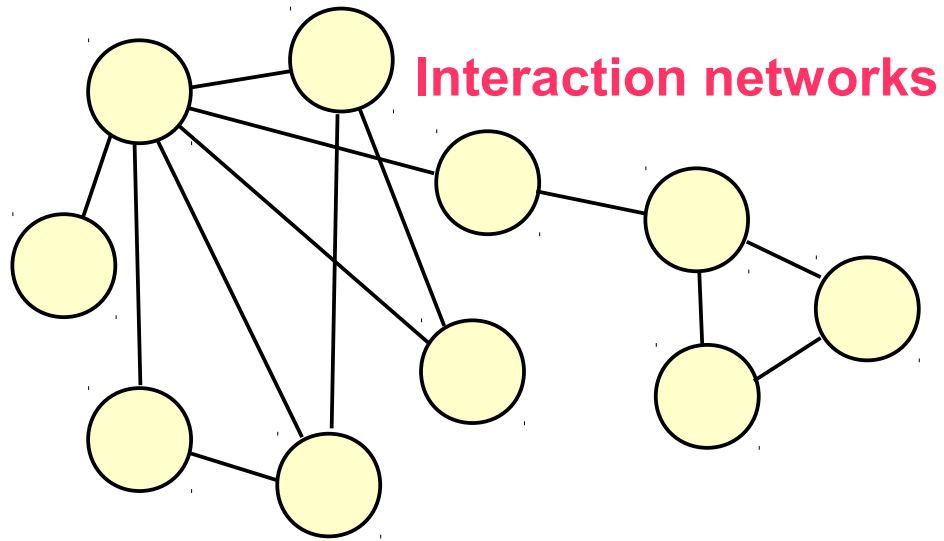


Entity Relationships

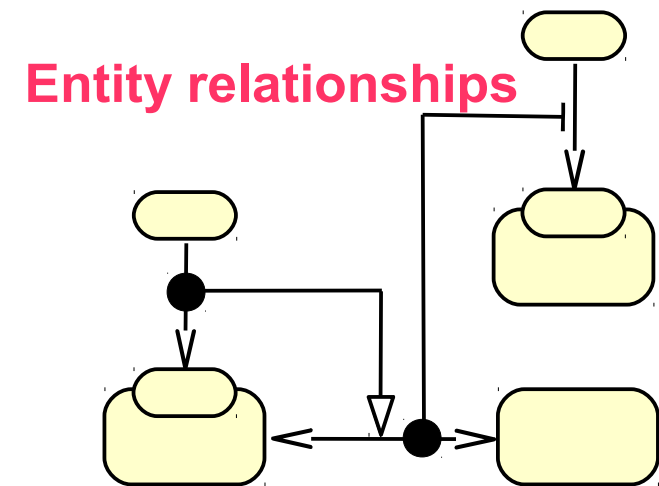
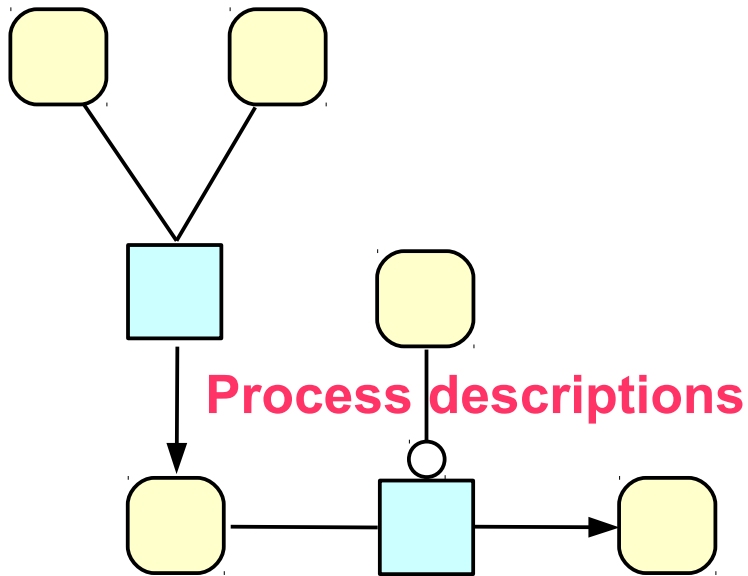


Activity Flows

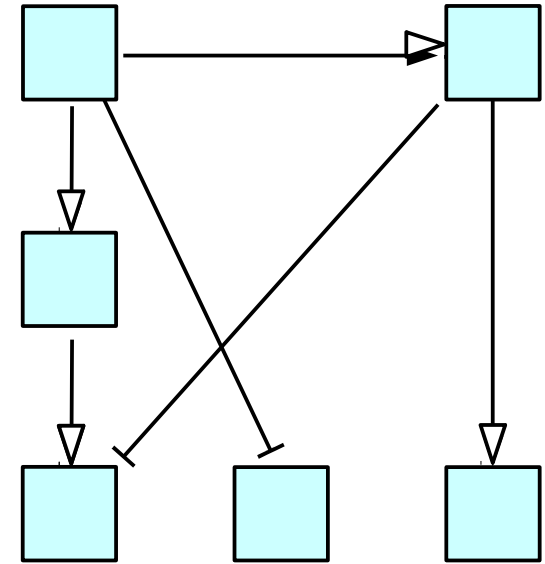




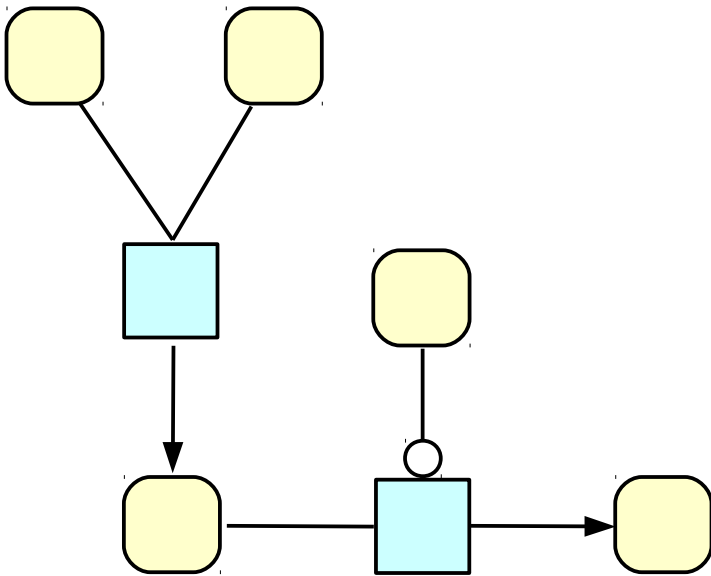
Four types of networks in systems biology



Activity flows

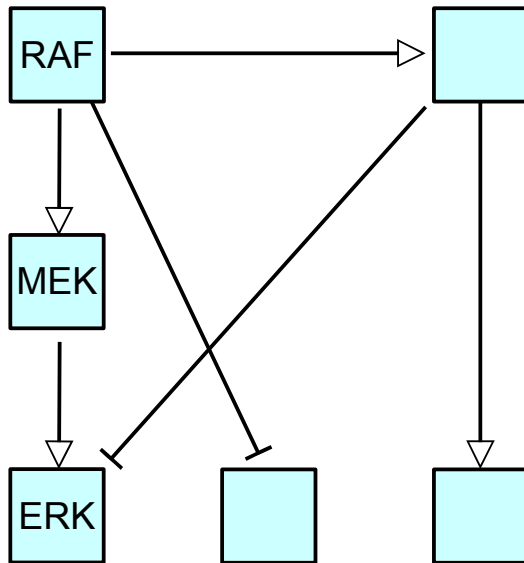


Path2models focus



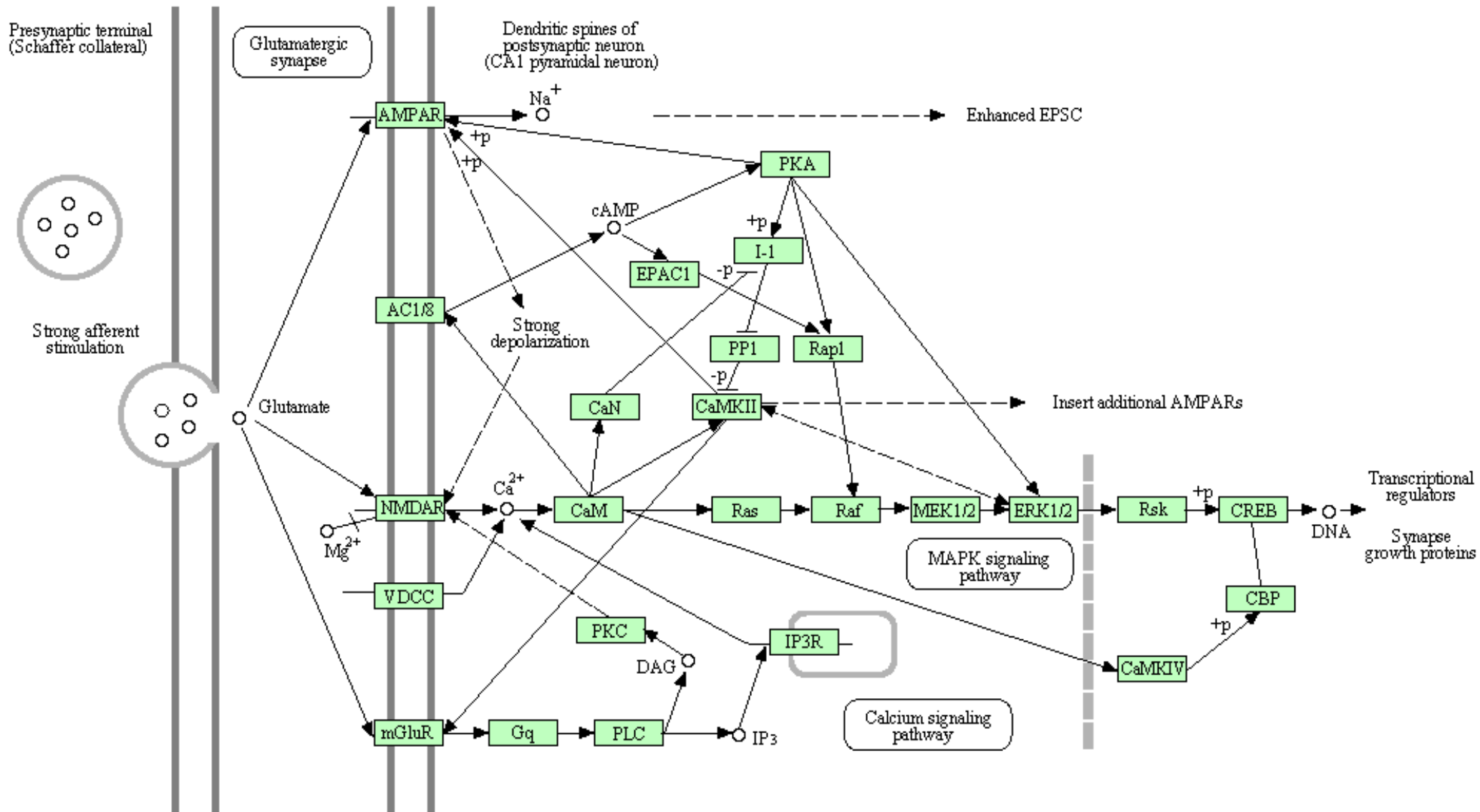
Process descriptions

Influence diagrams (activity-flows)



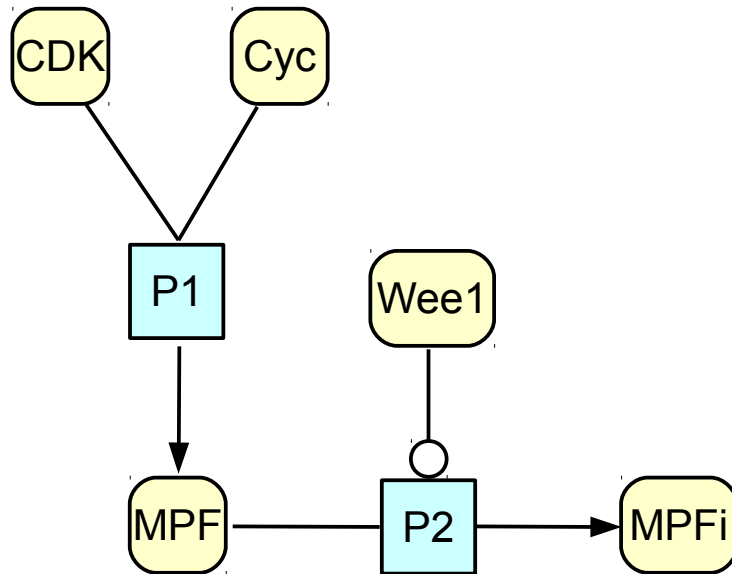
- Signalling pathways, gene regulatory networks
- Nodes represent activities
- Directional
- Sequential
- Non-mechanistic
- Logical modelling

LONG-TERM POTENTIATION

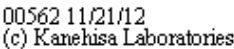


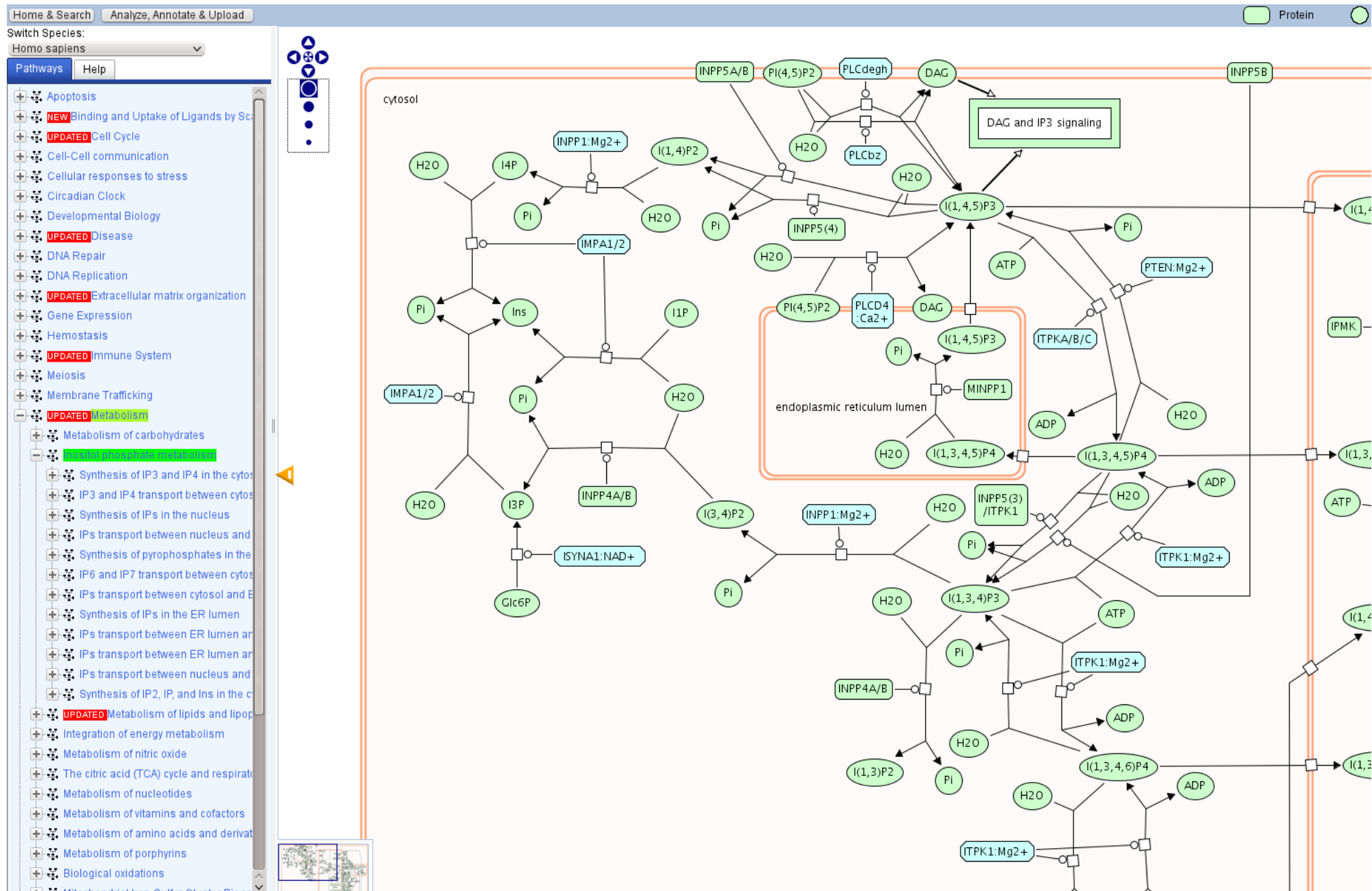


Process Descriptions



- Biochemistry, Metabolic networks
- Nodes represent populations of reactants and reactions
- Directional
- Sequential
- Mechanistic
- Subjected to combinatorial explosion
- Process modelling (ODE, SSA)





Three parallel workflows



Signalling
Pathways



Logical models
of individual signalling pathways

Three parallel workflows



Signalling
Pathways



Logical models
of individual signalling pathways



Metabolic
Networks



Chemical kinetics models
of individual metabolic pathways

Three parallel workflows



Signalling
Pathways



Logical models
of individual signalling pathways



Metabolic
Networks



Chemical kinetics models
of individual metabolic pathways



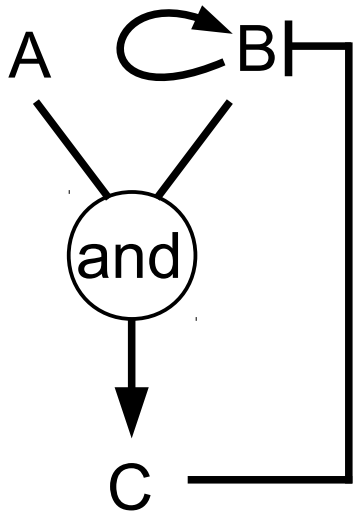
Metabolic
Networks



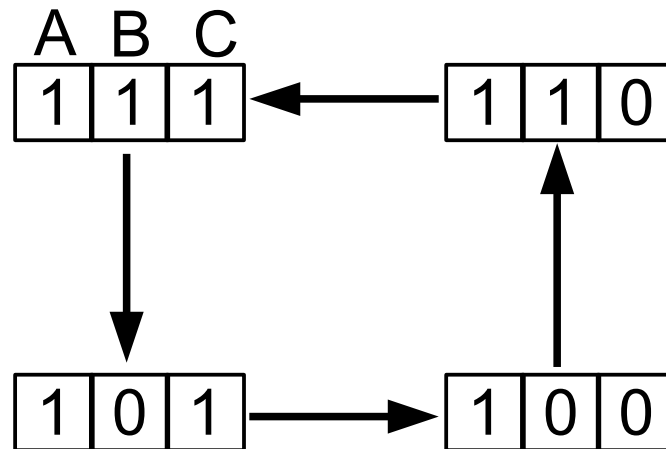
Flux Balance Analysis
of whole genome reconstructions

Signalling pathways: Logical models

- Variables can take a discrete number of values, at least 2
- Transitions of output are expressed as logical combinations of input values
- Simulations can be:
 - synchronous: all the nodes are updated at once
 - asynchronous: nodes are updated one after the other
- One can add delays, inputs etc.



Influence diagram



state diagram



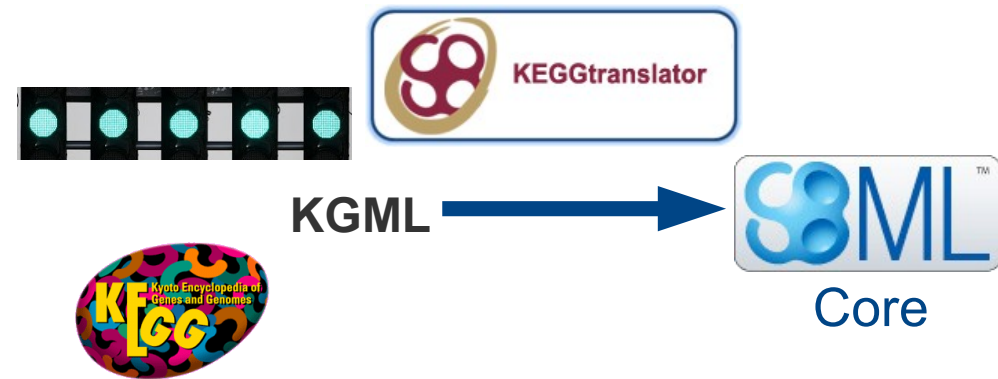
From KEGG metabolic pathways to full kinetic models



KGML



From KEGG metabolic pathways to full kinetic models



From KEGG metabolic pathways to full kinetic models



Systems Biology Ontology vocabularies

- Entities, that is existing objects, whether functional or material, such as “**macromolecule**”, or “**channel**”.
- Roles of reaction participants, including terms like “**substrate**”, “**catalyst**” etc.
- Parameter used in quantitative models. This vocabulary includes terms like “**Michaelis constant**”, “**forward unimolecular rate constant**” etc. A term may contain a precise mathematical expression stored as a MathML lambda function. The variables refer to other parameters.
- Mathematical expressions. Examples of terms are “**mass action kinetics**”, “**Henri-Michaelis-Menten equation**” etc. A term may contain a precise mathematical expression stored as a MathML lambda function. The variables refer to the other vocabularies.
- Modelling framework to precise how to interpret the rate-law. E.g. “**continuous modelling**”, “**discrete modelling**” etc.
- Event type, such as “**catalysis**” or “**addition of a chemical group**”.

Courtot et al. Controlled vocabularies and semantics in Systems Biology.
Mol Syst Biol (2011), 7: 543

Systems Biology Ontology

+ -

SBO:0000000 - sbo term

+ ⓘ [SBO:0000236 - entity](#)

+ ⓘ [SBO:0000231 - interaction](#)

+ ⓘ [SBO:0000064 - mathematical expression](#)

+ ⓘ [SBO:0000355 - conservation law](#)

+ ⓘ [SBO:0000001 - rate law](#)

+ ⓘ [SBO:0000268 - enzymatic rate law](#)

+ ⓘ [SBO:0000150 - enzymatic rate law for irreversible](#)

+ ⓘ [SBO:0000151 - enzymatic rate law for irreversible](#)

+ ⓘ [SBO:0000152 - enzymatic rate law for irreversible](#)

+ ⓘ [SBO:0000028 - enzymatic rate law for irreversible](#)

+ ⓘ [SBO:0000031 - Briggs-Haldane](#)

+ ⓘ [SBO:0000029 - Henri-Michaelis-](#)

+ ⓘ [SBO:0000199 - normalised enzyme](#)

+ ⓘ [SBO:0000030 - Van Slyke-Cullen](#)

+ ⓘ [SBO:0000269 - enzymatic rate law for unireactant](#)

+ ⓘ [SBO:0000192 - Hill-type rate law, generalised form](#)

+ ⓘ [SBO:0000012 - mass action rate law](#)

+ ⓘ [SBO:0000391 - steady state expression](#)

+ ⓘ [SBO:0000004 - modelling framework](#)

+ ⓘ [SBO:0000003 - participant role](#)

+ ⓘ [SBO:0000002 - quantitative parameter](#)

Legend

ⓘ "is a" relationship

Name

Briggs-Haldane rate law

Definition

Rate-law presented in "G.E. Briggs and J.B.S. Haldane (1925) A note on the kinetics of enzyme action, Biochem. J., 19: 338-339". It is a general rate equation that does not require the restriction of equilibrium of Henri-Michaelis-Menten or irreversible reactions of Van Slyke, but instead make the hypothesis that the complex enzyme-substrate is in quasi-steady-state. Although of the same form than the Henri-Michaelis-Menten equation, it is semantically different since Km now represents a pseudo-equilibrium constant, and is equal to the ratio between the rate of consumption of the complex (sum of dissociation of substrate and generation of product) and the association rate of the enzyme and the substrate.

MathML

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Rendered equation

$$\lambda(kcat, Et, S, Km) = \frac{kcat \times Et \times S}{Km + S}$$

Miscellaneous

Date of creation:

23 February 2006, 14:00

Date of last modification:

25 November 2008, 16:27

Parent(s)

[SBO:0000028](#) enzymatic rate law for irreversible non-modulated non-interacting unireactant enzymes (is a)

Children

This term has no child.

History [+]

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```

functional compartment

simple chemical
simple chemical
enzyme

catalysis

substrate

product

catalyst

Briggs-Haldane equation

Km

kcat

Conversion between modeling frameworks

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discrete simulator

$$v1 = \frac{(k_{-1} + V)}{U} \cdot [A] \cdot [C]$$

$$v2 = k_{-1} \cdot [D]$$

$$v3 = V \cdot [D]$$

continuous simulator

$$\nu = \frac{C \cdot V \cdot [A]}{(U + [A])}$$



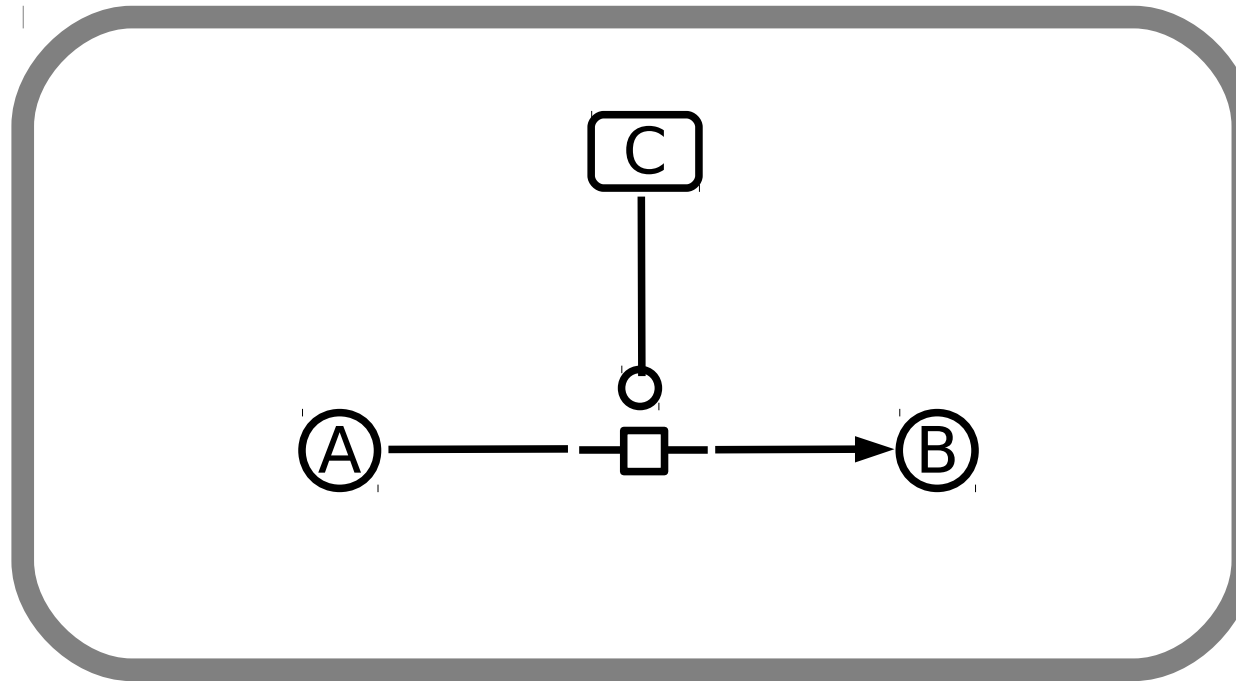
to SBGN conversion using SBO

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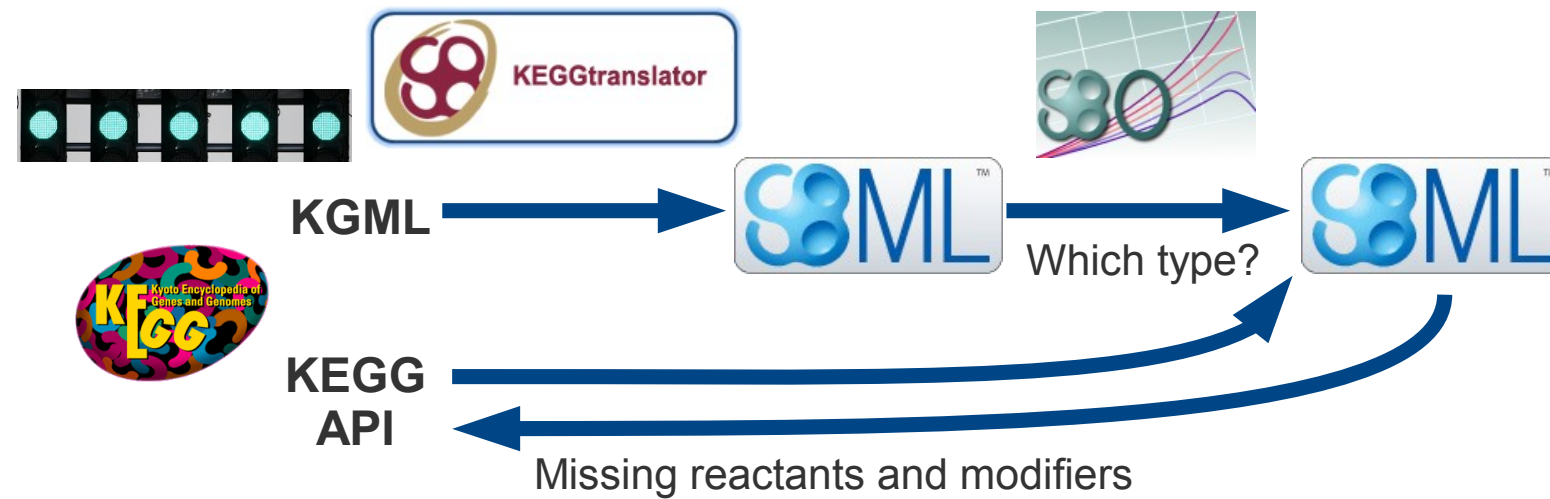
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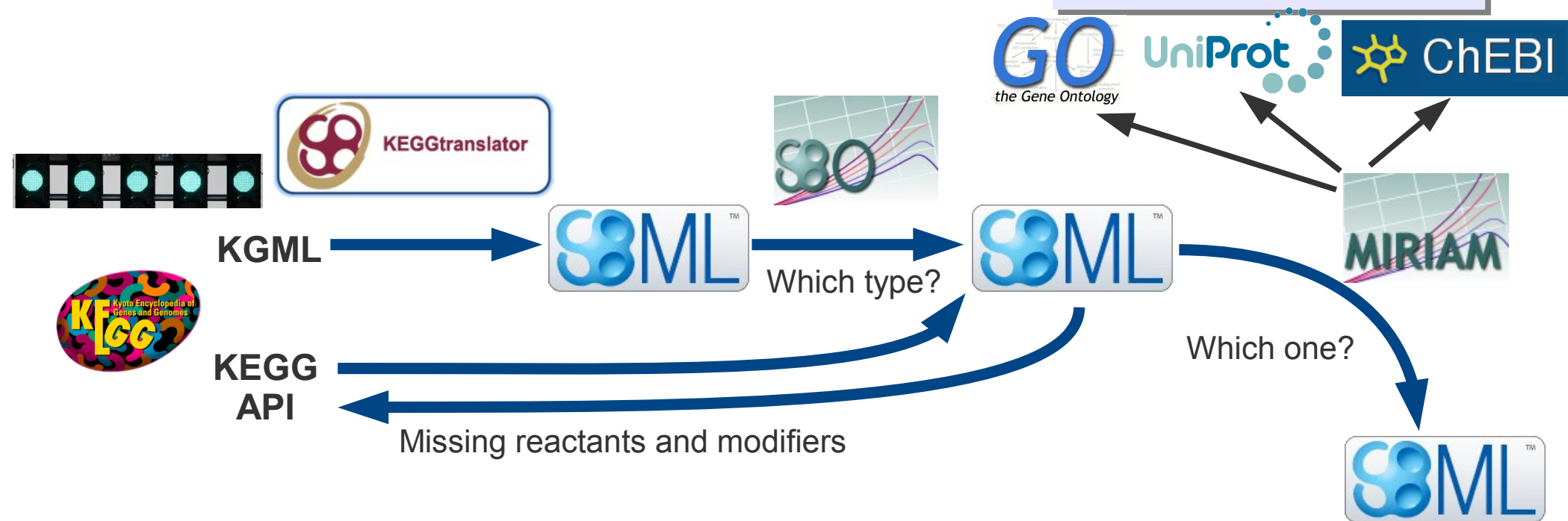
<http://www.sbgn.org/>



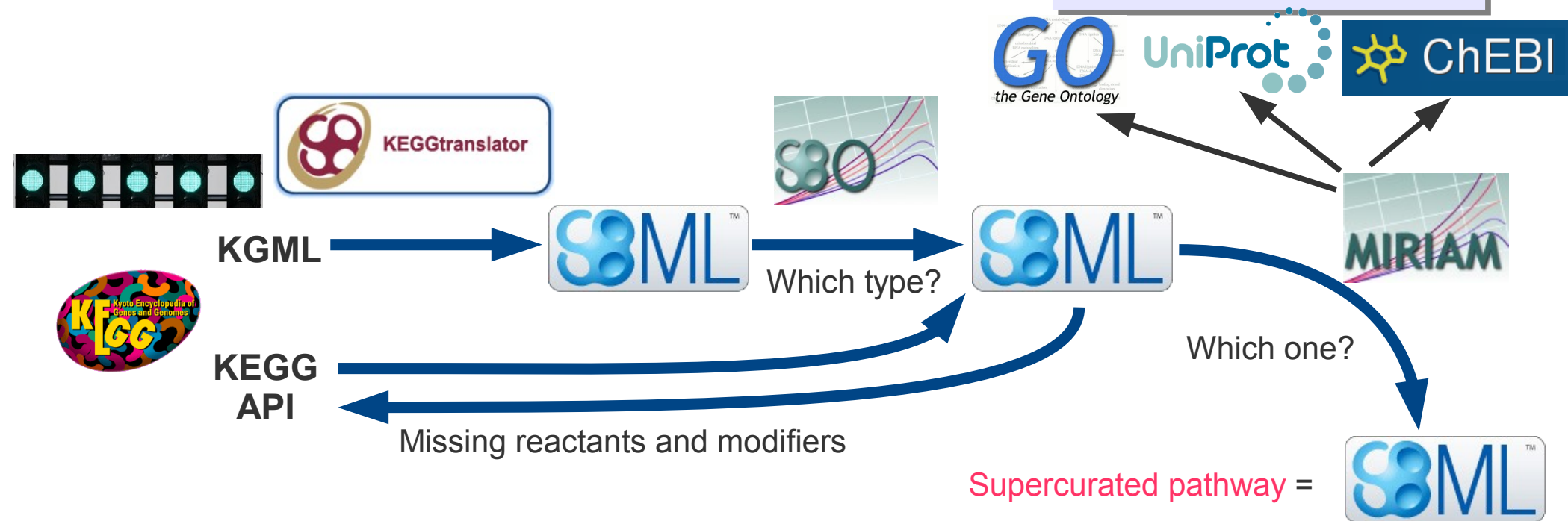
From KEGG metabolic pathways to full kinetic models



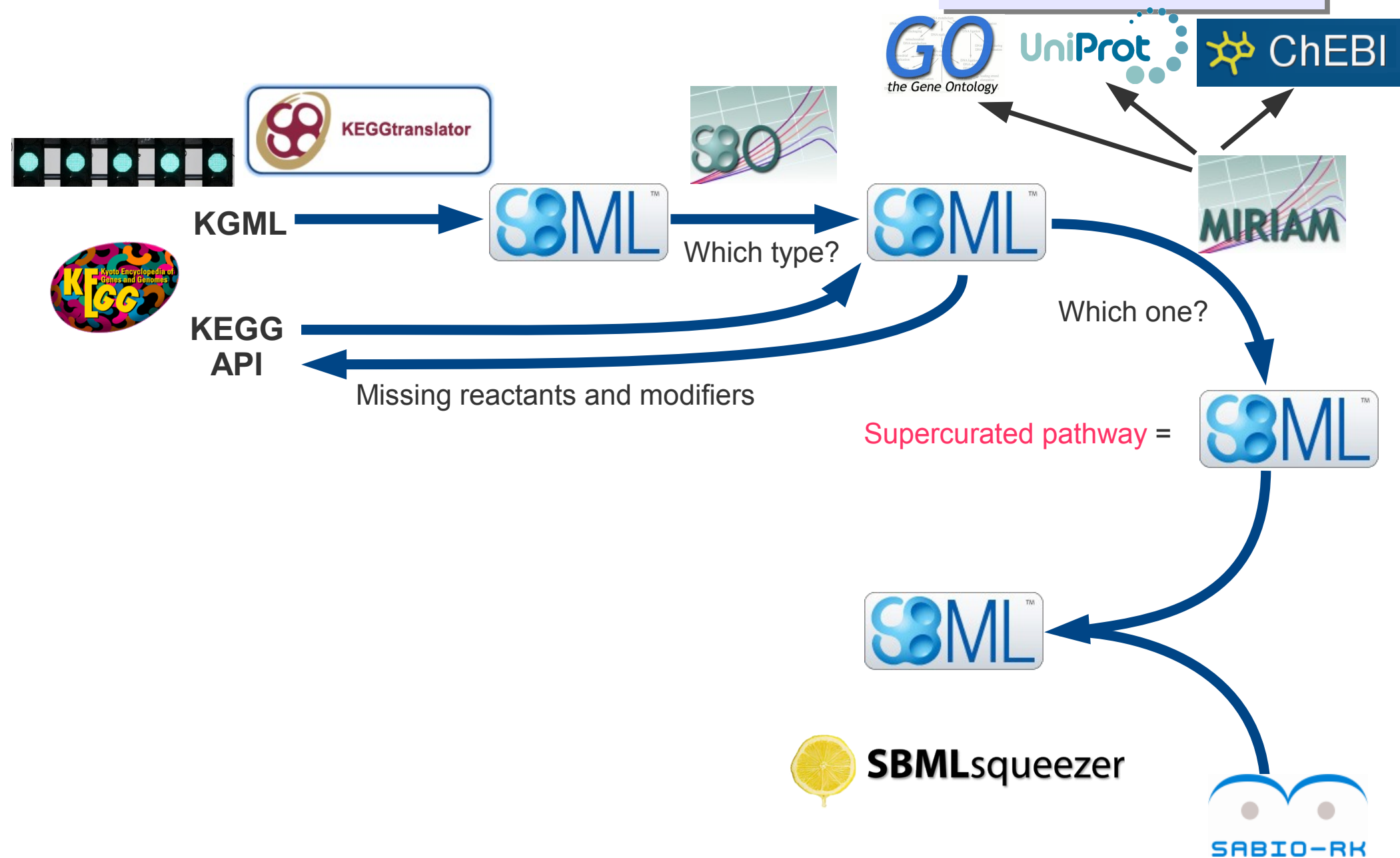
From KEGG metabolic pathways to full kinetic models



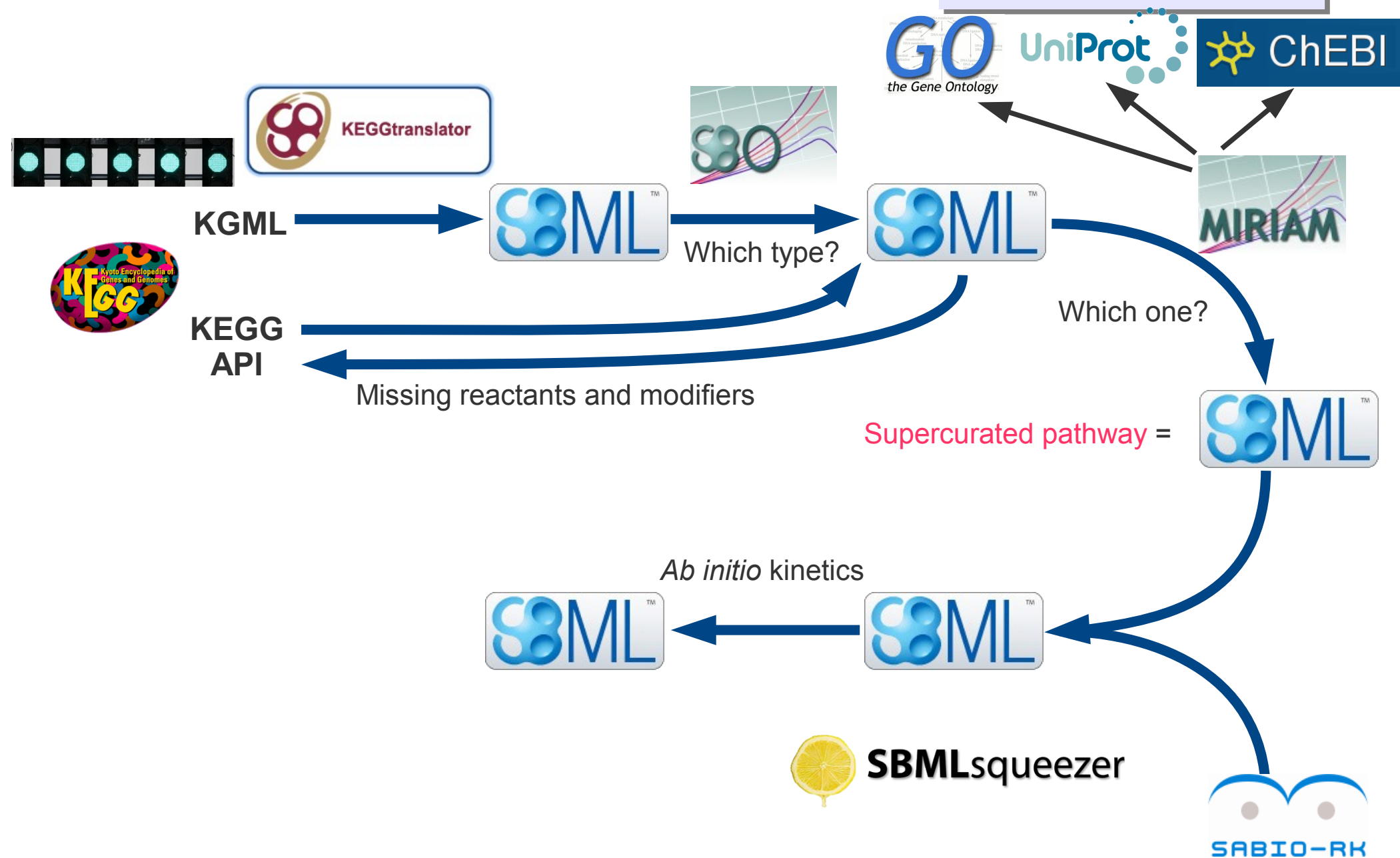
From KEGG metabolic pathways to full kinetic models



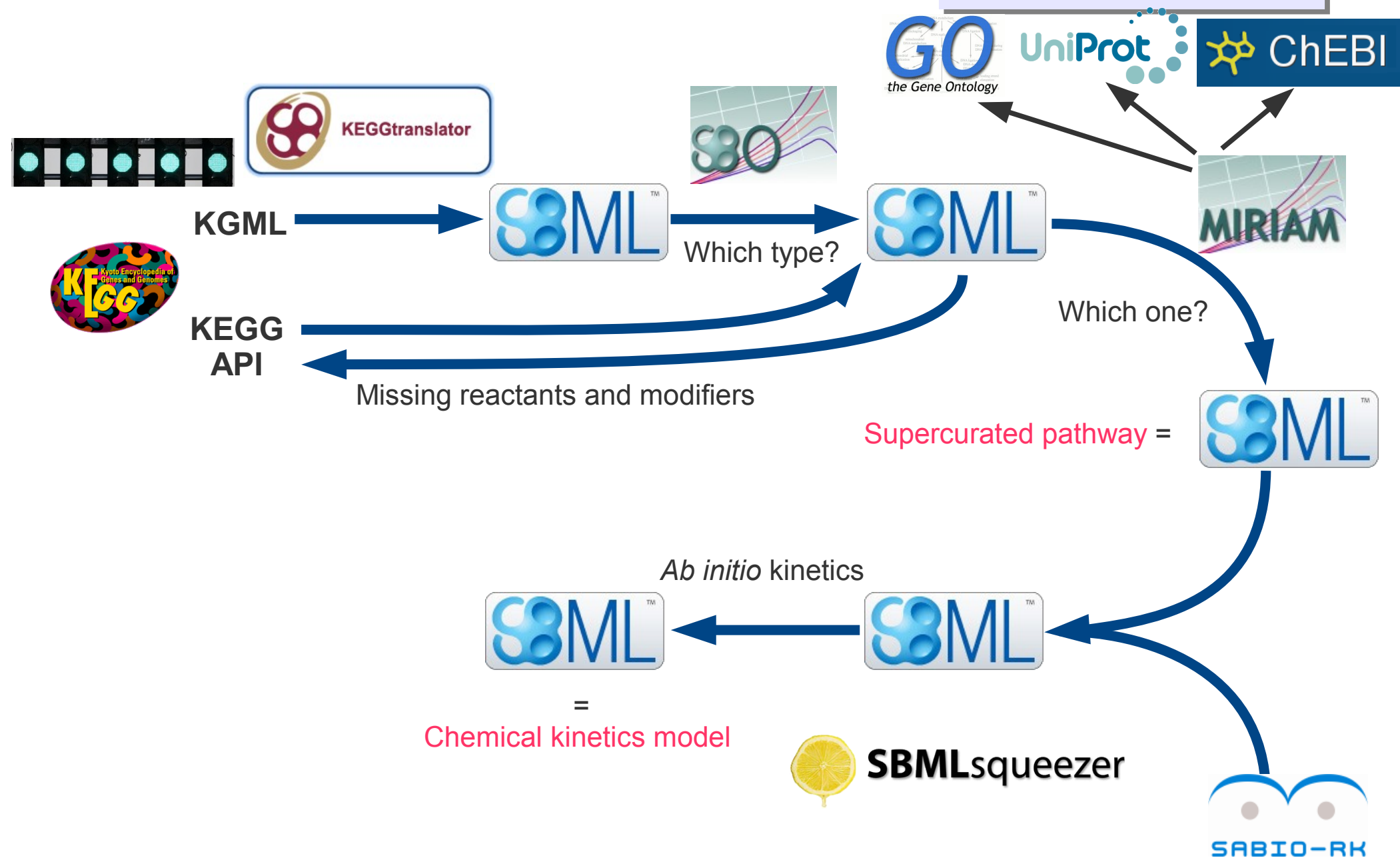
From KEGG metabolic pathways to full kinetic models



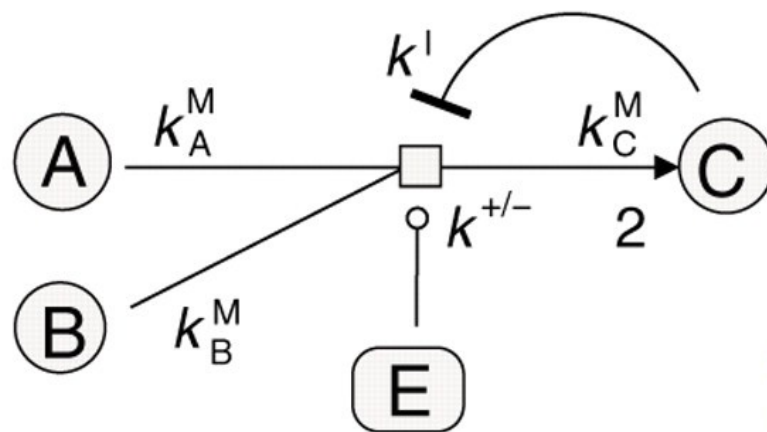
From KEGG metabolic pathways to full kinetic models



From KEGG metabolic pathways to full kinetic models



Metabolic reactions: Common modular rate-law



Reaction rate

Enzyme level

Stoichiometry, 3 parametrizations

$$v = u f \frac{T}{D + D^{\text{reg}}}$$

Complete or partial regulation

5 rate laws

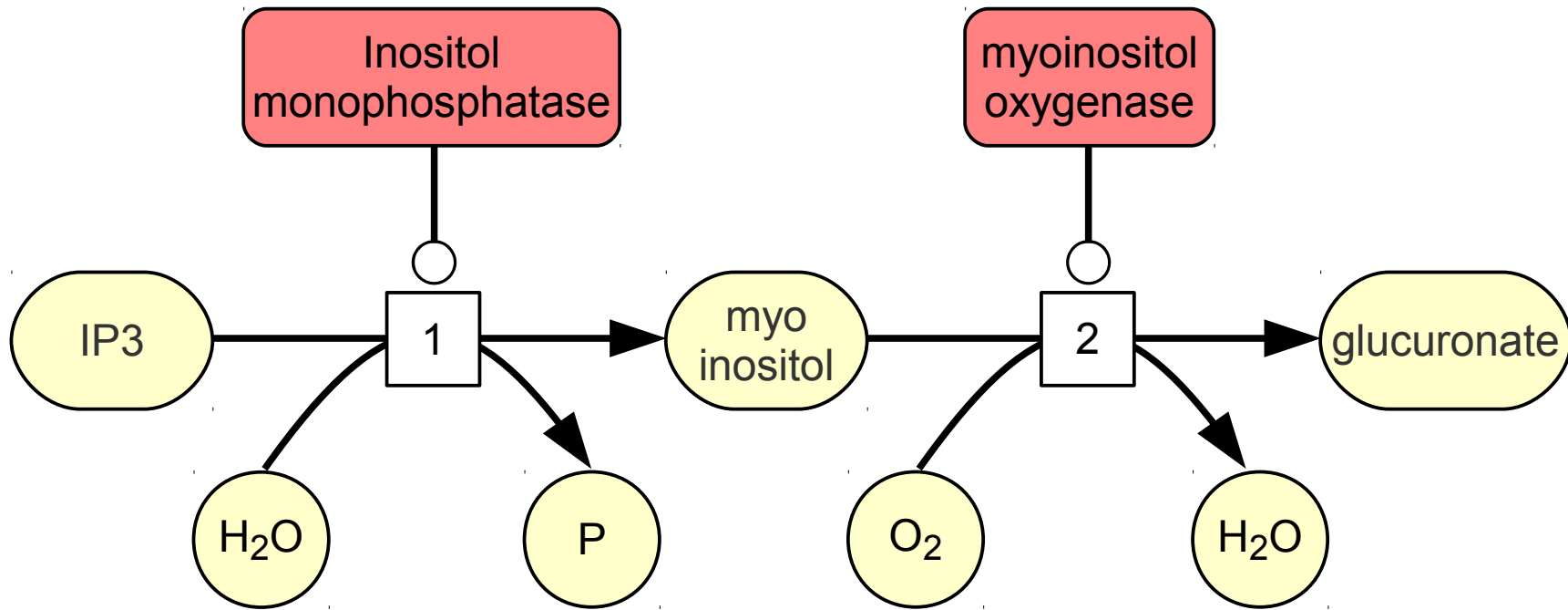
Specific regulation

- Common rate law
- Direct binding rate law
- Simultaneous binding rate law
- Force dependent rate law
- Power Law

$$T = k_r^+ \prod_i \left(\frac{c_i}{k_{ri}^M} \right)^{m_{ri}^+} - k_r^- \prod_i \left(\frac{c_i}{k_{ri}^M} \right)^{m_{ri}^-}$$

Liebermeister, Uhlenhof, Klipp (2010) Modular rate laws for enzymatic reactions: thermodynamics, elasticities and implementation. *Bioinformatics* 26: 1528-1534

Unparametrised Vs. known kinetics



$$v1 = [IMPA] \times k_{cat} \times \frac{[IP3]}{K_m + [IP3]}$$

To estimate

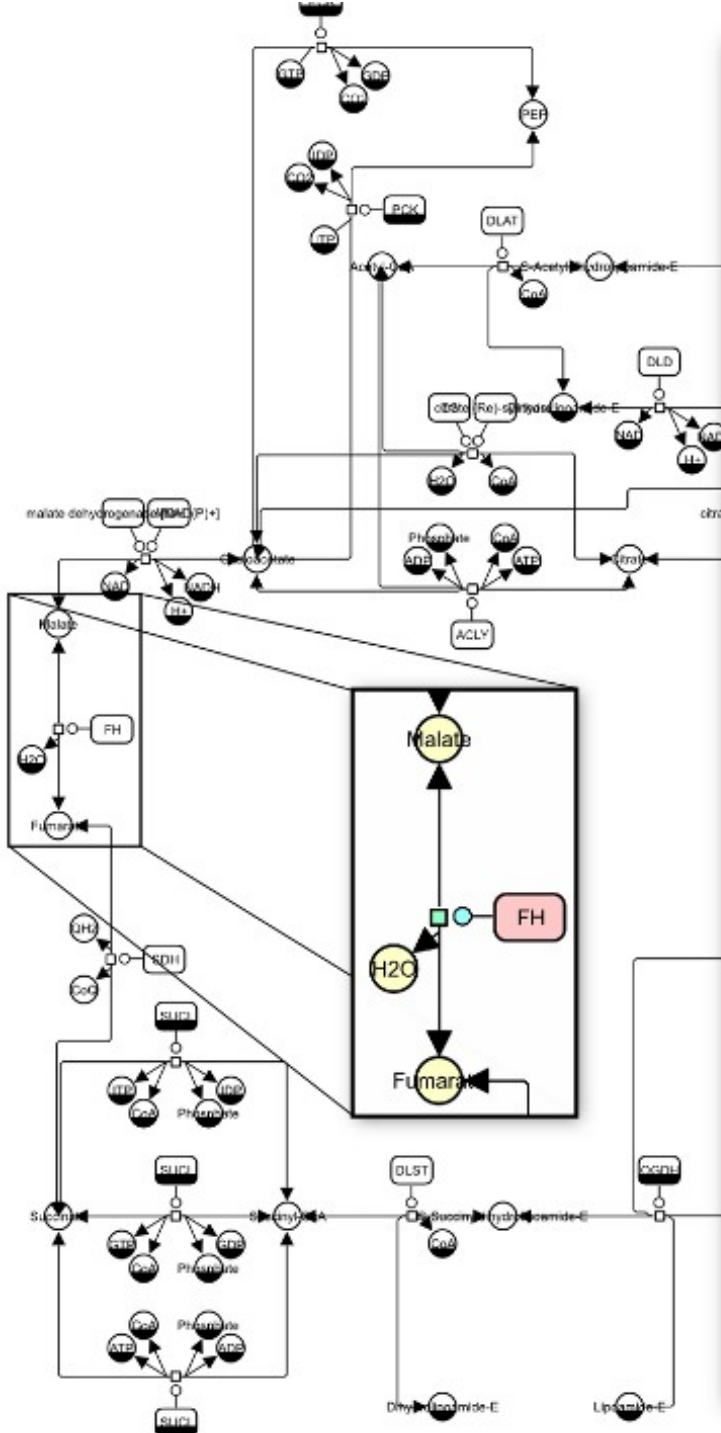
$$v2 = V_{max} \times \frac{[myo inositol]}{K_m + [myo inositol]}$$

$3.5 \cdot 10^{-5} \text{ mol} \cdot \text{s}^{-1} \cdot \text{g}^{-1}$

0.0033 M

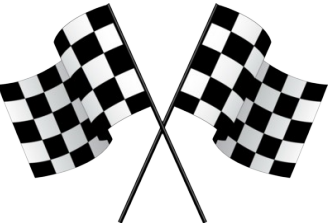


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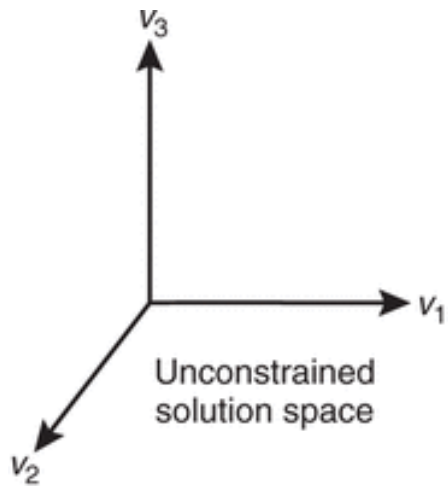


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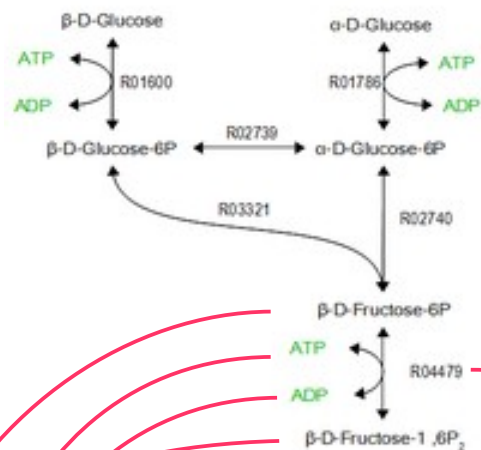
full kinetic models



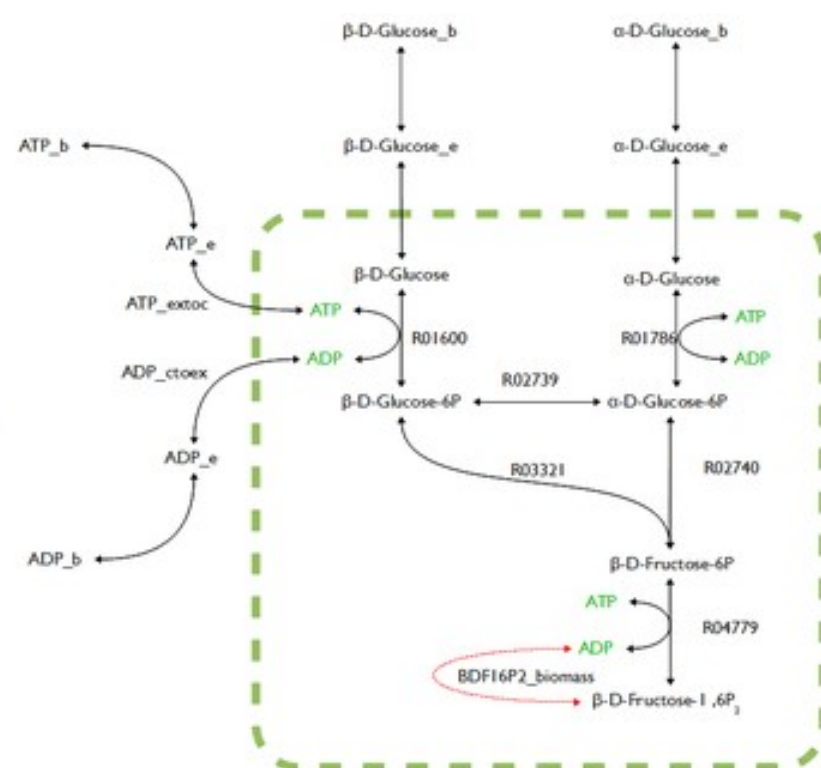
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 \times
 \begin{array}{c} \mathbf{V} \end{array}
 \begin{pmatrix} \text{Flux 1} \\ \text{Flux 2} \\ \text{Flux 3} \\ \text{Flux 4} \\ \dots \\ \text{Flux n} \end{pmatrix}
 =
 \begin{array}{c} \dot{\mathbf{x}} \end{array}
 \begin{pmatrix} d[x1]/dt \\ d[x2]/dt \\ d[x3]/dt \\ \dots \\ d[xm]/dt \end{pmatrix}$$



Whole genome reconstructions: Flux balance analysis models



Prepare for FBA



	R02739	R03321	R02740	R01600	R01786	R04779
C00002	0	0	0	-1	-1	-1
C00008	0	0	0	1	1	1
C00221	0	0	0	-1	0	0
C00267	0	0	0	0	-1	0
C00668	-1	0	-1	0	1	0
C01172	1	-1	0	1	0	0
C05345	0	1	1	0	0	-1
C05378	0	0	0	0	0	1

	R02739_c	R03321_c	R02740_c	R01600_c	R01786_c	R04779_c	ATP_extoc_tr	ADP_extoc_tr	BDF16P2_biomass_tr	ADG_extoc_tr	BDF16P2_biomass_tr
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C00002[e]	0	0	0	0	0	0	-1	0	0	0	0
C00008[c]	0	0	0	1	1	1	0	-1	0	0	1
C00008[e]	0	0	0	0	0	0	0	1	0	0	0
C00221[c]	0	0	0	-1	0	0	0	0	1	0	0
C00221[e]	0	0	0	0	0	0	0	0	-1	0	0
C00267[c]	0	0	0	0	-1	0	0	0	0	1	0
C00267[e]	0	0	0	0	0	0	0	0	0	-1	0
C00668[c]	-1	0	-1	0	1	0	0	0	0	0	0
C01172[c]	1	-1	0	1	0	0	0	0	0	0	0
C05345[c]	0	1	1	0	0	-1	0	0	0	0	0
C05378[c]	0	0	0	0	0	1	0	0	0	0	-1

Workflow to build a Path2Models whole genome reconstruction



Core

Fbc



KEGG-extract

MetaCyc-extract

Merge

Reconcile metabolite and reaction ids

Merge

Add growth medium

Add biomass components

Add Gene-Protein Relationships

Add flux bounds

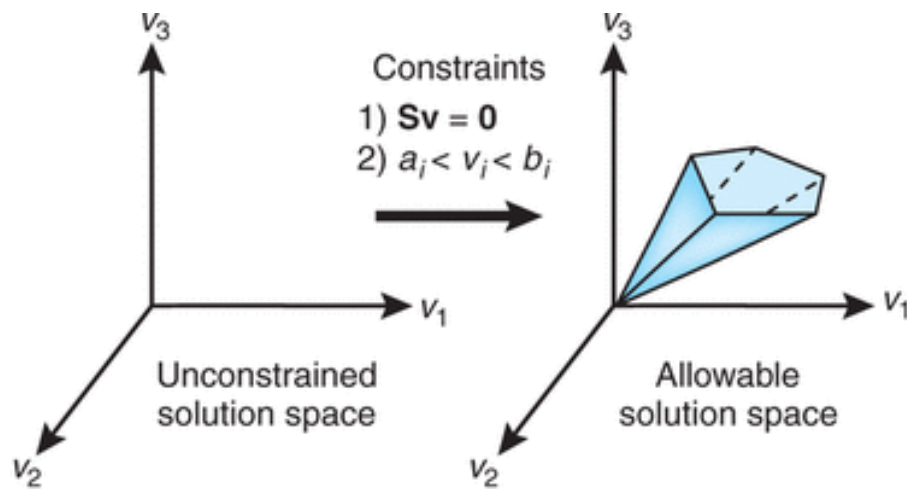
Format for COBRA

Draft

Steady-states:
Concentrations do not vary
Inputs = outputs

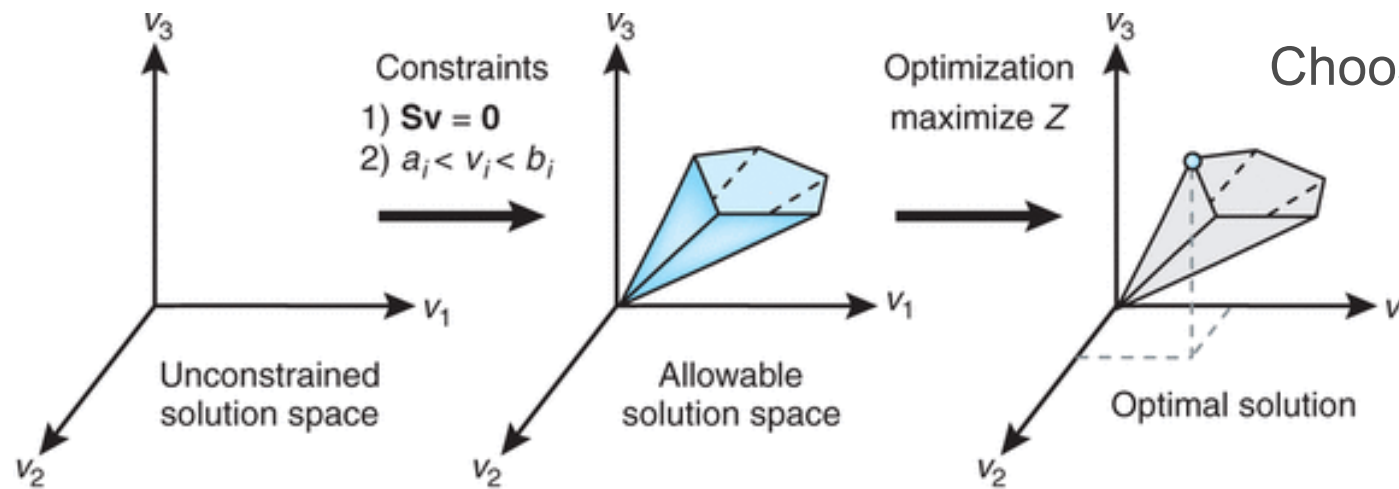
$$\mathbf{S} \begin{matrix} & \text{Reaction 1} & \text{Reaction 2} & \text{Reaction 3} & \text{Reaction 4} & \dots & \text{Reaction n} \\ \text{Reactant 1} & -1 & -1 & 0 & 0 & \dots & 1 \\ \text{Reactant 2} & 0 & -1 & 0 & -2 & \dots & 0 \\ \text{Reactant 3} & -1 & 1 & -1 & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots & \dots & \dots \\ \text{Reactant m} & 2 & 0 & 1 & 0 & \dots & 0 \end{matrix} \times \begin{matrix} \mathbf{V} \\ \text{Flux 1} \\ \text{Flux 2} \\ \text{Flux 3} \\ \text{Flux 4} \\ \dots \\ \text{Flux n} \end{matrix} = \mathbf{0}$$

More reactions than reactants = undetermined (more variables than equations)



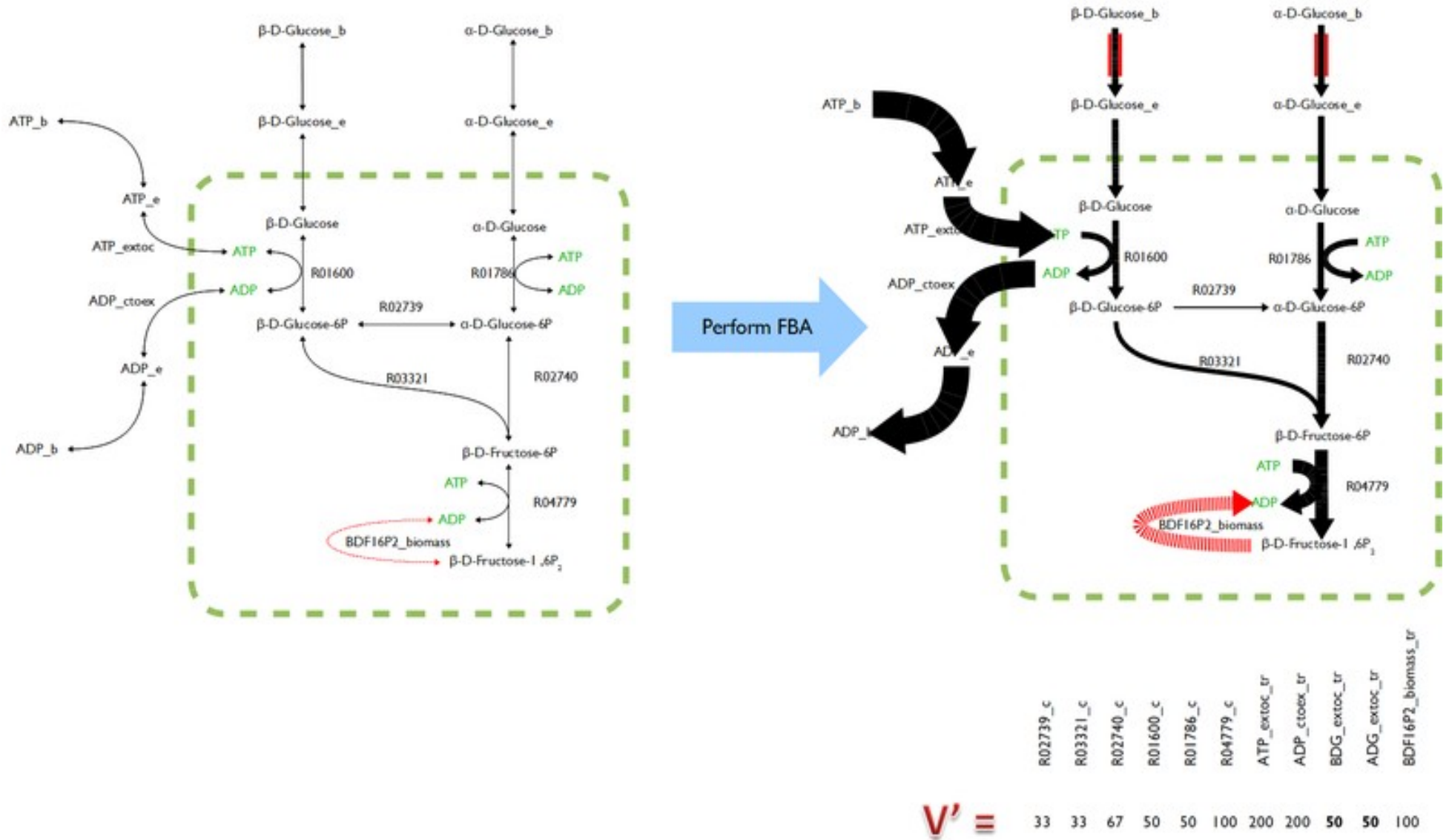
$$\begin{array}{c} \mathbf{S} \\ \text{Reactant 1} \\ \text{Reactant 2} \\ \text{Reactant 3} \\ \dots \\ \text{Reactant m} \end{array} \begin{array}{c} \text{Reaction 1} \\ \text{Reaction 2} \\ \text{Reaction 3} \\ \text{Reaction 4} \\ \dots \\ \text{Reaction n} \end{array} \begin{pmatrix} -1 & -1 & 0 & 0 & \dots & 1 \\ 0 & -1 & 0 & -2 & \dots & 0 \\ -1 & 1 & -1 & 0 & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots & \dots \\ 2 & 0 & 1 & 0 & \dots & 0 \end{pmatrix} \times \begin{array}{c} \mathbf{v} \\ \text{Flux 1} \\ \text{Flux 2} \\ \text{Flux 3} \\ \text{Flux 4} \\ \dots \\ \text{Flux n} \end{array} = 0$$

More reactions than reactants = undetermined (more variables than equations)

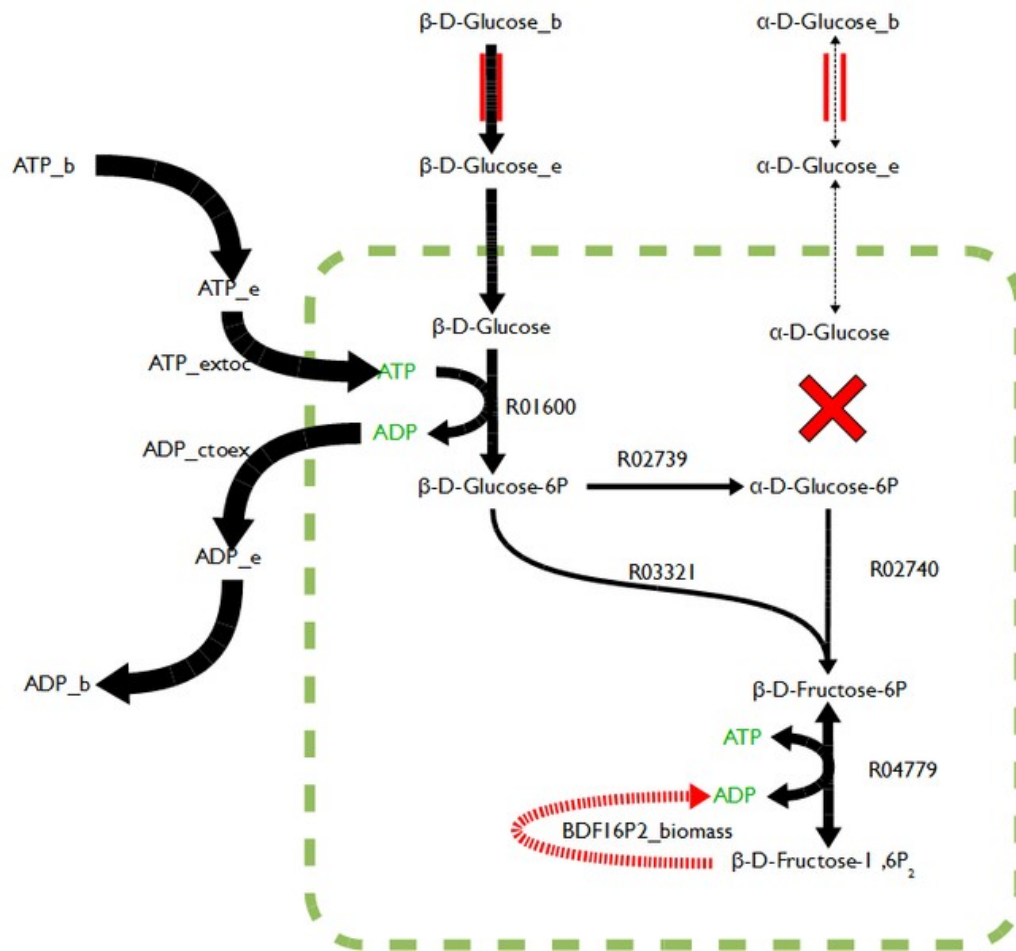


Choose an objective function
(maximise biomass
or ATP production)

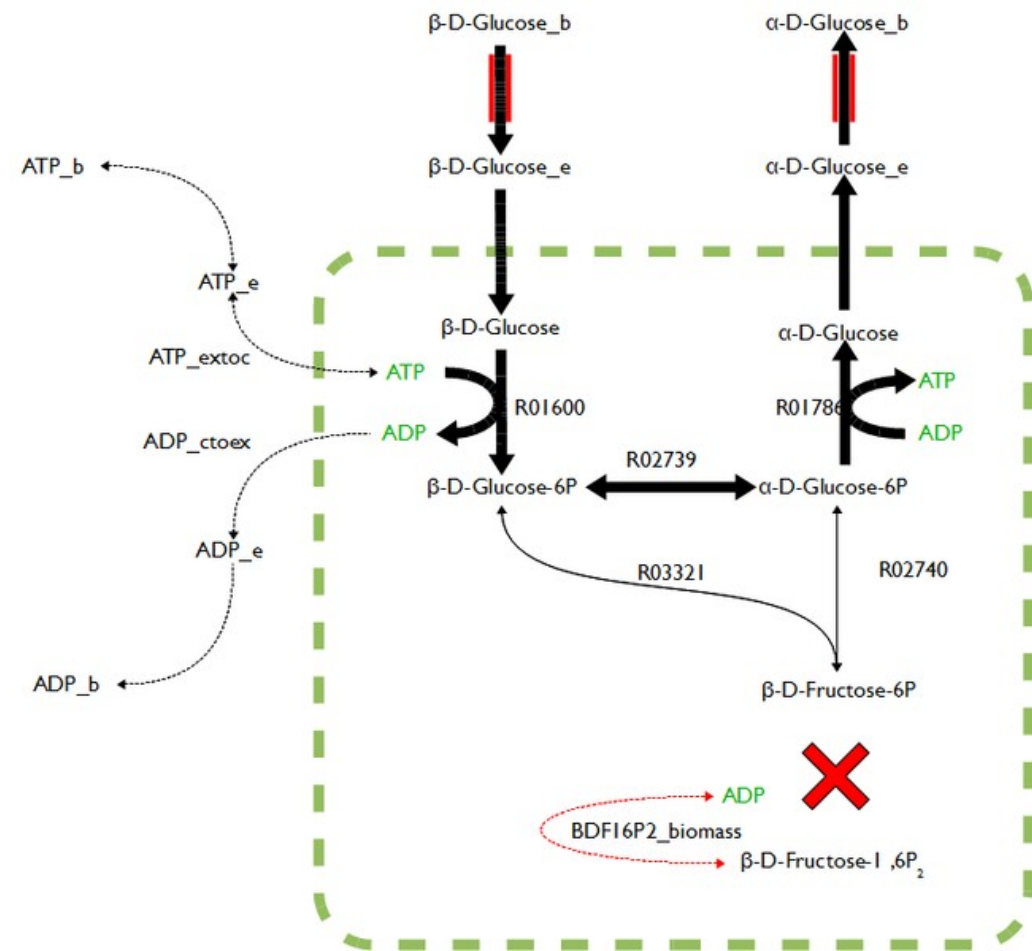
Application of FBA



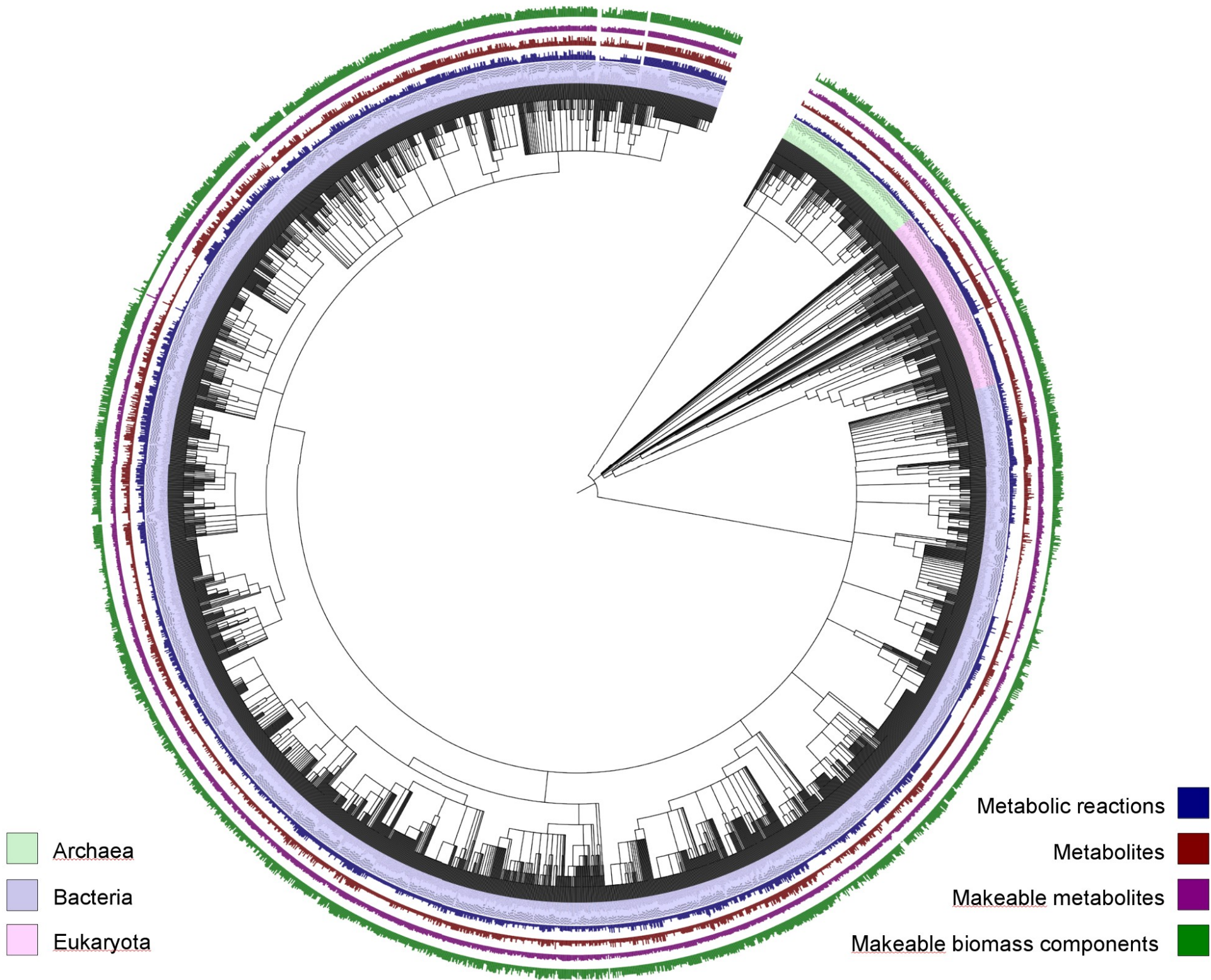
Perturbations

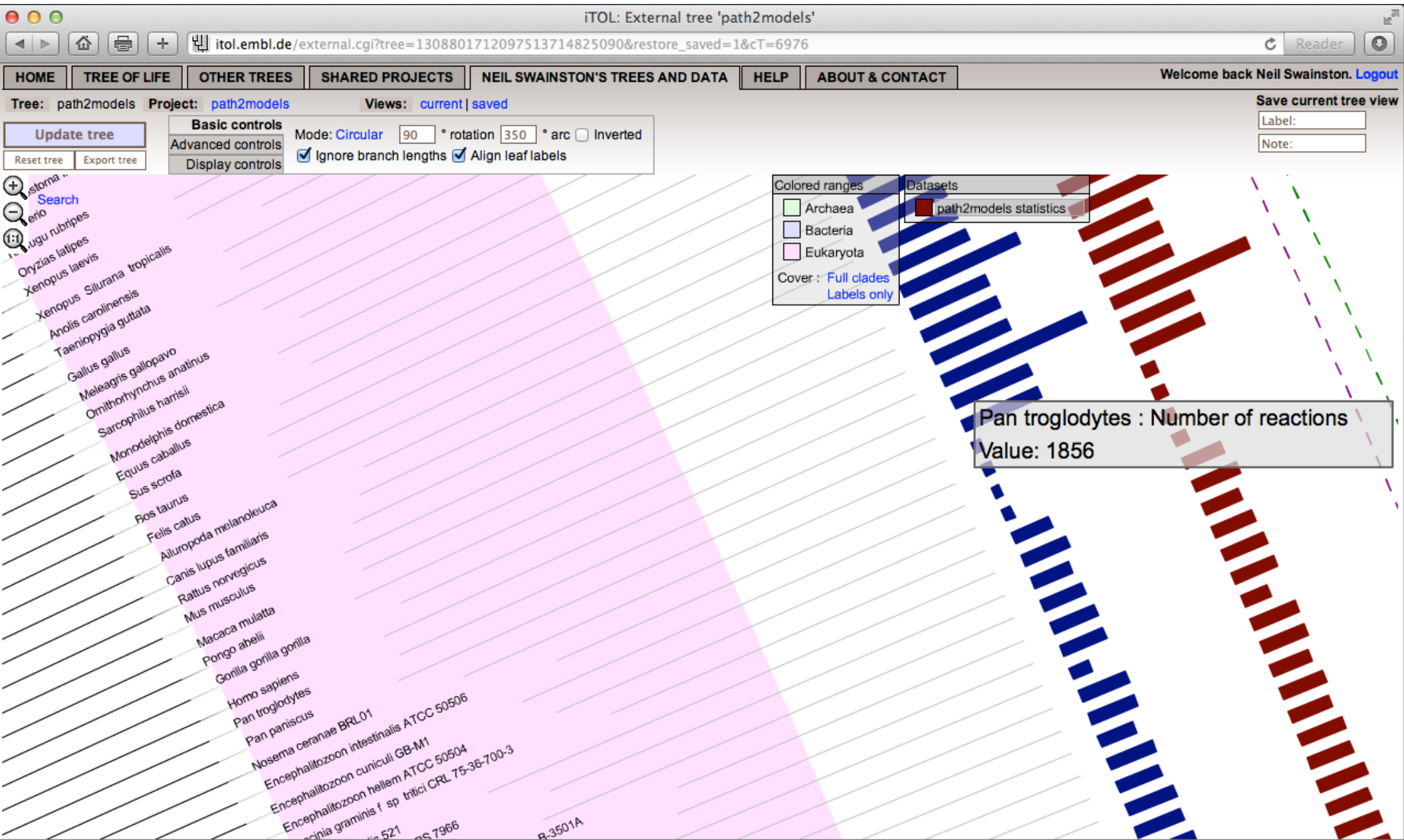


Non-lethal mutation

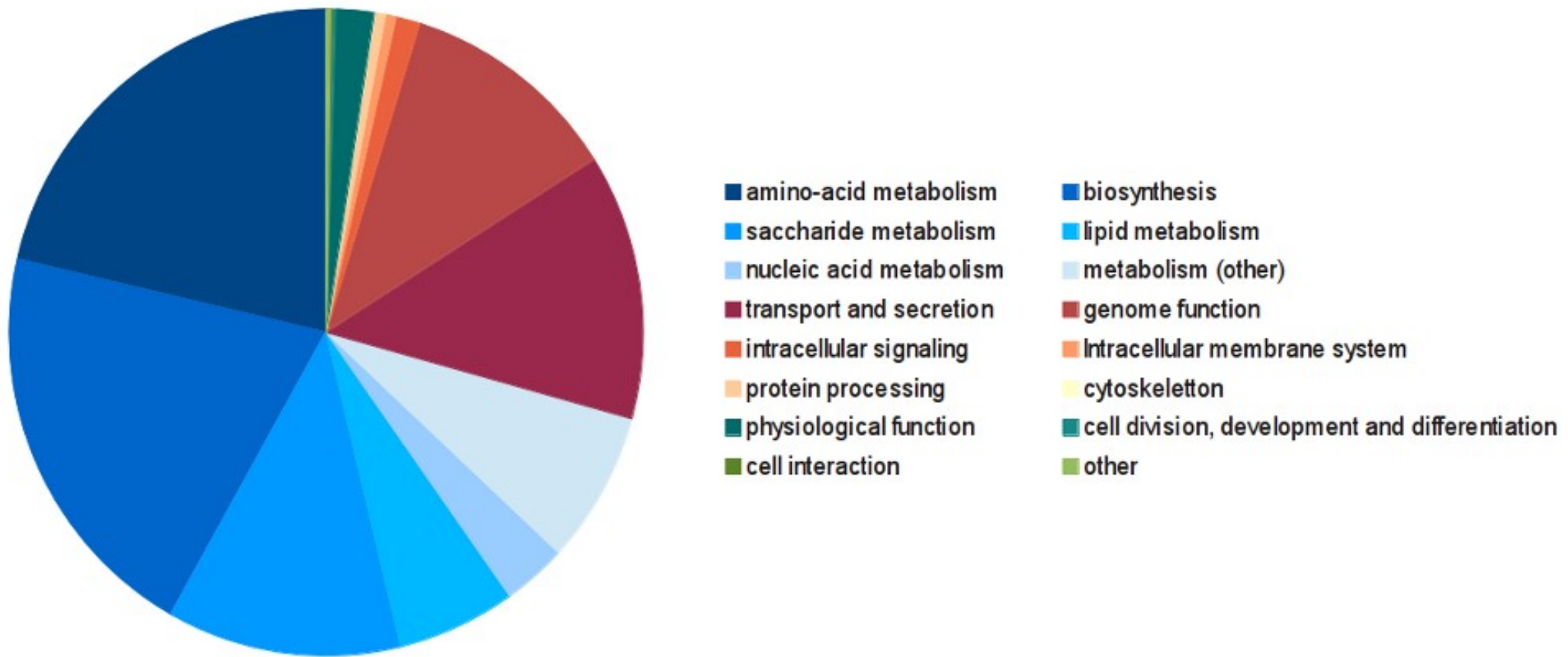


lethal mutation

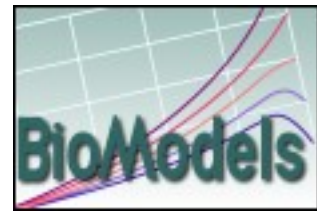




Gene Ontology Coverage



26th BioModels Database release



- October 2013 – 5th release of Path2Models data
- 112 898 common modular rate law models of metabolic networks
- 27 306 qualitative models of signalling pathways
- 2 630 whole genome flux balance analysis models
- 12 280 007 mathematical relations
- 432 154 677 cross references
- <http://www.ebi.ac.uk/biomodels-main/path2models>

Inositol phosphate metabolism - Mus musculus

[Download SBML](#)[Additional files](#)[Send feedback](#)

Model information

Identifier: BMID000000038685**Format:** SBML L3 V1 (Layout)**Project:** [path2models](#)**Categories:** [metabolic](#)**Submission:** 17 May 2012 22:37:29 UTC**Last modified:** 10 Dec 2012 03:55:58 UTC**Published:** 19 May 2012 23:49:21 UTC

Annotations

isDescribedBy[inositol metabolic process](#)**occursIn**[Mus musculus](#)**isDerivedFrom**[Inositol phosphate metabolism](#)[Gene Ontology](#)[Taxonomy](#)[KEGG Pathway](#)

Model of "Inositol phosphate metab

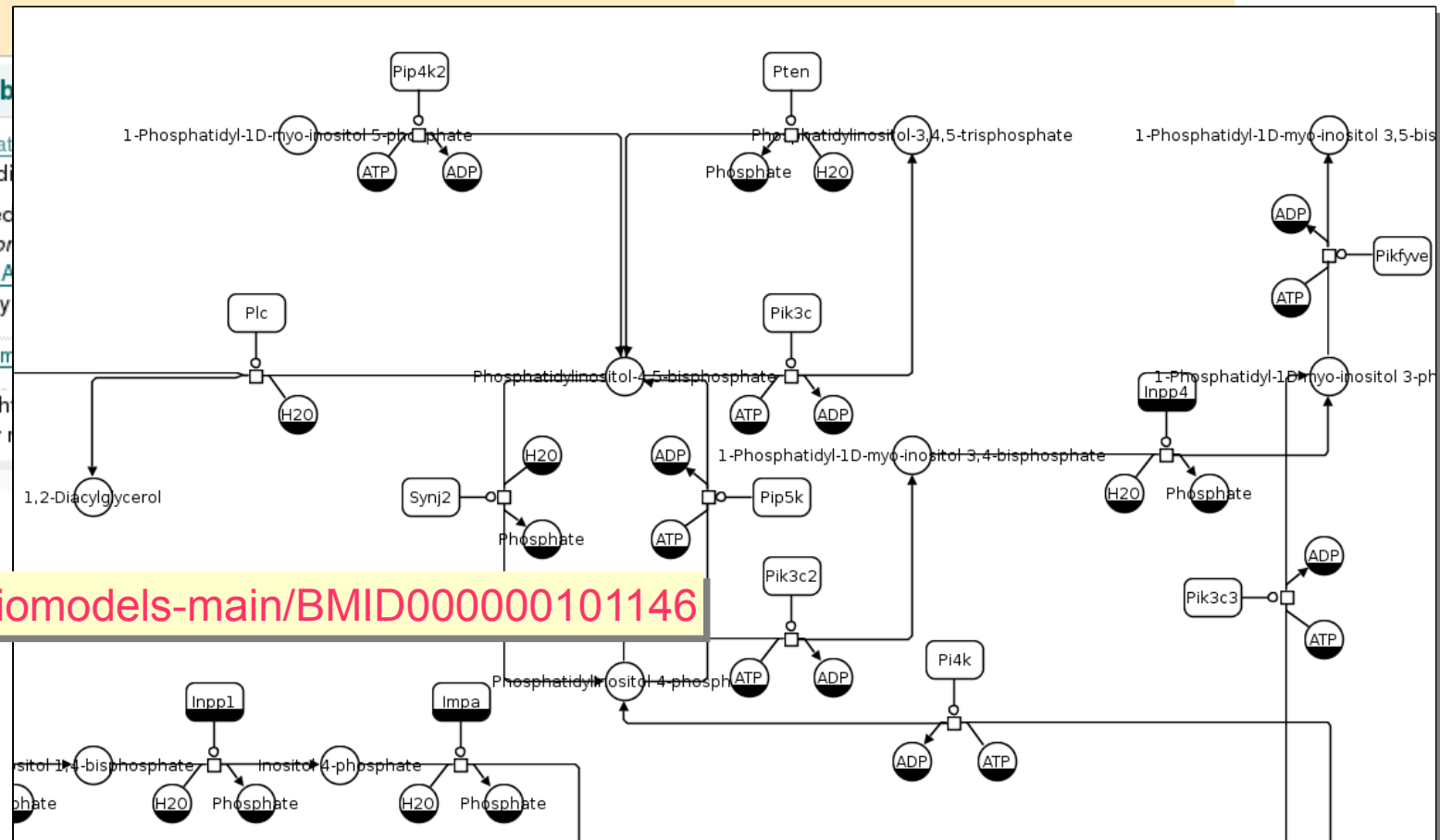
Graphical representation of 'Inositol phosphat

(PNG image hosted by the Kyoto Encyclop

This model has been automatically generated
formats. Wrzodek C, Dräger A, Zell A. *Bioinform*
Some kinetic information were added from [SA](#)
The missing kinetic equations were added by

This model has been produced by the [path2m](#)

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<http://www.ebi.ac.uk/biomodels-main/BMID000000101146>

What can I do with Path2Models?





Mihai Glont
Henning Hermjakob
Sarah Keating
Camille Laibe
Nicolas Rodriguez
Julio Saez-Rodriguez
Martijn van Iersel
Michael Schubert



Andreas Dräger
Roland Keller
Matthias Rall
Clemens Wrzodek
Andreas Zell
Finja Bünel
Florian Mittag



Douglas Kell
Pedro Mendes
Neil Swainston



Claudine Chaouya



Falk Schreiber
Tobias Czauderna

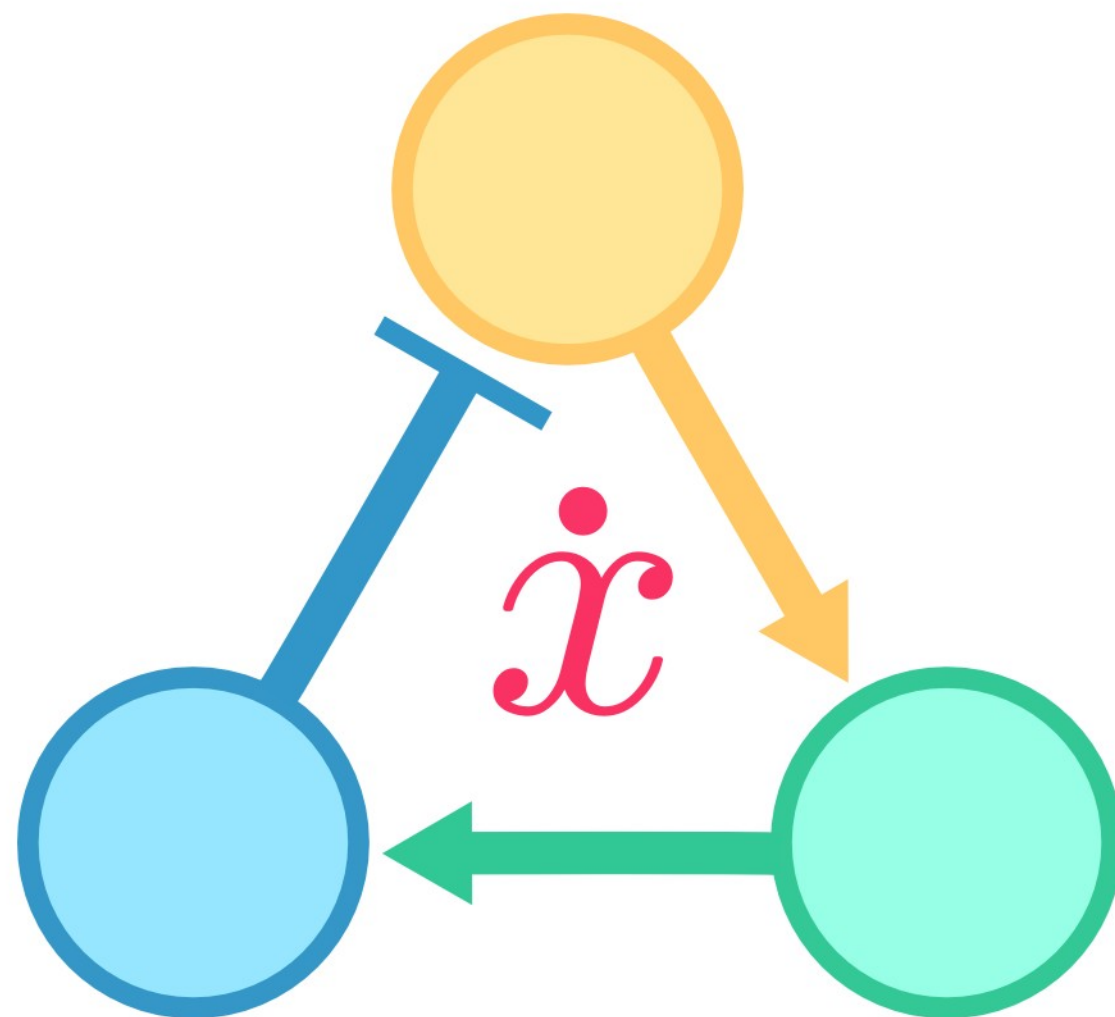
Heidelberg Institute for
Theoretical Studies



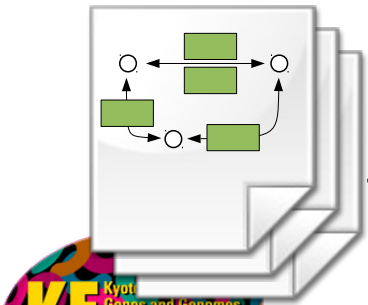
Martin Golebiewski
Wolfgang Müller



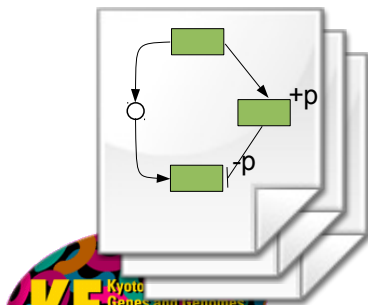
Michael Hucka



1515 species



Metabolic Networks
116 000



Signalling
Pathways
(30333)



SBML
core



SBML
qual

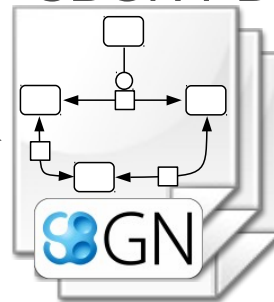


Whole genome
reconstructions

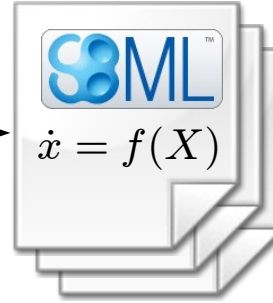
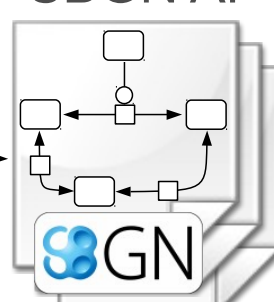


SBML core

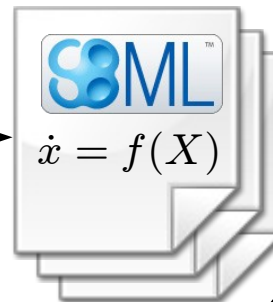
SBGN PD



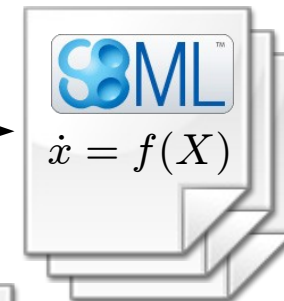
SBGN AF



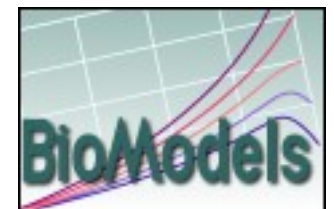
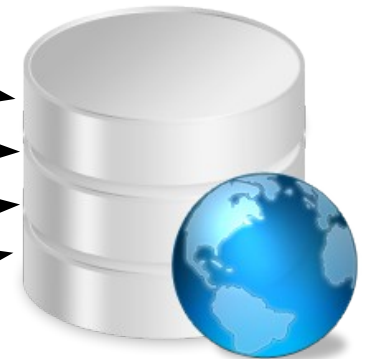
Modular
Rate-law
(112898)



Logical
Models
(27306)



SBML fbc
(1846)



<http://www.ebi.ac.uk/biomodels-main/path2models>